



*Cosmic Rays,
interstellar
voyagers*

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how do cosmic rays travel?

how do they disperse?

how fast do they travel?

wicked facts & beautiful models

super rays to reveal gas



Popular Science MONTHLY

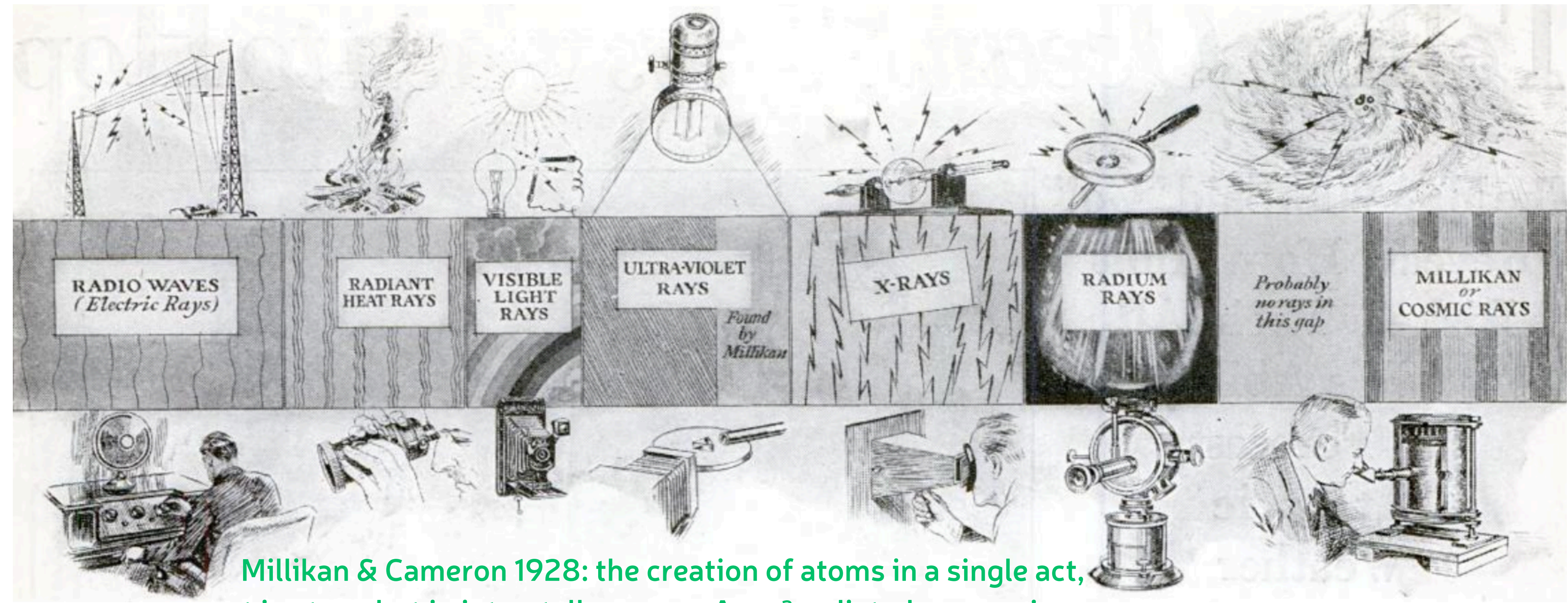


JULY, 1928

SUMNER BLOSSOM *Editor*

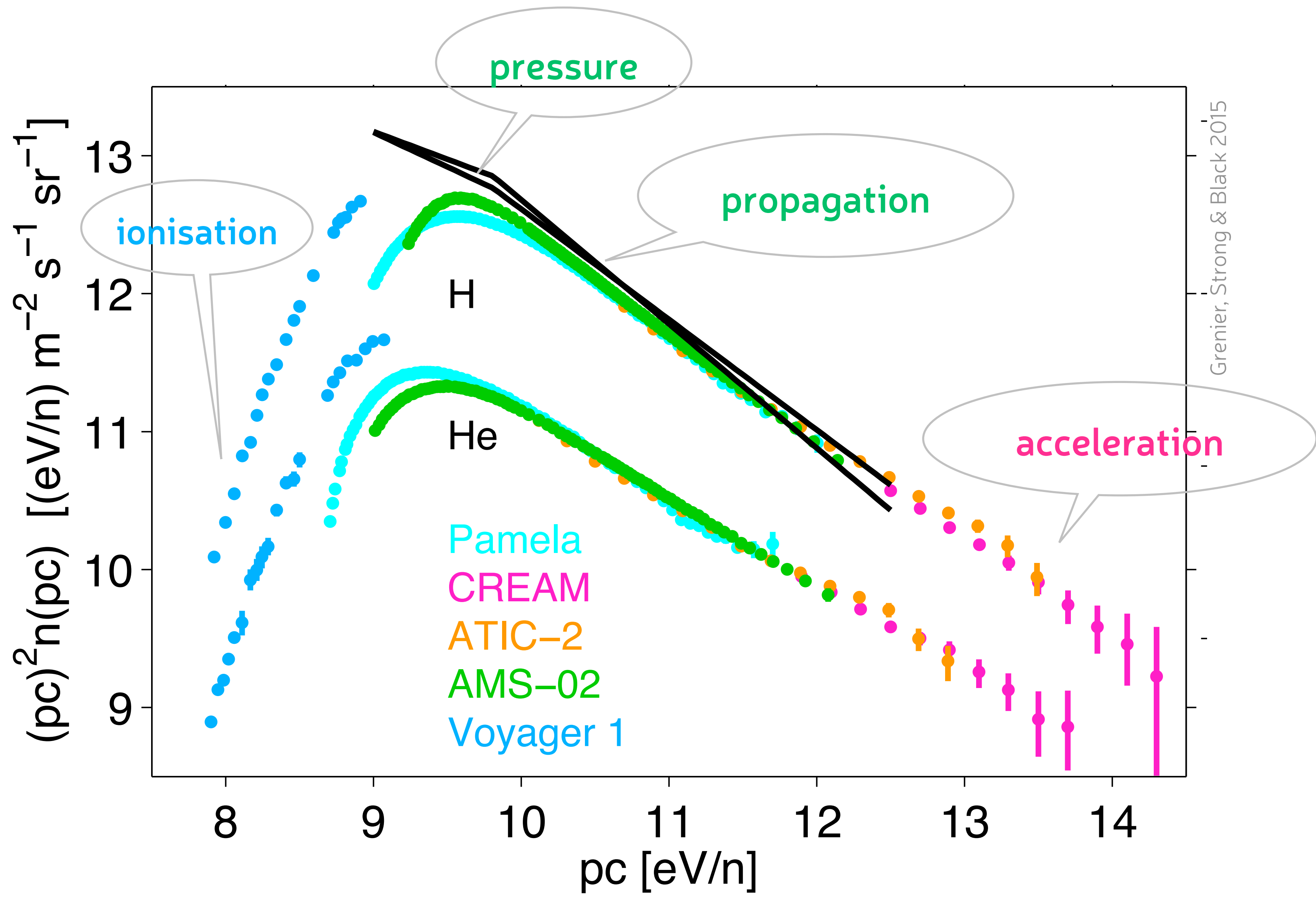
VOL. 113, NO. 1

Super-Rays Reveal Secret of Creation



Millikan & Cameron 1928: the creation of atoms in a single act, not in stars, but in interstellar space, $\Delta m c^2$ radiated as cosmic rays

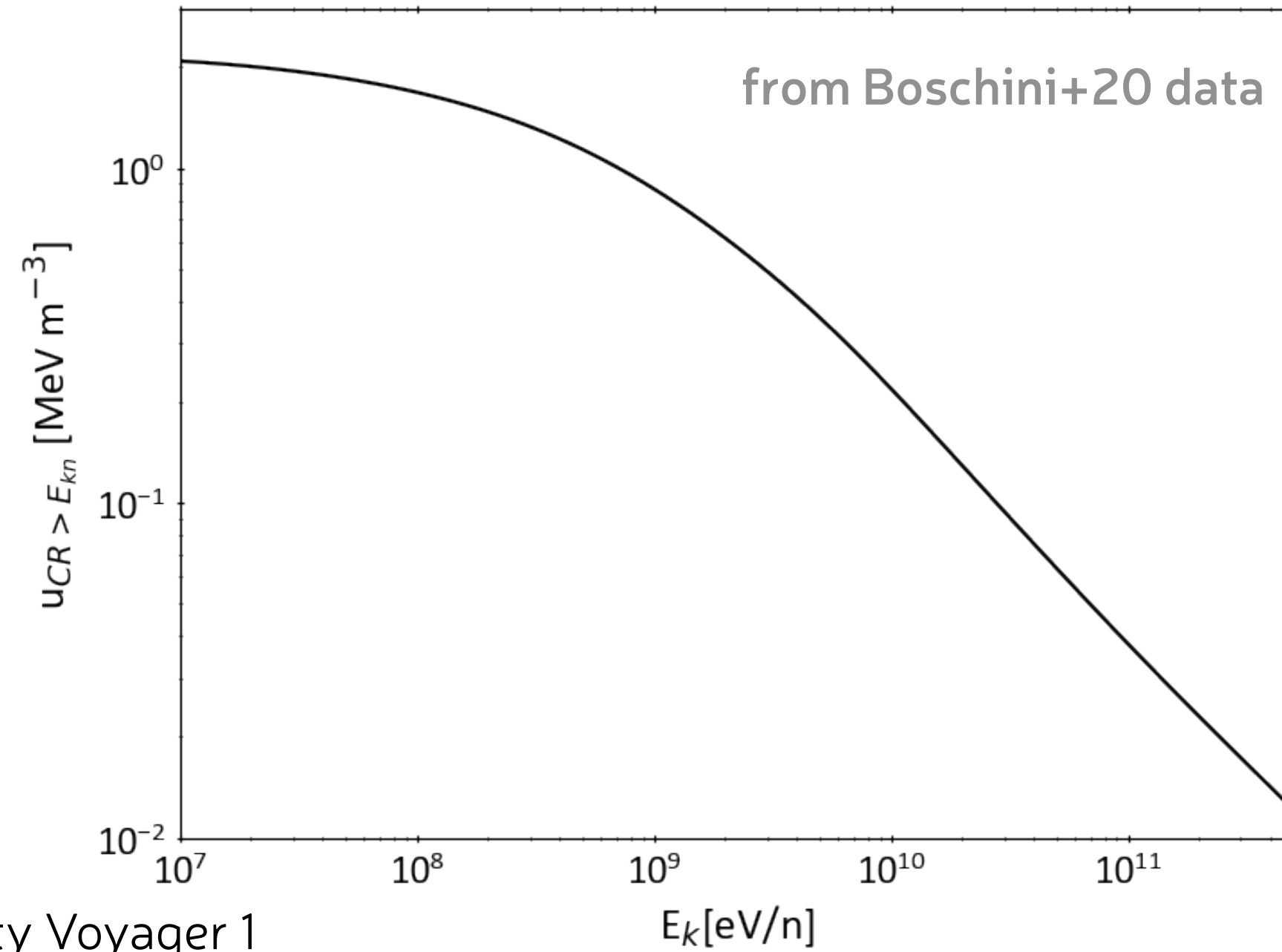
which energy for what?



local cosmic-ray energy density

- Voyager 1 nuclei+e > 3 MeV/n : $u_{CR} = 0.83 - 1.02 \text{ MeV m}^3$ Cummings+2016
- heliosphere demodulated spectra $u_{CR} \approx 2 \text{ MeV m}^3$

local energy equipartition

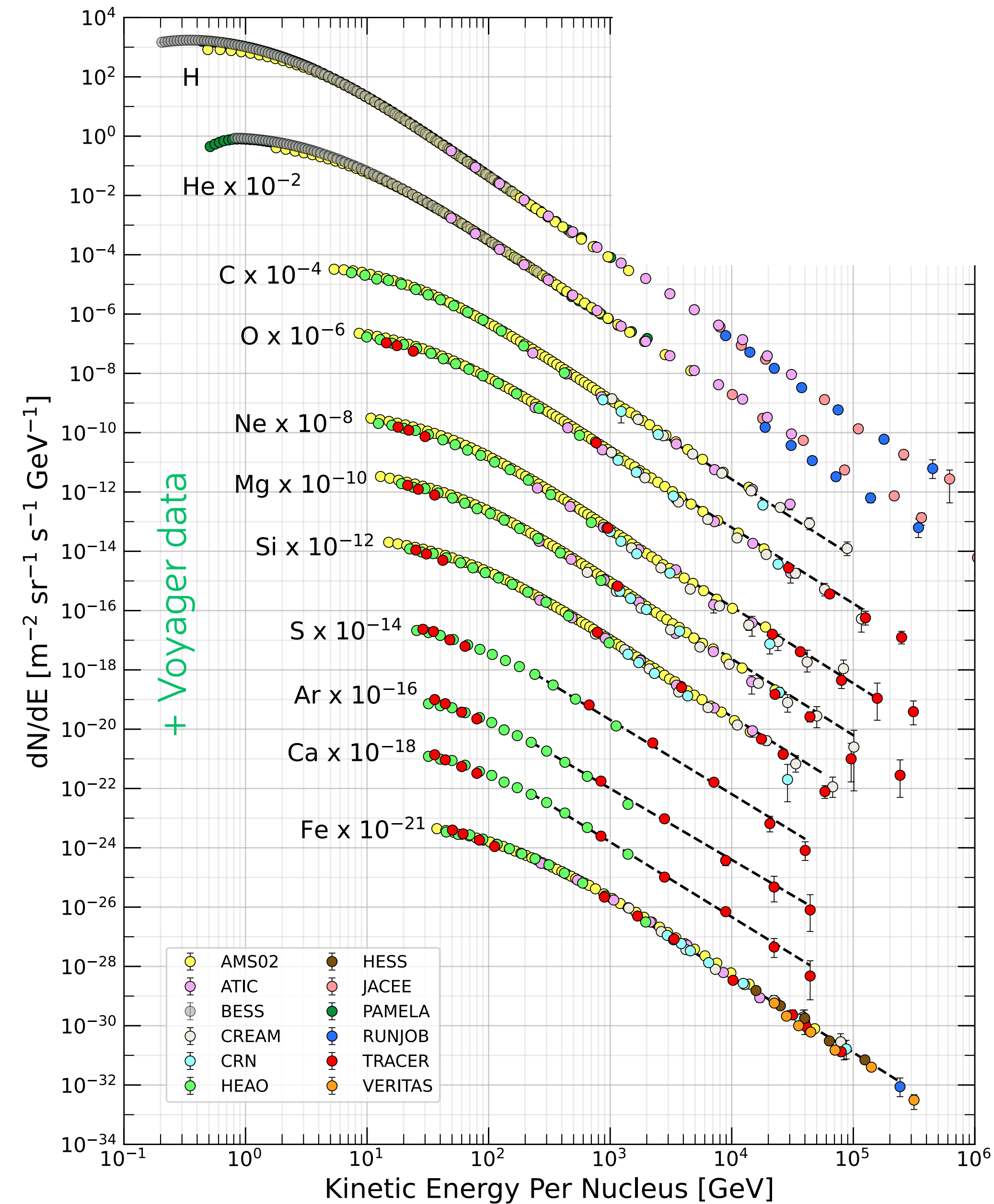


- local magnetic-field energy density Voyager 1
 - $B_{tot} = (0.56 \pm 0.01) \text{ nT} \Rightarrow B^2/2\mu_0 = 0.78 \pm 0.03 \text{ MeV m}^3$
- local gas pressure $\frac{p}{k} = \frac{N}{V}T = 10^{3.58 \pm 0.175} \text{ K cm}^{-3}$ Jenkins & Tripp 2011
- so $u_{th} = 0.49^{+0.24}_{-0.16} \text{ MeV m}^{-3}$
- turbulent kinetic energy densities Hard & Kalberla 2007

CNM: $\frac{1}{2}\rho\sigma_v^2 = 0.6 \text{ MeV m}^{-3} \left(\frac{n_{HI}}{30 \text{ cm}^{-3}}\right) \left(\frac{\sigma_{vHI}}{1.7 \pm 0.3 \text{ km/s}}\right)^2$

LNM: $\frac{1}{2}\rho\sigma_v^2 = 0.5 \text{ MeV m}^{-3} \left(\frac{n_{HI}}{3 \text{ cm}^{-3}}\right) \left(\frac{\sigma_{vHI}}{5.0 \pm 0.2 \text{ km/s}}\right)^2$

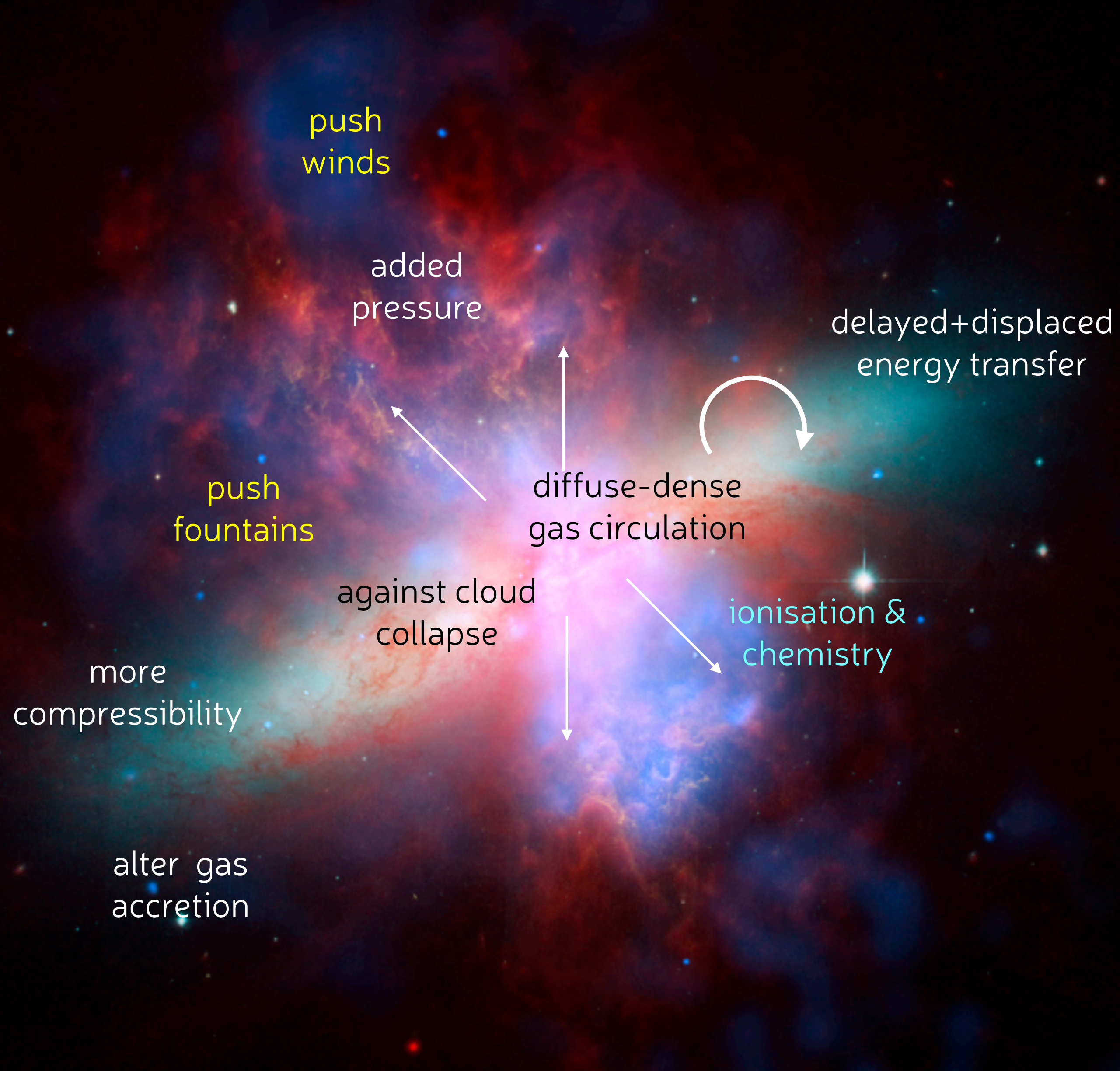
WNM: $\frac{1}{2}\rho\sigma_v^2 = 0.4 \text{ MeV m}^{-3} \left(\frac{n_{HI}}{0.5 \text{ cm}^{-3}}\right) \left(\frac{\sigma_{vHI}}{10.3 \pm 0.3 \text{ km/s}}\right)^2$



cosmic-ray feedback on galaxy evolution

\gtrsim GeV CRays
self or interstellar
confinement?
diffusion coeff $\kappa(E)$?
how uneven $\kappa(E)$?
halo extent?

> 100 TeV CRay
acceleration?
sources?



GeV CRays
as gas tracers

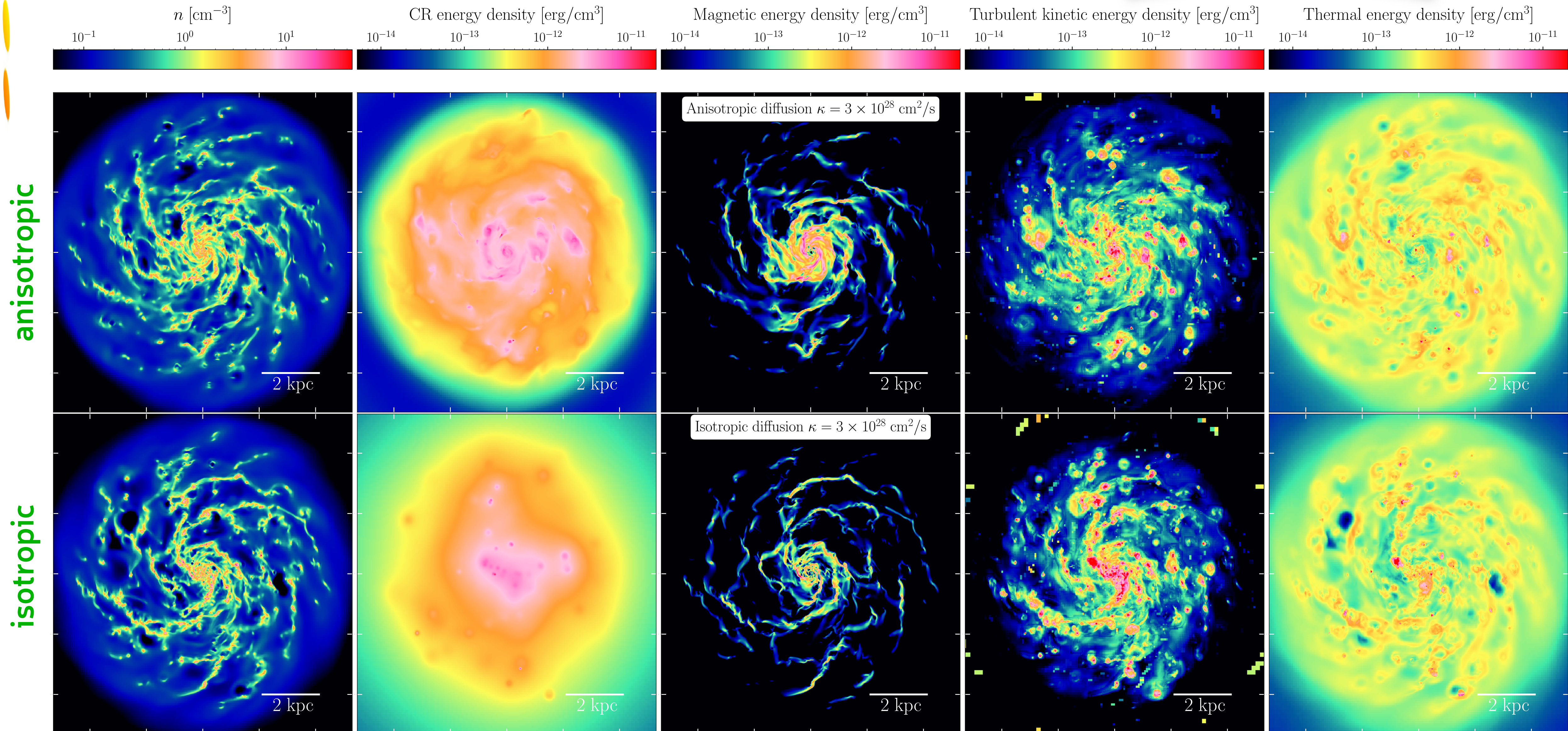
< 100 MeV CRays
sources?
diffusion properties?
why strong variations?

gas-rich dwarf galaxies

- $M_{\text{tot}} = 10^{11} M_{\odot}$, $M_{\text{b}} = 10^9 M_{\odot}$, $\text{SFR} \sim 1 M_{\odot} / \text{yr}$, starting from smooth gas & smooth B
- multiphasic gas down to 9-pc resolution, ideal MHD with RAMSES

$3 \times 10^{28} \text{ m}^2/\text{s}$

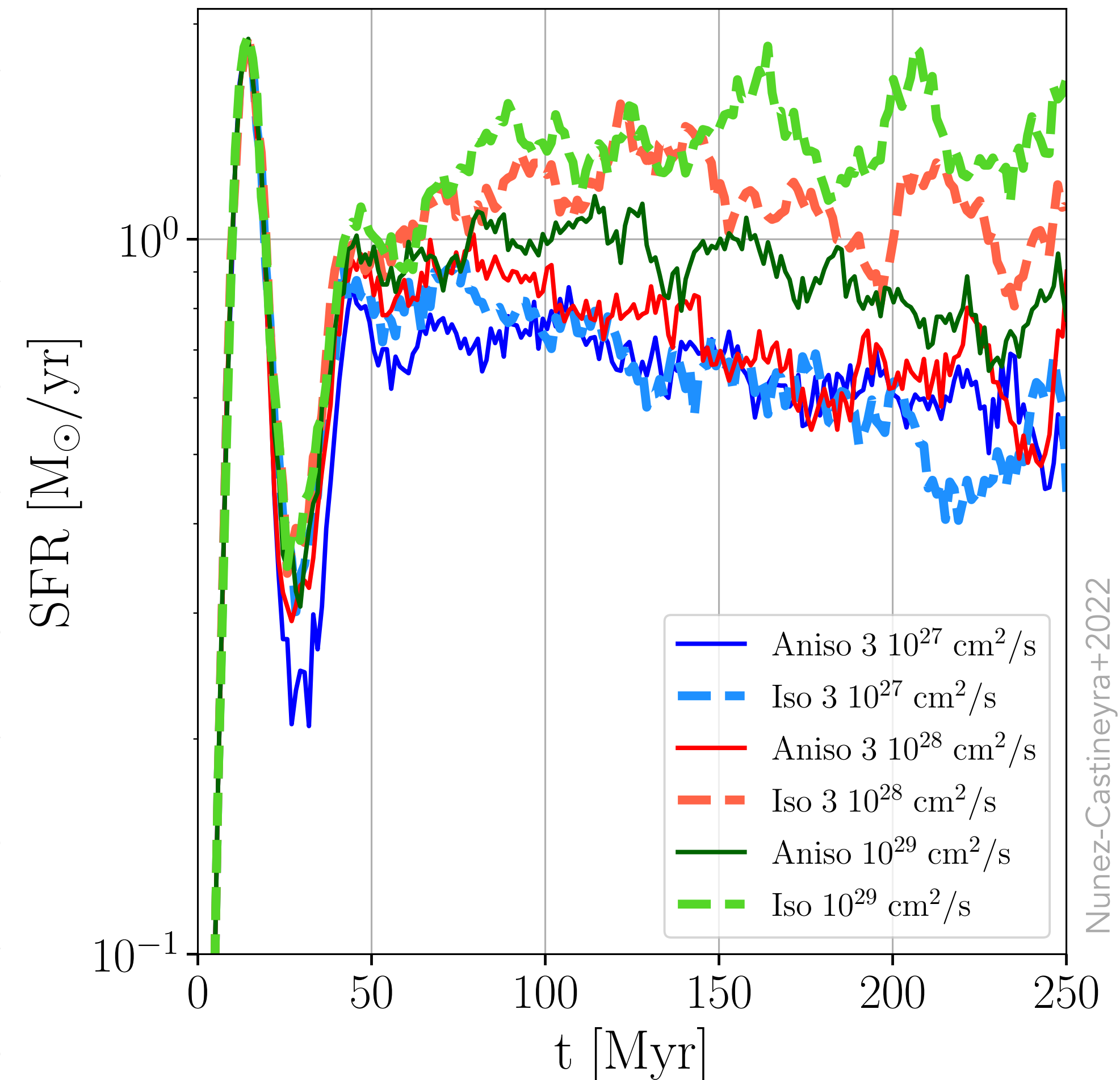
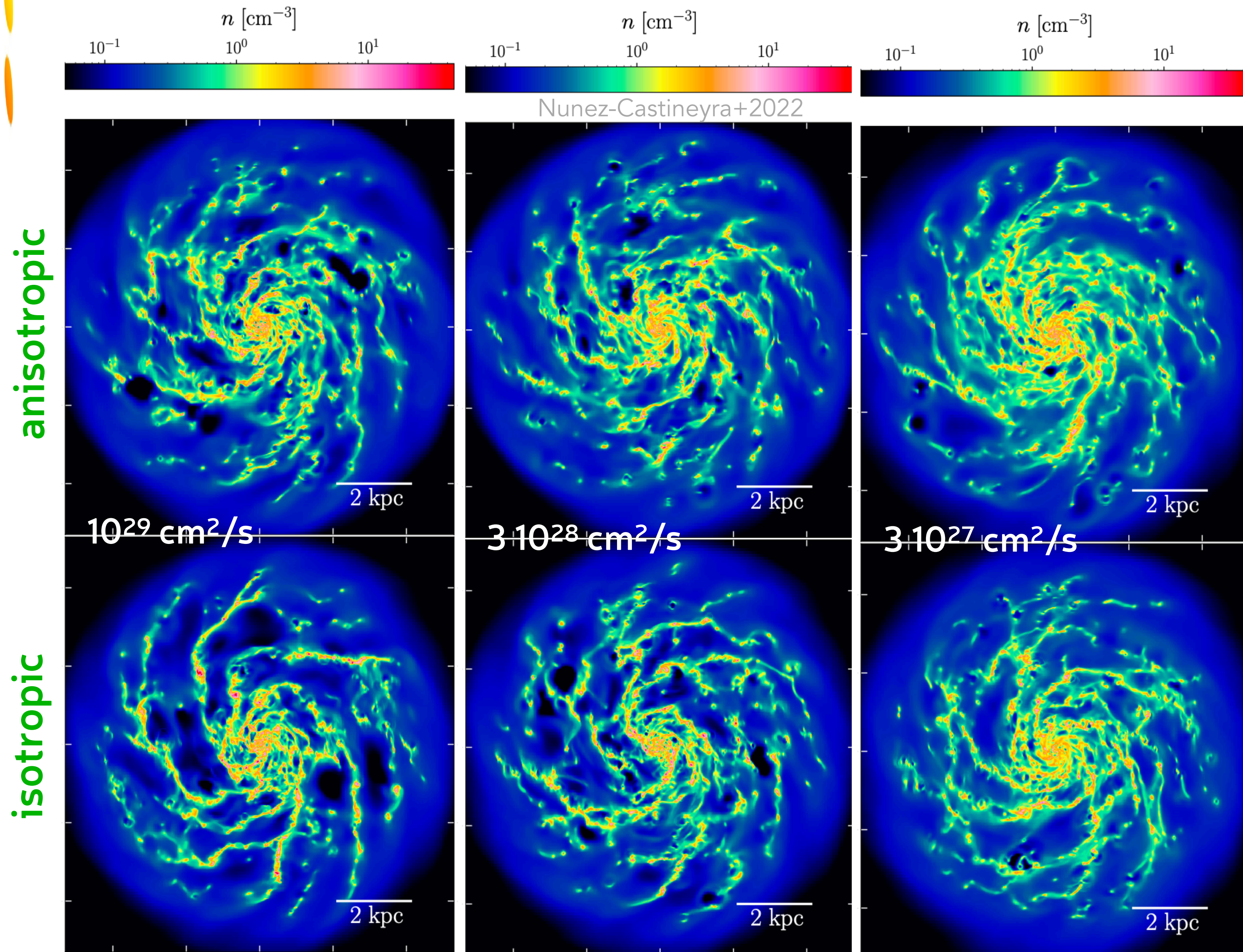
$U_{\text{turb}} \& U_{\text{CR}} > U_{\text{therm}} \& U_{\text{B}}$
on 100- 200 pc scales



gas & star-formation response to cosmic rays

- $R > 2$ kpc : increased P_{CR} pressure => SFR suppressed by $< 50\%$
- $R < 2$ kpc : increased P_{CR} and $\langle B \rangle \times 3.5$ where $e_{CR} \gtrsim 1-2$ eV/cm³ => SFR suppressed by 2.5
- not SN-induced turbulence, but role of increased fountains? gal. wind?

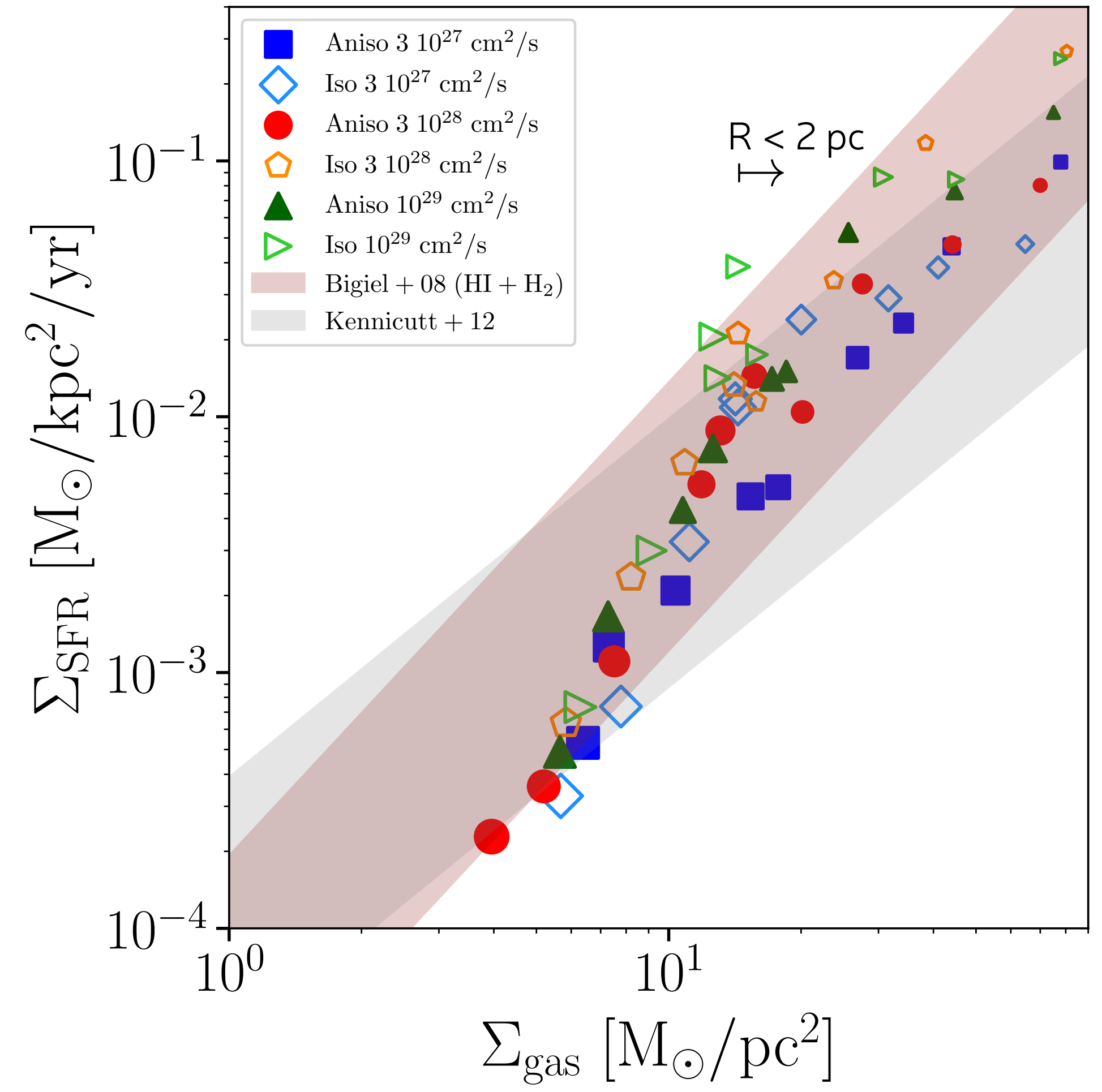
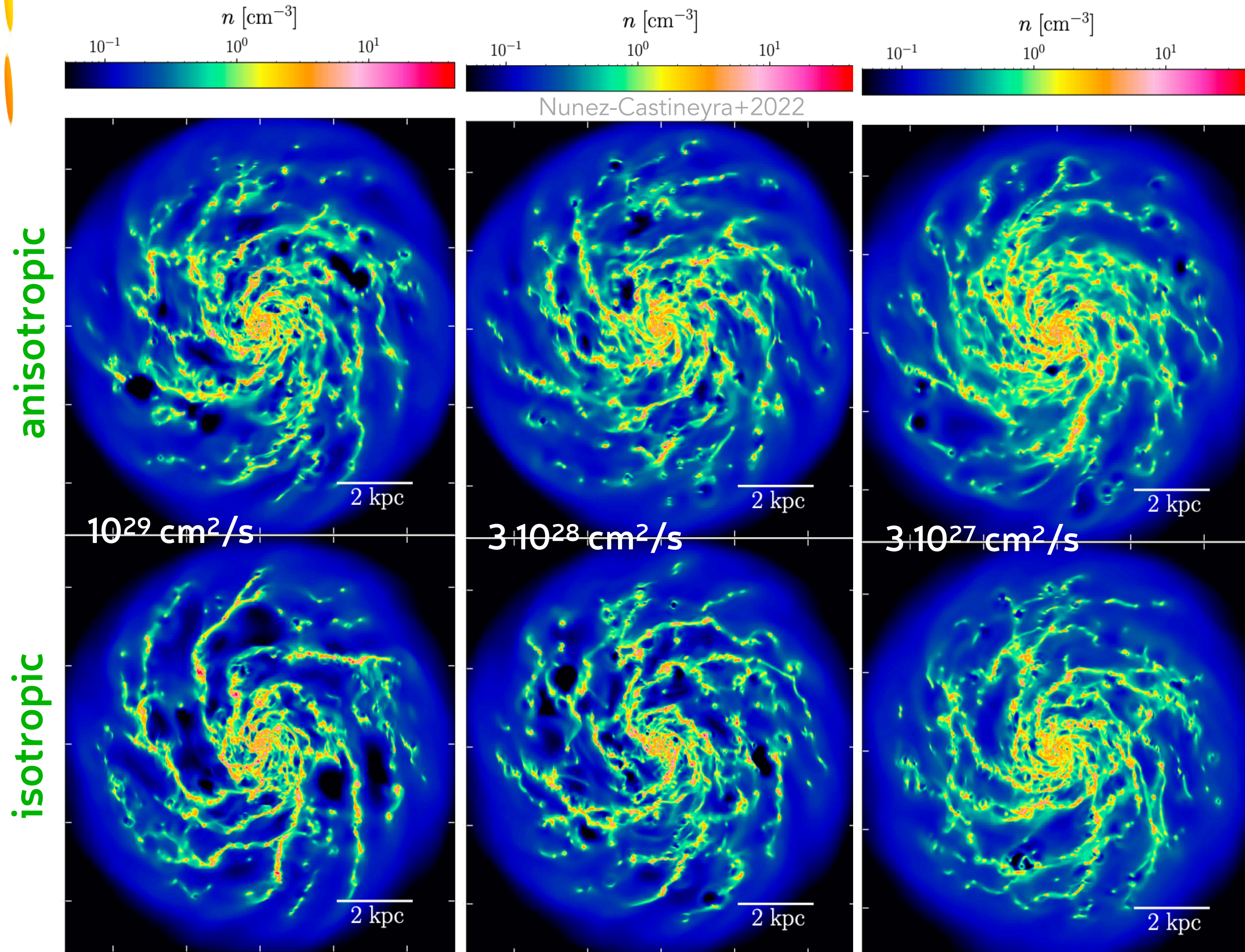
smoother gas & suppressed SFR
if slow/anisotropic CR diffusion



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low-energy,
ionising
cosmic rays

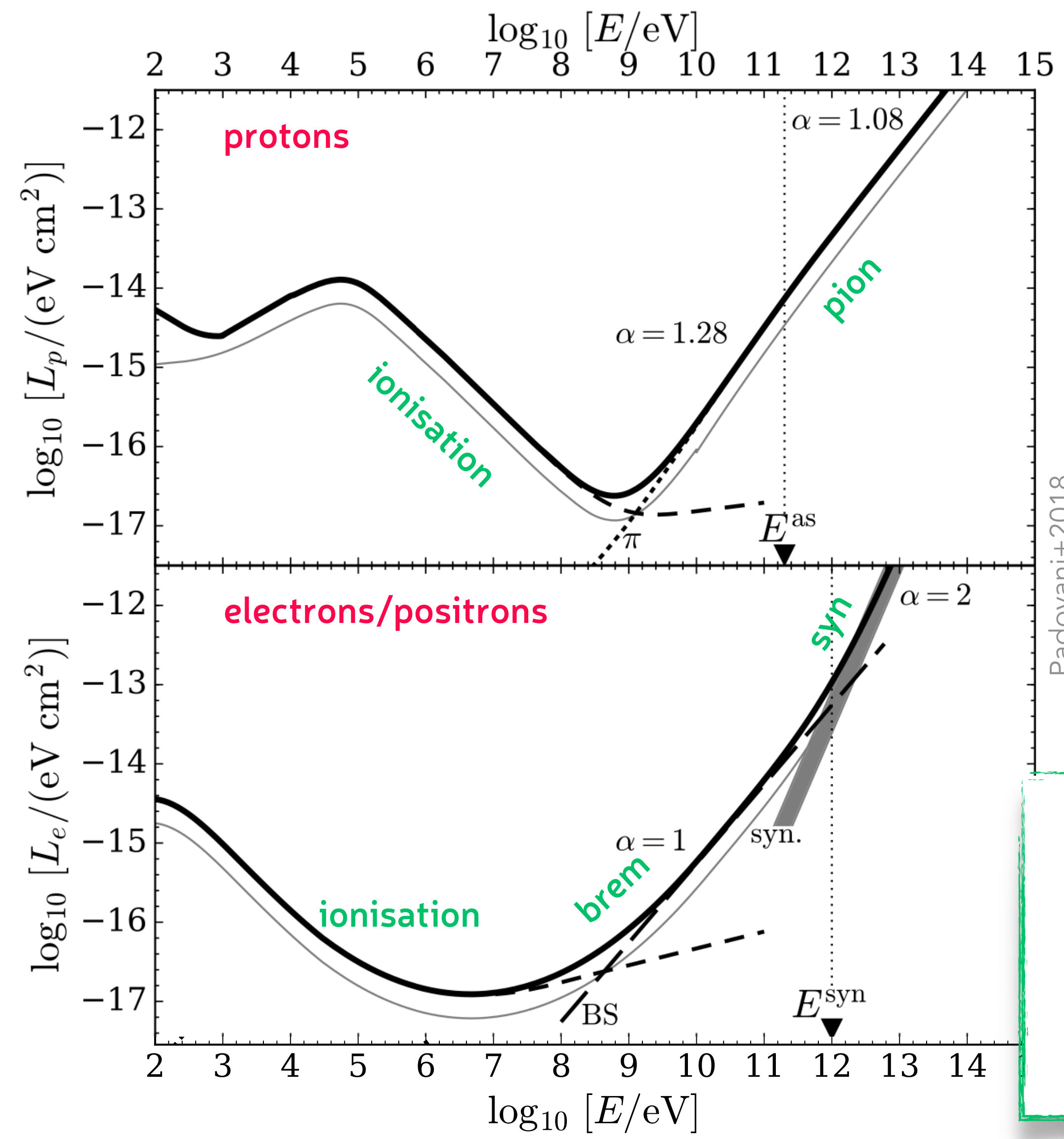


● loss functions

$$\left\{ \begin{array}{l} \text{continuous loss } L(E) = \int_0^{\Delta E_{max}} E' \frac{d\sigma(E, E')}{dE'} dE' \\ \text{catastrophic loss } L(E) \sim E\sigma(E) \end{array} \right.$$

● range functions

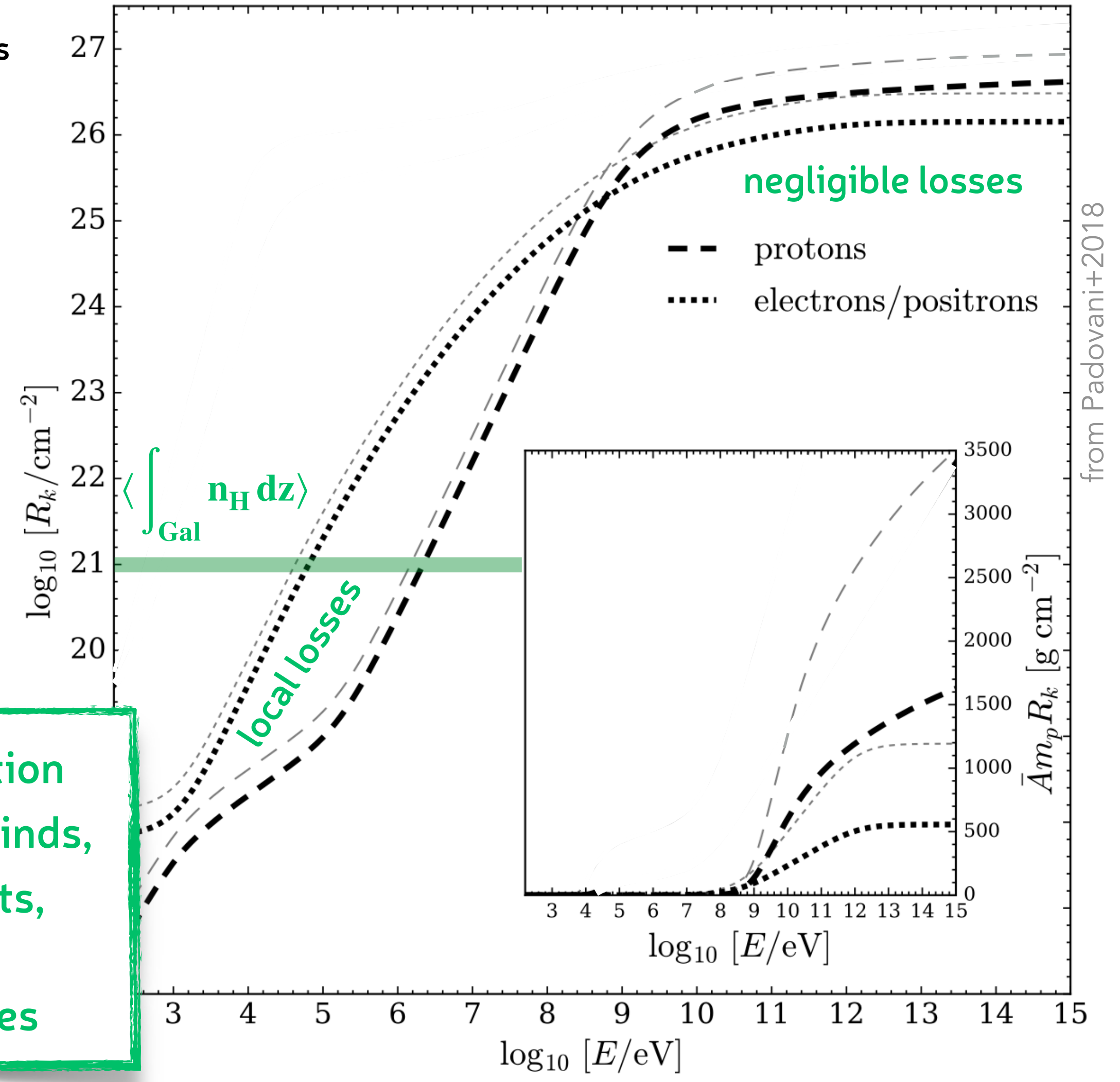
$$\int_s n_{ISM} ds = R_k(E_{initial}) - R_k(E_{final})$$



in molecular gas (thick curves)
 in atomic gas (thin curves)

Padovani+2018

**local production
 (star flares+winds,
 protostar jets,
 shocks...)
 & local losses**

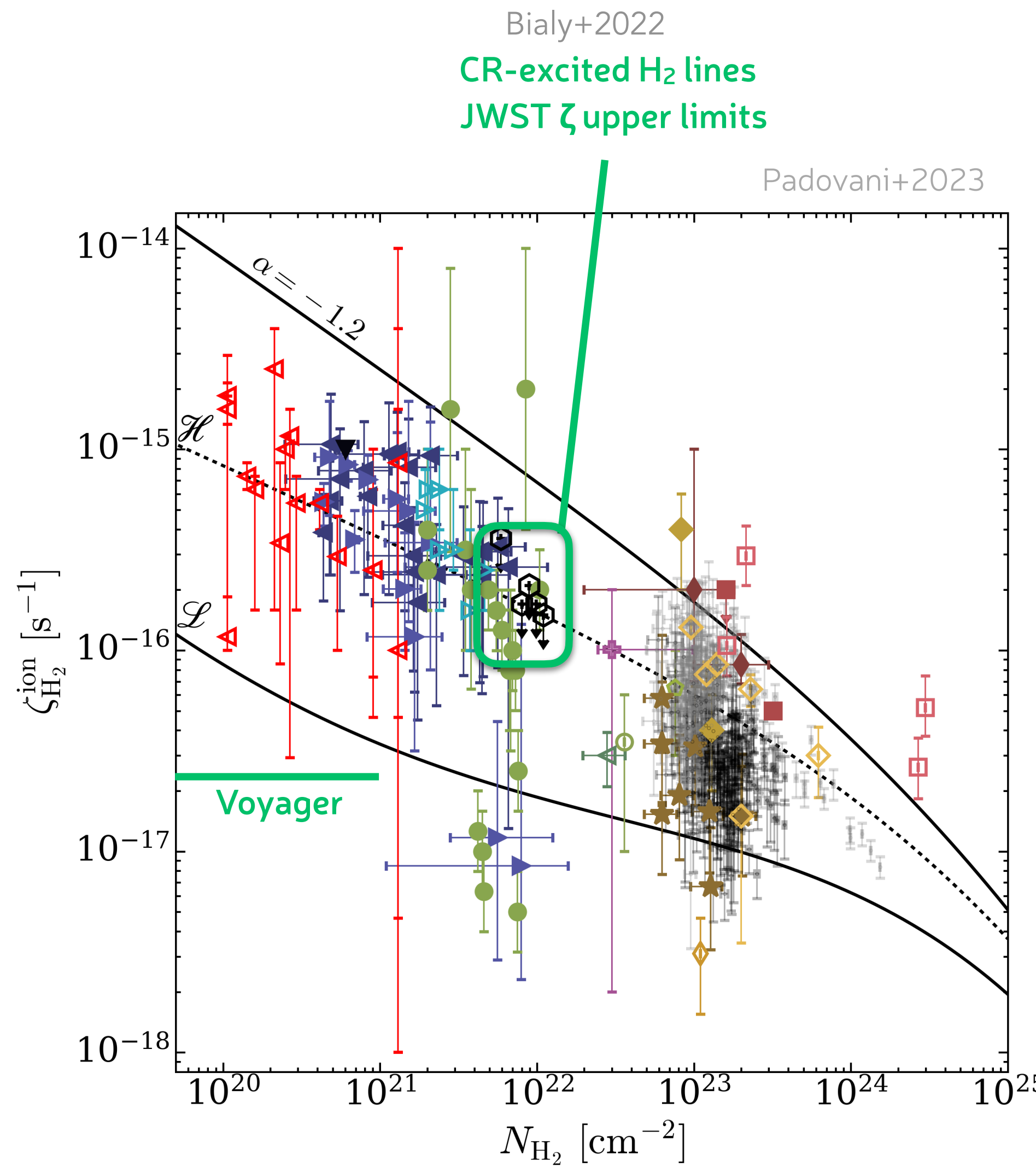
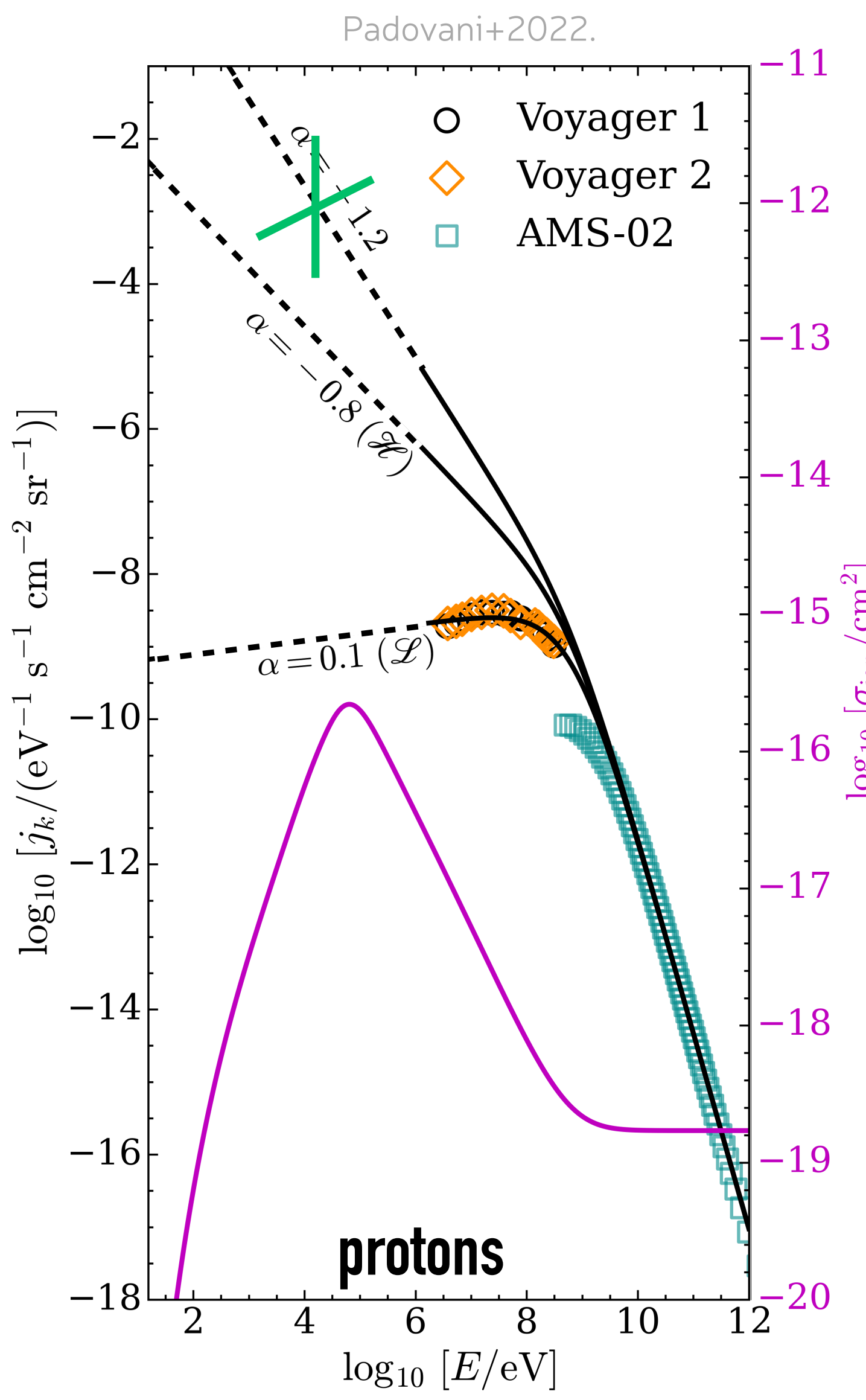
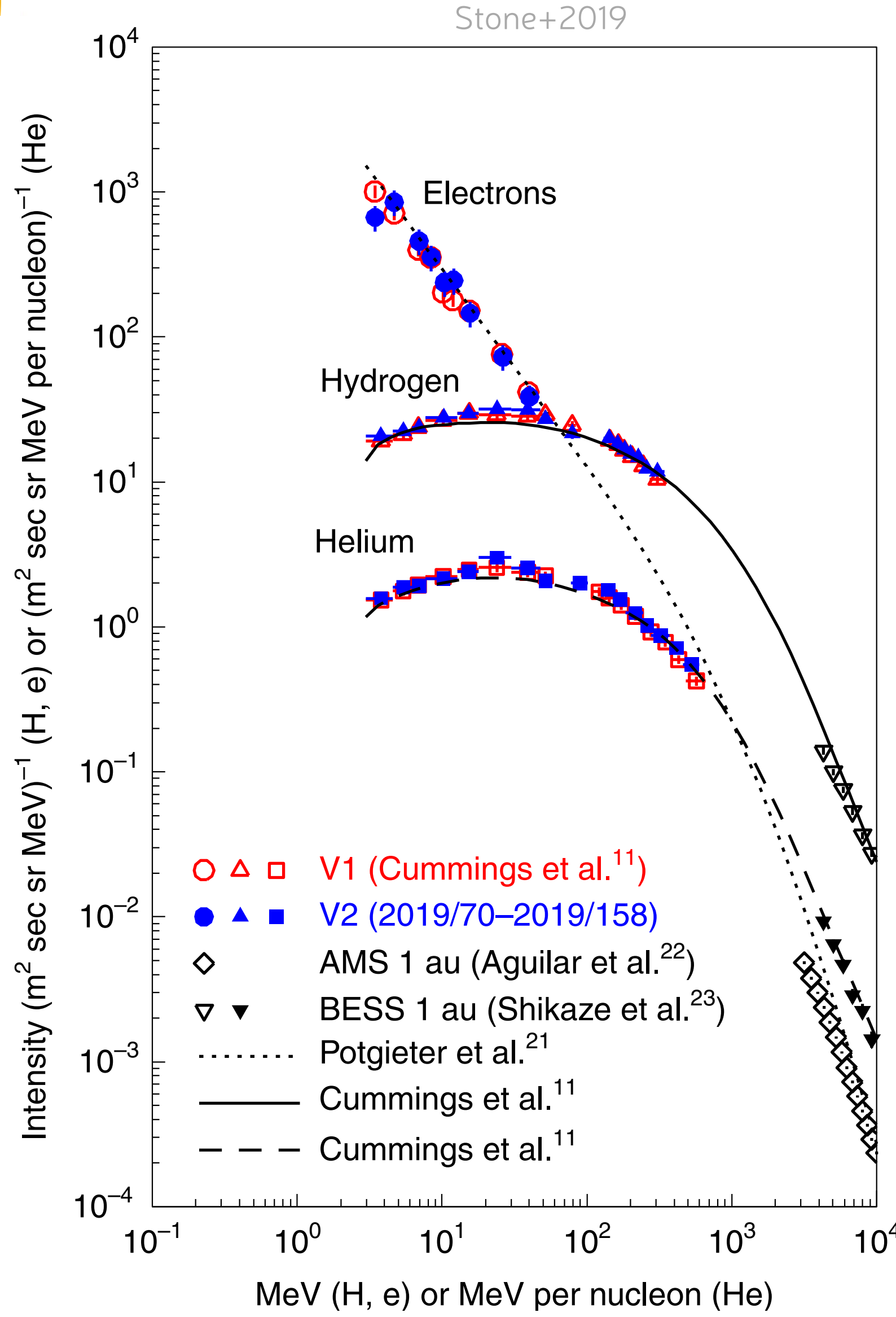


low-energy cosmic-ray gradients

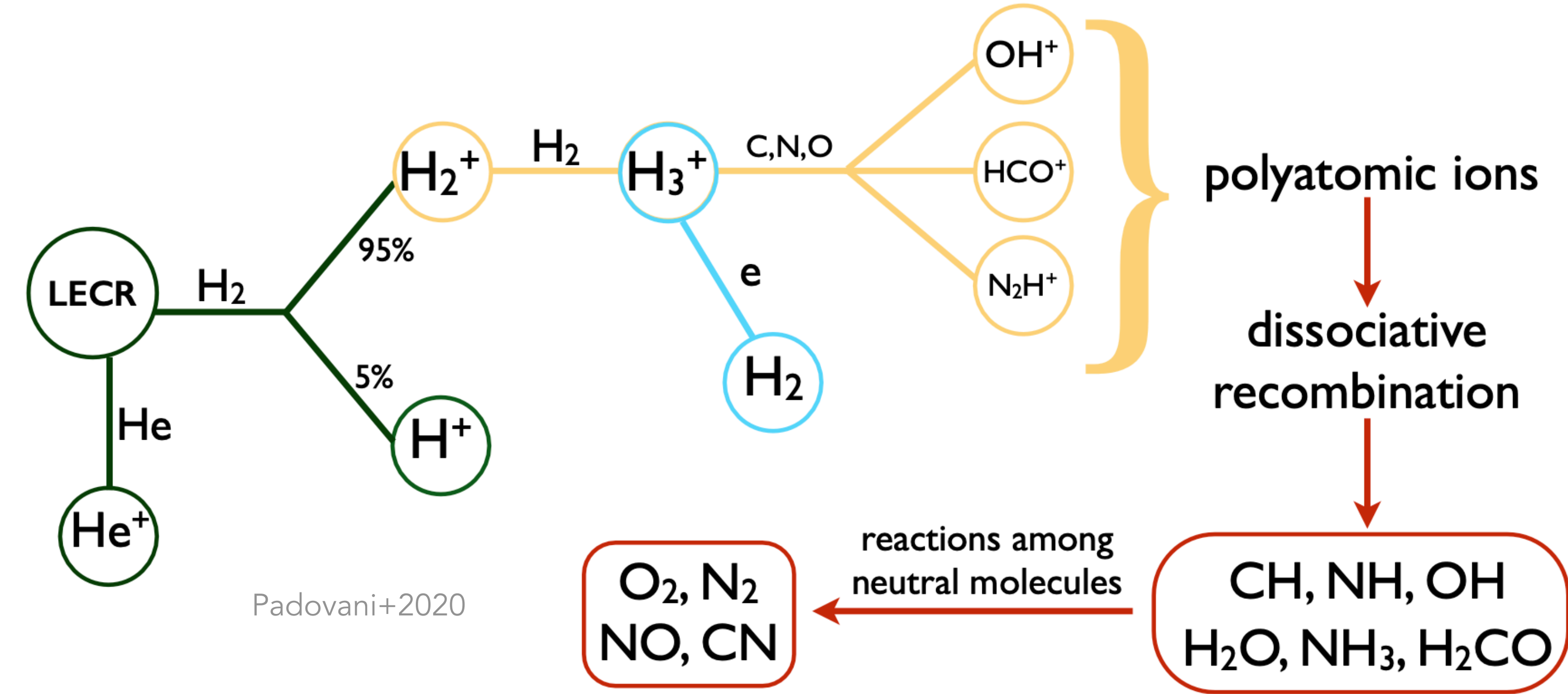
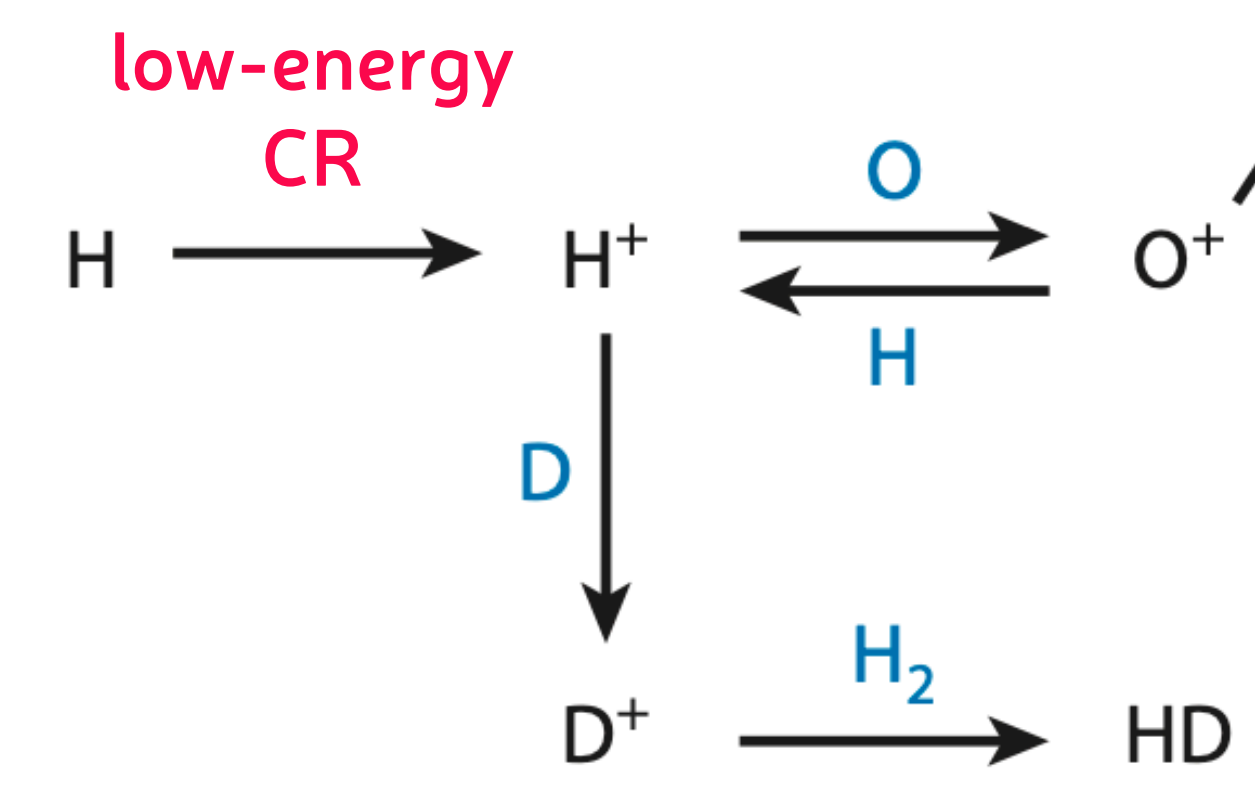
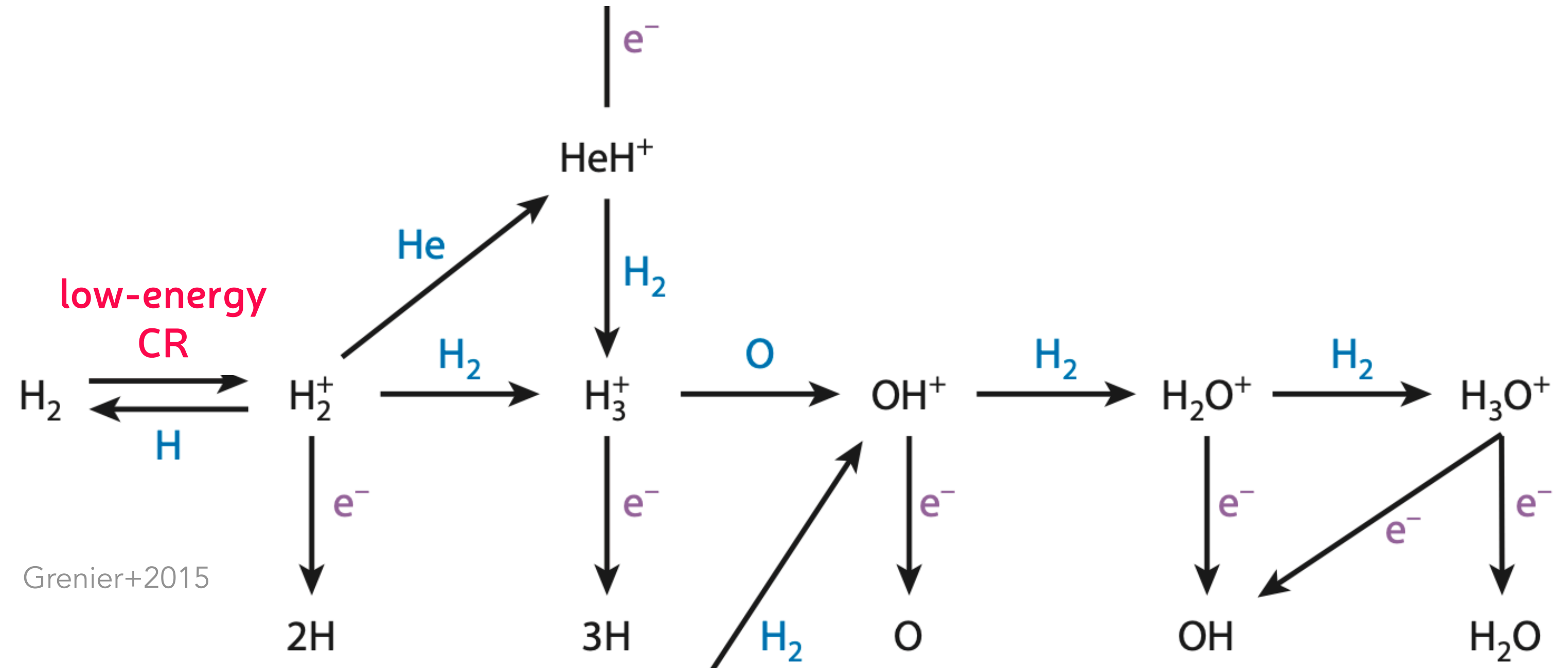
● from Voyager CR data : $\zeta_{CR}^H = (1.51 - 1.64) \times 10^{-17} \text{ s}^{-1}$

Cummings+2016

$$\zeta_{CR}^H \approx 0.65 \zeta_{CR}^{H_2}$$



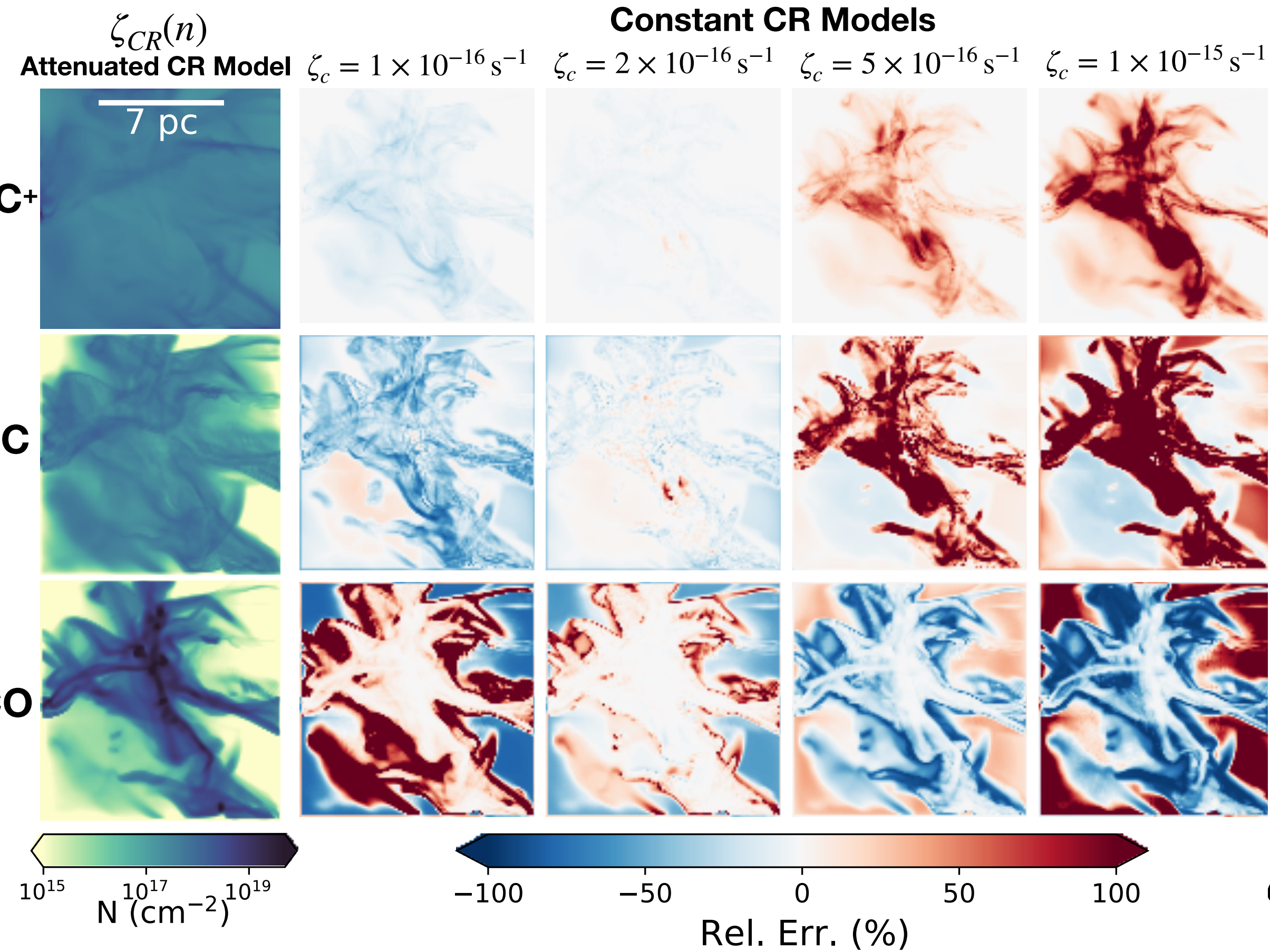
cosmic-ray induced interstellar chemistry



● hydrolysis of HCN oligomers
=> amino acids

low-energy cosmic-ray induced interstellar chemistry

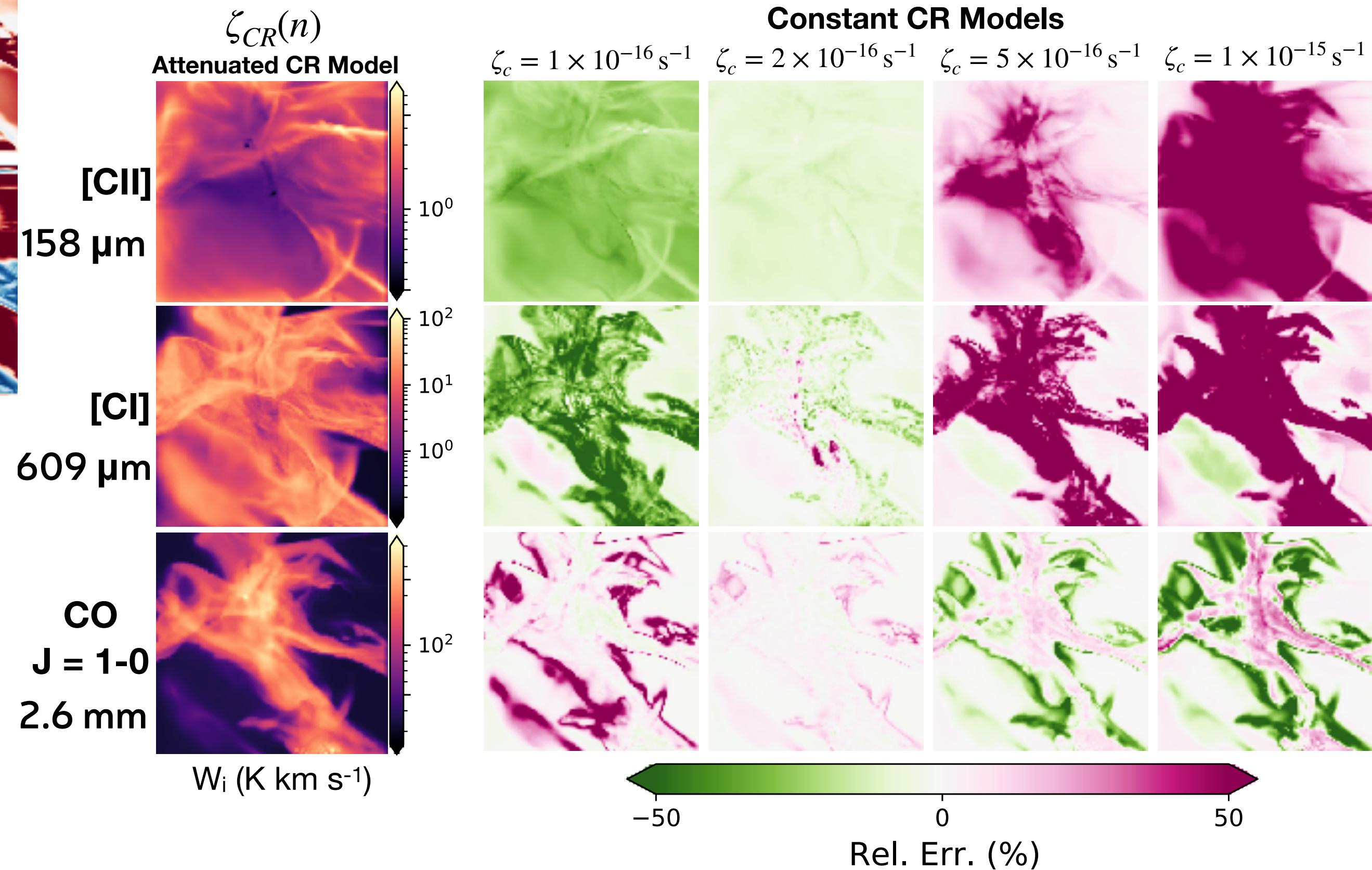
● variations in column densities through the cloud



Gaches+2022

significant impact of ζ_{CR} on CII (158 μm), CI (609 μm), and CO (J=1-0) cooling intensities in a cloud

● variations in cooling line intensities



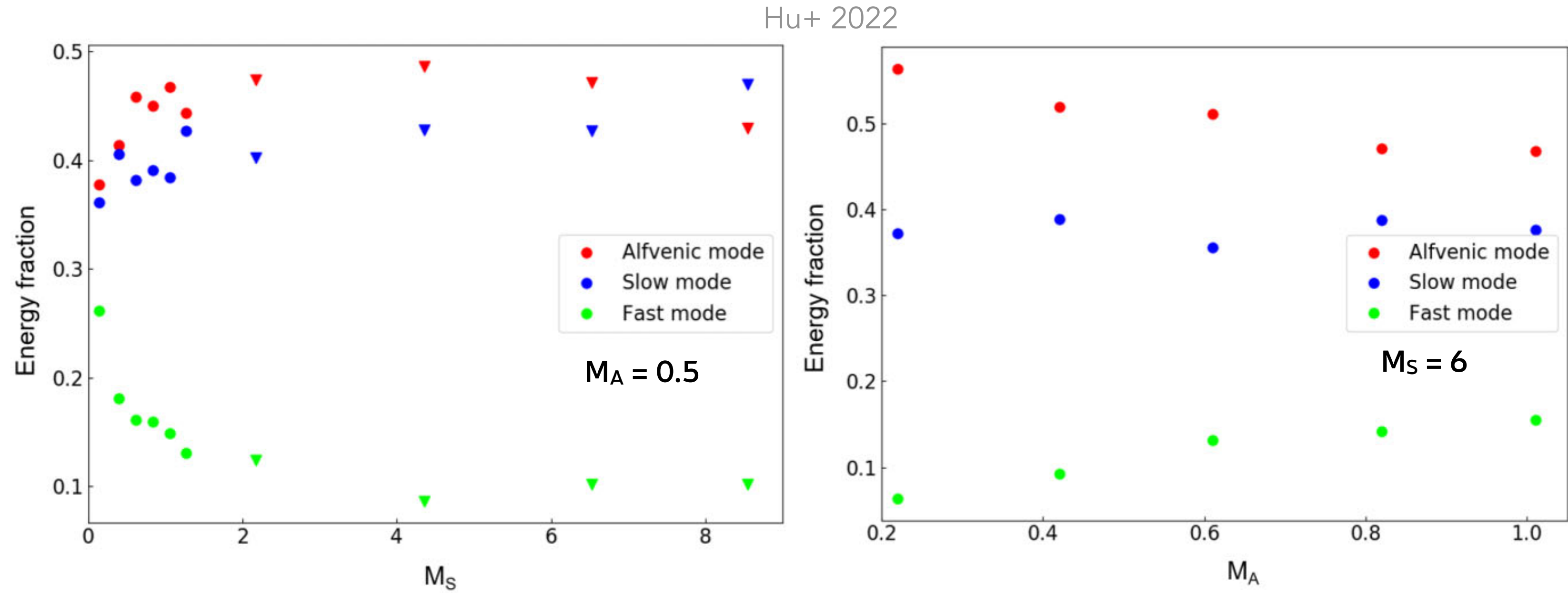
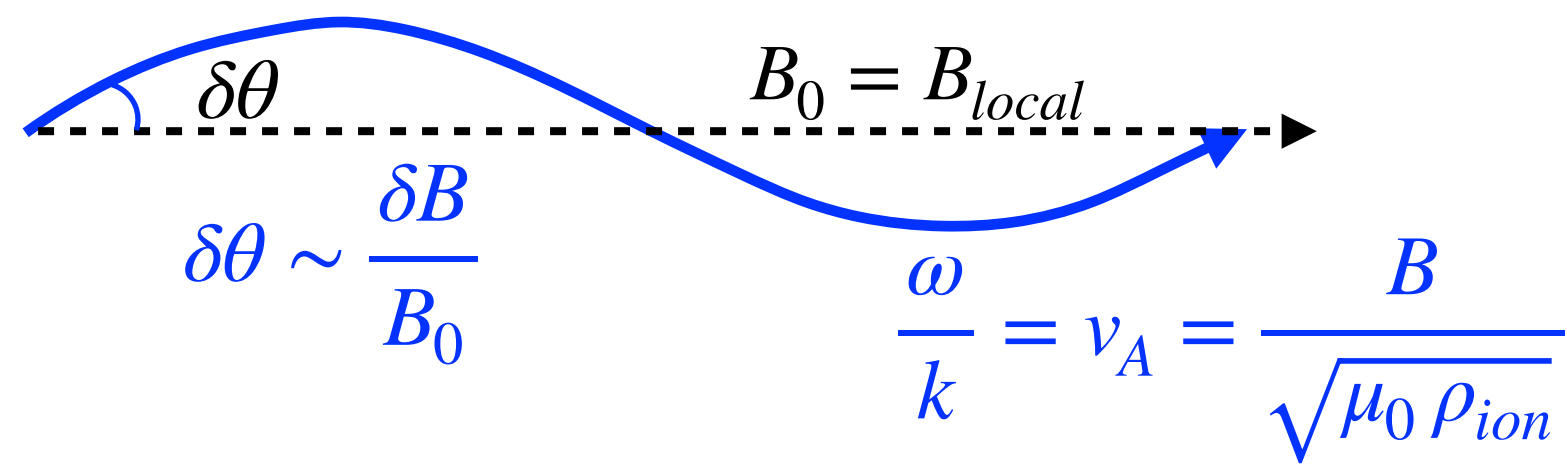
How do
GeV cosmic rays
travel?



3 fundamental modes of MHD turbulence

- energy fraction as a function of the sonic and Alfvénic Mach numbers

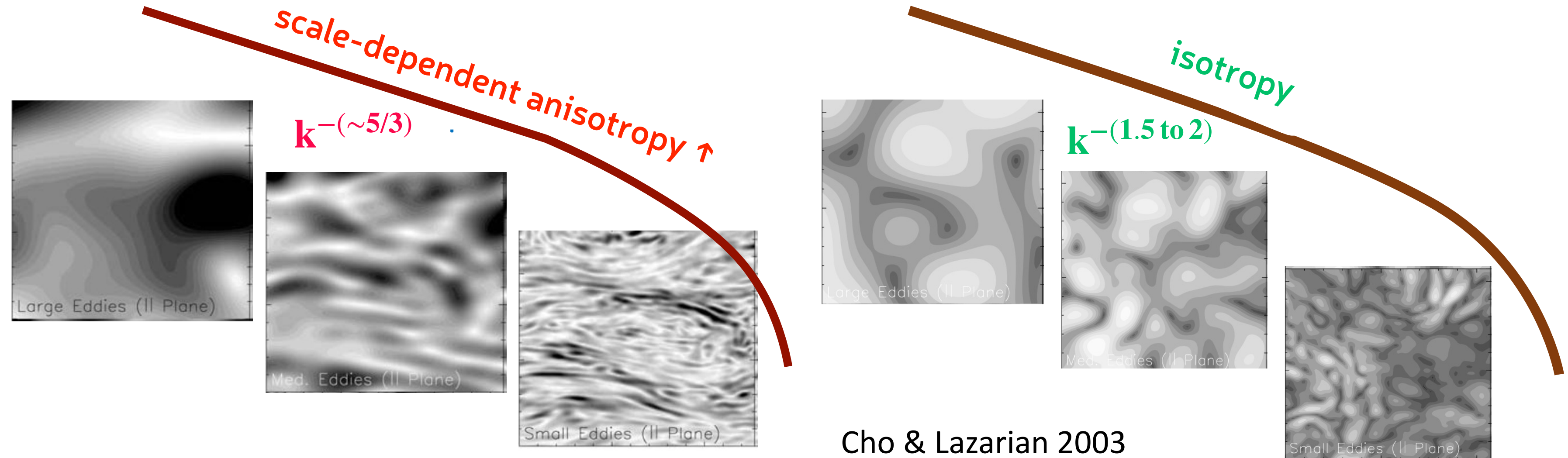
- Alfvén transverse wave driven by magnetic tension propagating along B at v_A .



Alfvén modes

Fast modes

- cascading and anisotropy of the slow mode imposed by Alfvén modes



Cho & Lazarian 2003
Hu et al. 2024

© Siyao Xu

cosmic-ray transport modes

- gyro pulsation: $\Omega_{gyr} = \frac{|q|B_0}{\gamma mc}$

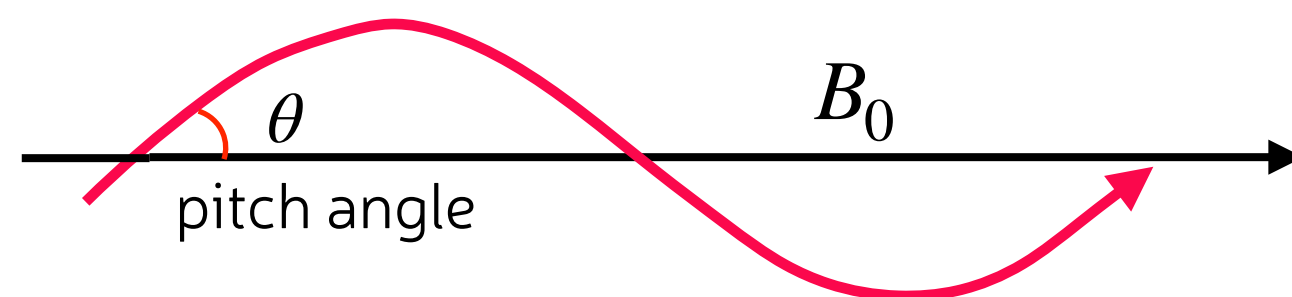
- Larmor gyroradius $R_{gyr} = \frac{p_{\perp}}{|q|B} = \frac{v_{\perp}}{\Omega_{gyr}}$

$$R_{gyr} = 1.2 \cdot 10^{-6} \text{ pc} \left(\frac{B}{1 \text{ nT}} \right)^{-1} \left(\frac{E_{kin}}{10 \text{ GeV}} \right)$$

$$R_{gyr} = 0.25 \text{ au} \left(\frac{B}{1 \text{ nT}} \right)^{-1} \left(\frac{E_{kin}}{10 \text{ GeV}} \right)$$

- magnetic moment $\mu_B = \frac{p_{\perp}^2}{2B}$
(conserved if adiabatic conditions
 $B \sim \text{constant}$ within R_{gyr} and T_{gyr})

- pitch angle



$$\mu = \cos \theta_{pitch} = \frac{\vec{p} \cdot \vec{B}}{pB} = \frac{v_{\parallel}}{v}$$

$$v_{\perp} = v \sqrt{1 - \mu^2}$$

weak B or large E

quasi-ballistic $R_{gyr} \gg l_{coherent B}$

κ_{\parallel} diffusion

$R_{gyr} \lesssim \lambda_B$

gyro-resonant scattering

κ_{\perp} diffusion

$R_{gyr} \lesssim l_{coherent B}$

B line random walk

$R_{gyr} \approx \rho_{curv B}$

non-adiabatic kicks in kinks

$R_{gyr} < l_{coherent B}$

B line random walk

mirroring

strong B or low E

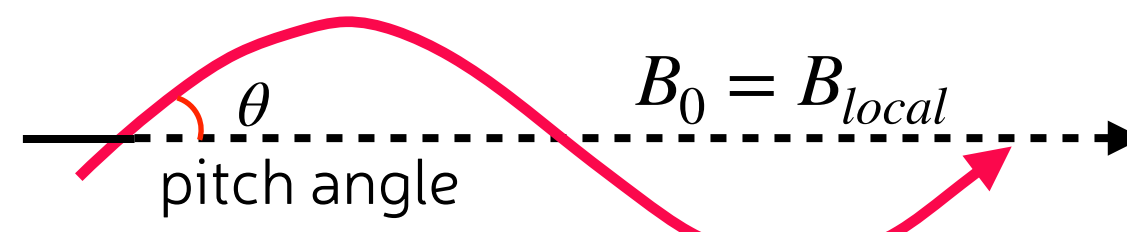
gyro-resonant pitch-angle diffusion

- **gyro-resonant scattering** on all MHD waves, in particular Alfvén waves,
 - mediated by the Lorentz force
 - gyro-resonance when the Doppler-shifted rotation rate ω_r of a circularly polarised wave is a multiple of the CR gyro frequency.

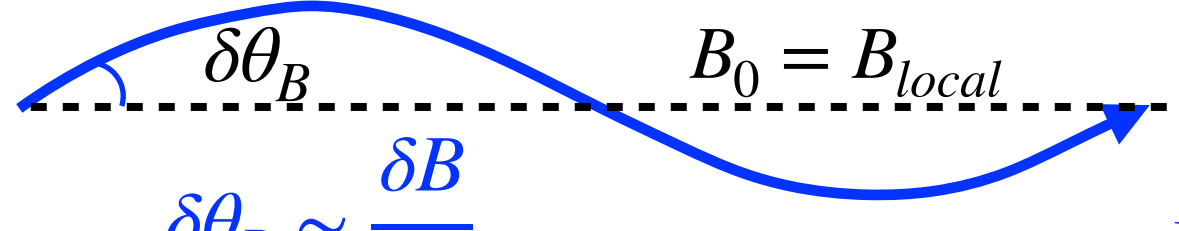
$$\mathbf{k}_{\parallel} \mathbf{v}_{\parallel} - \omega_r = \pm n \Omega_{\text{gyr}}$$

=> interaction with the rotating \vec{E} of the Doppler-shifted wave rotating in the same direction and at the same frequency as the CR rotation in its rest frame.

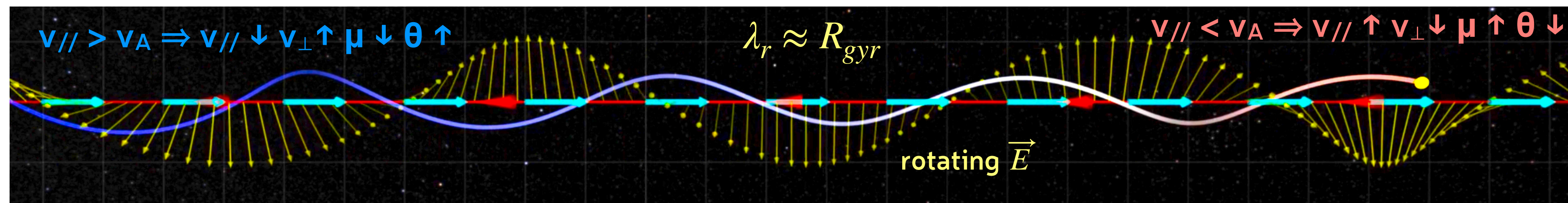
- $n = 1$ for Alfvén waves propagating // B_0 $\omega_r = kv_A$ hence $k_{\parallel}(v_{\parallel} - v_A) = \pm \Omega_{\text{gyr}}$



$$\mu = \cos \theta_{\text{pitch}} = \frac{\vec{p} \cdot \vec{B}}{pB} = \frac{v_{\parallel}}{v} \quad v_{\perp} = v \sqrt{1 - \mu^2}$$



$$\delta \theta_B \sim \frac{\delta B}{B_0} \quad v_A^2 = \frac{B^2}{\mu_0 \rho_{\text{ion}}}$$



- implying a random “walk” in $\mu = \frac{v_{\parallel}}{v}$

described by diffusion with scattering deviation $|\delta \theta| \sim \delta \theta_B \sim \delta B/B$

and scattering frequency

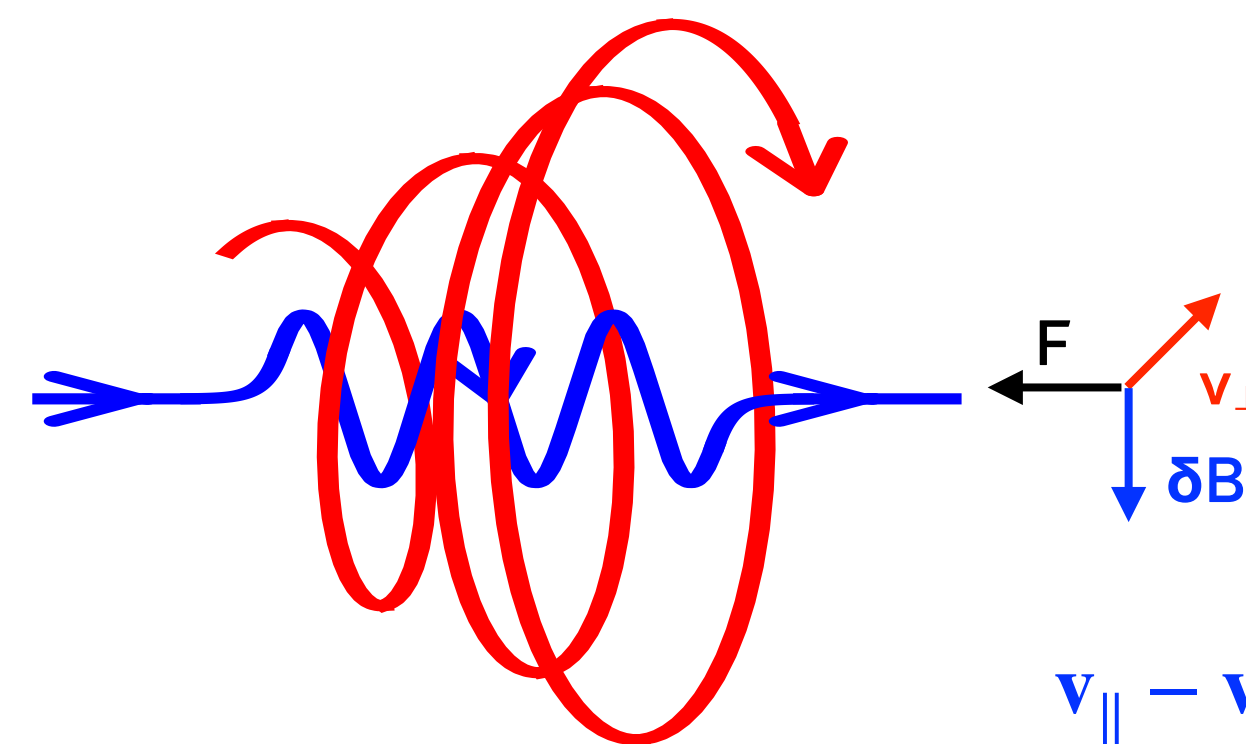
$$\nu_{sc} \approx \frac{\langle \delta \theta^2 \rangle}{\delta t} \sim \nu_{\text{gyr}} \left(\frac{\delta B}{B_0} \right)^2$$

- diffusion mean free path

$$\lambda_{sc} = \frac{\beta c}{\nu_{sc}} \propto R_{\text{gyr}} \left(\frac{B_0}{\delta B} \right)^2$$

- diffusion coefficient

$$\kappa_{\parallel} = \frac{1}{3} \lambda_{sc} \beta c = \frac{1}{3} \frac{\beta^2 c^2}{\nu_{sc}} \propto R_{\text{gyr}} \left(\frac{B_0}{\delta B} \right)^2$$



no \vec{E} in the wave frame
 $\Rightarrow (v_{\parallel} - v_A)^2 + v_{\perp}^2 = \text{cte}$
 $v_{\parallel} - v_A \downarrow \Rightarrow v_{\perp} \uparrow \Rightarrow \theta_{\text{pitch}} \uparrow \Rightarrow \mu \downarrow$
 and vice versa

$$\kappa_{\parallel} = \int_{-1}^{+1} \frac{v^2 (1 - \mu^2)}{4 \nu_{sc}} d\mu$$

transit-time damping (TTD) = transit-time surfing

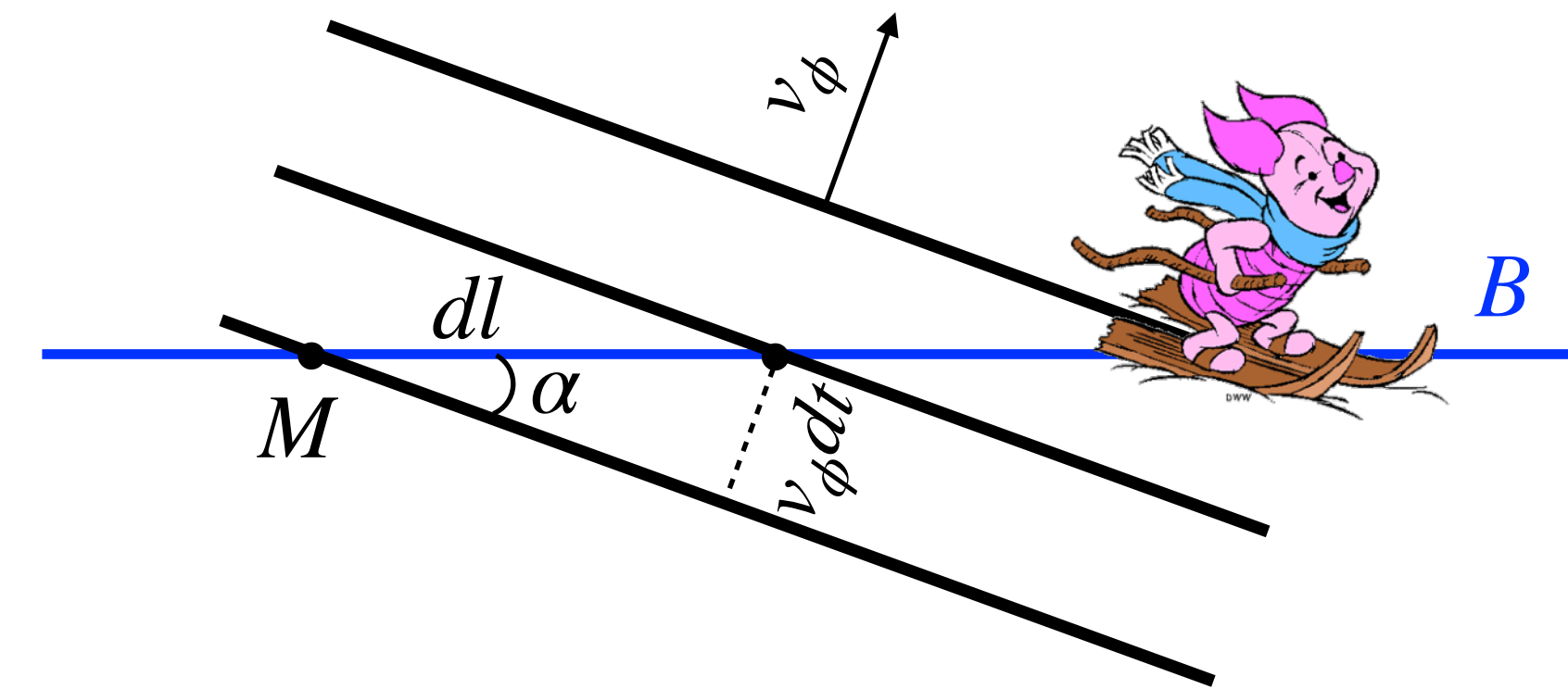
- surfing the wavefront of oblique compressible fast and slow wave modes

- v_ϕ = phase velocity of the compression wave.

- intersection point M between the wavefront and the mean local B moves at speed $v_M = \frac{dl}{dt} = \frac{v_\phi}{\sin \alpha}$

- surf if CR moves at $v_{\parallel} = v_M$

- small range of small α given the large v_{\parallel} of CRs



- $n = 0$ mode

- transit time for the CR to cross the wave: $n = 0 \Rightarrow k_{\parallel} v_{\parallel} = \omega_r \Rightarrow \tau = \frac{\lambda_{\parallel}}{v_{\parallel}} = \frac{2\pi}{k_{\parallel} v_{\parallel}} = \frac{2\pi}{\omega_r} = T$ equal to the wave period T

- CR gains/loses p_{\parallel} from the wave \vec{E} field

- stochastic gain because head-on interactions between CR and wave are more frequent than head-tail interactions (2nd order Fermi acceleration)

- hence wave damping

- no specific resonant scale : turbulence over all scales $l > R_{gyr}$ contributes to scattering.**

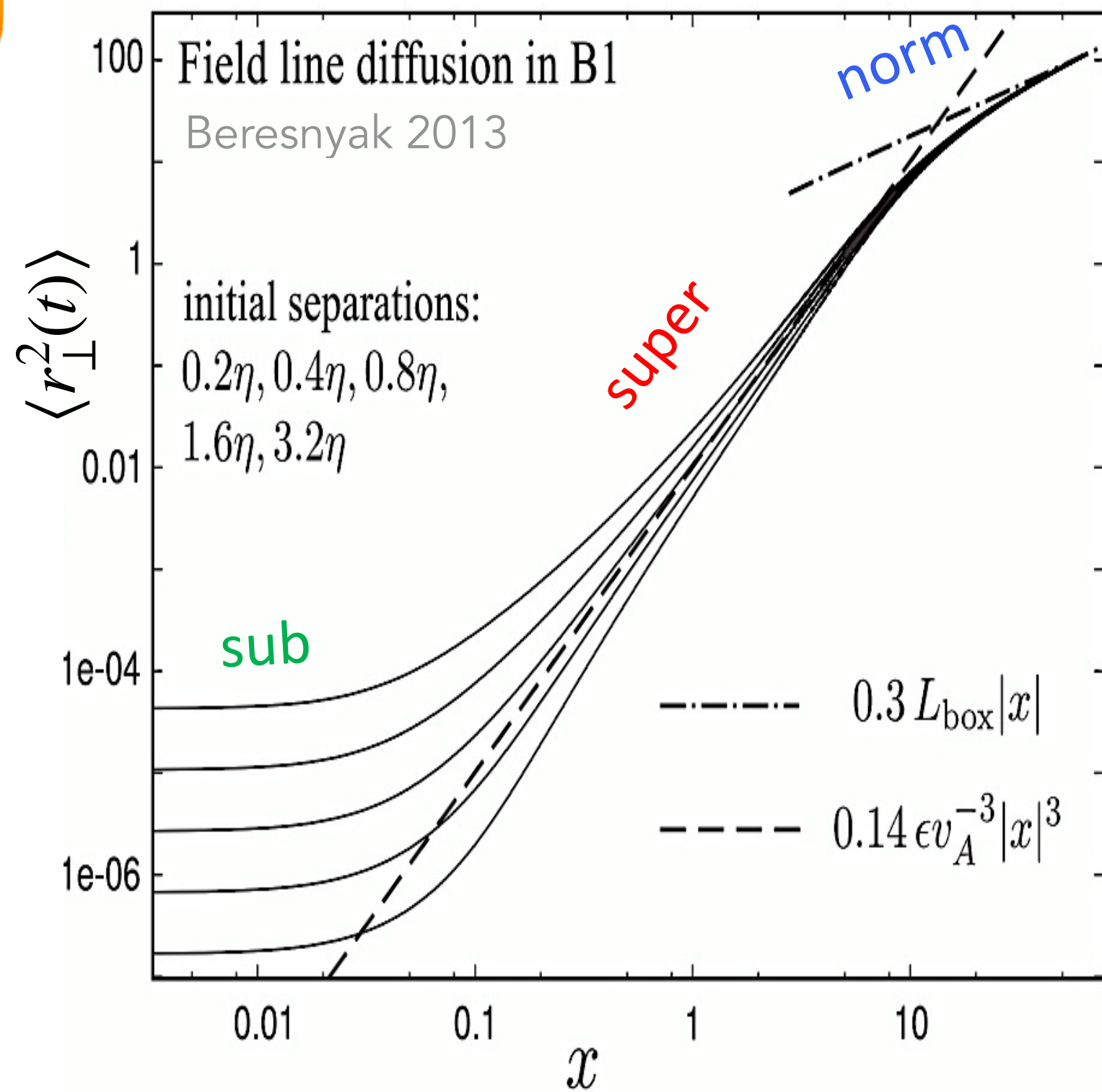
- TTD unable to scatter CRs at small pitch angles

- => TTD contributes to scattering, but **only if another process has distributed CRs to $\theta \gtrsim 60^\circ$**

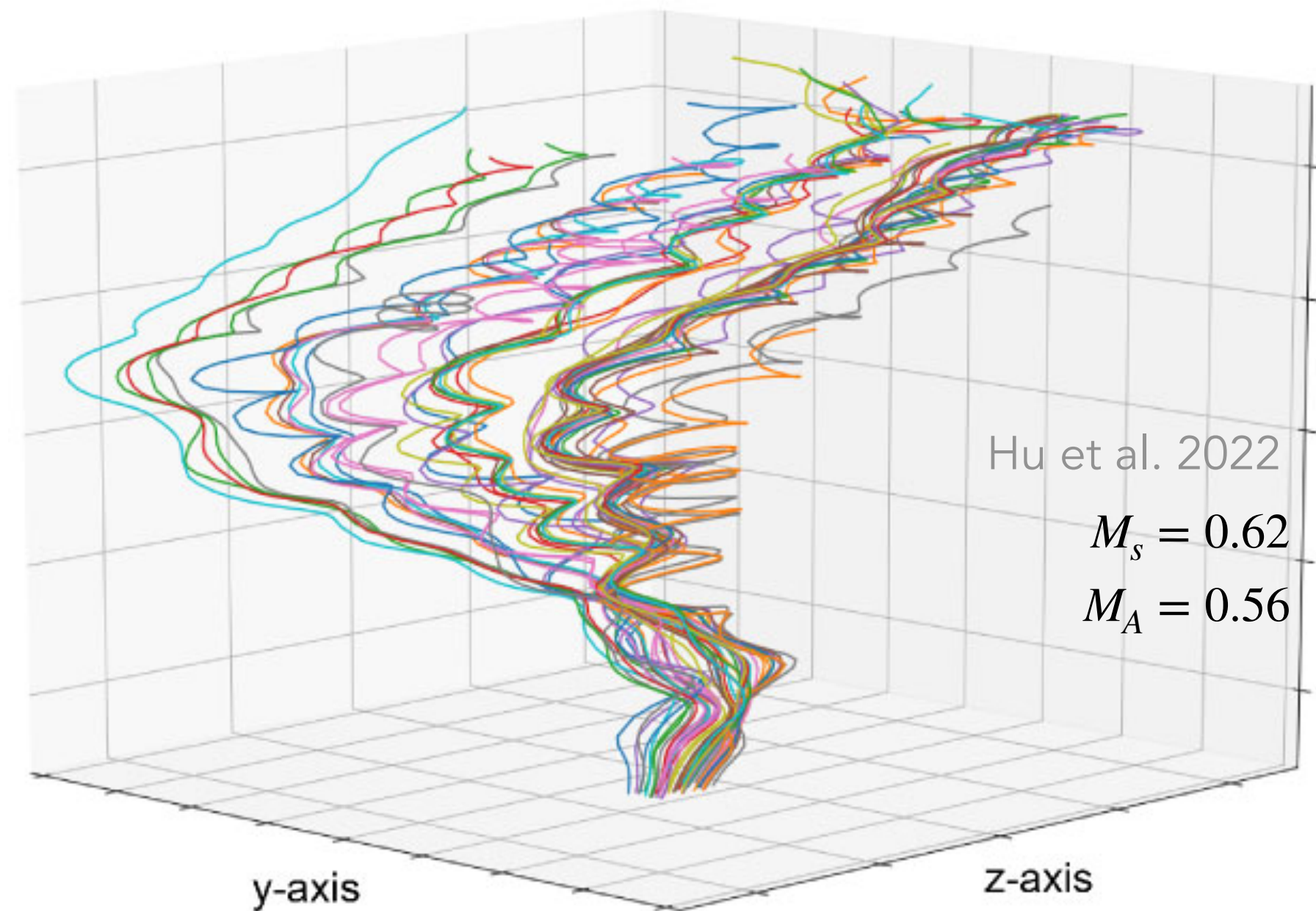
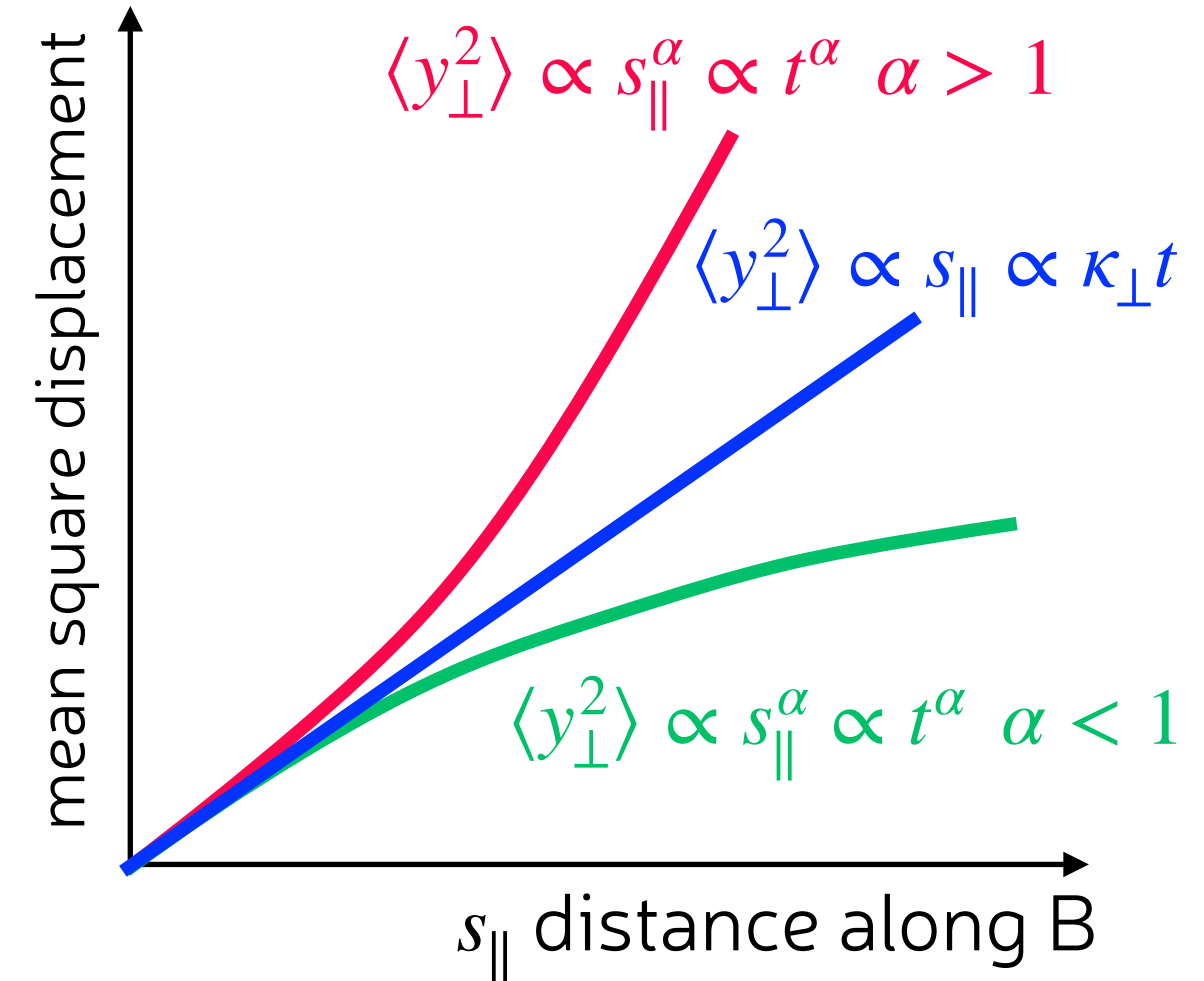
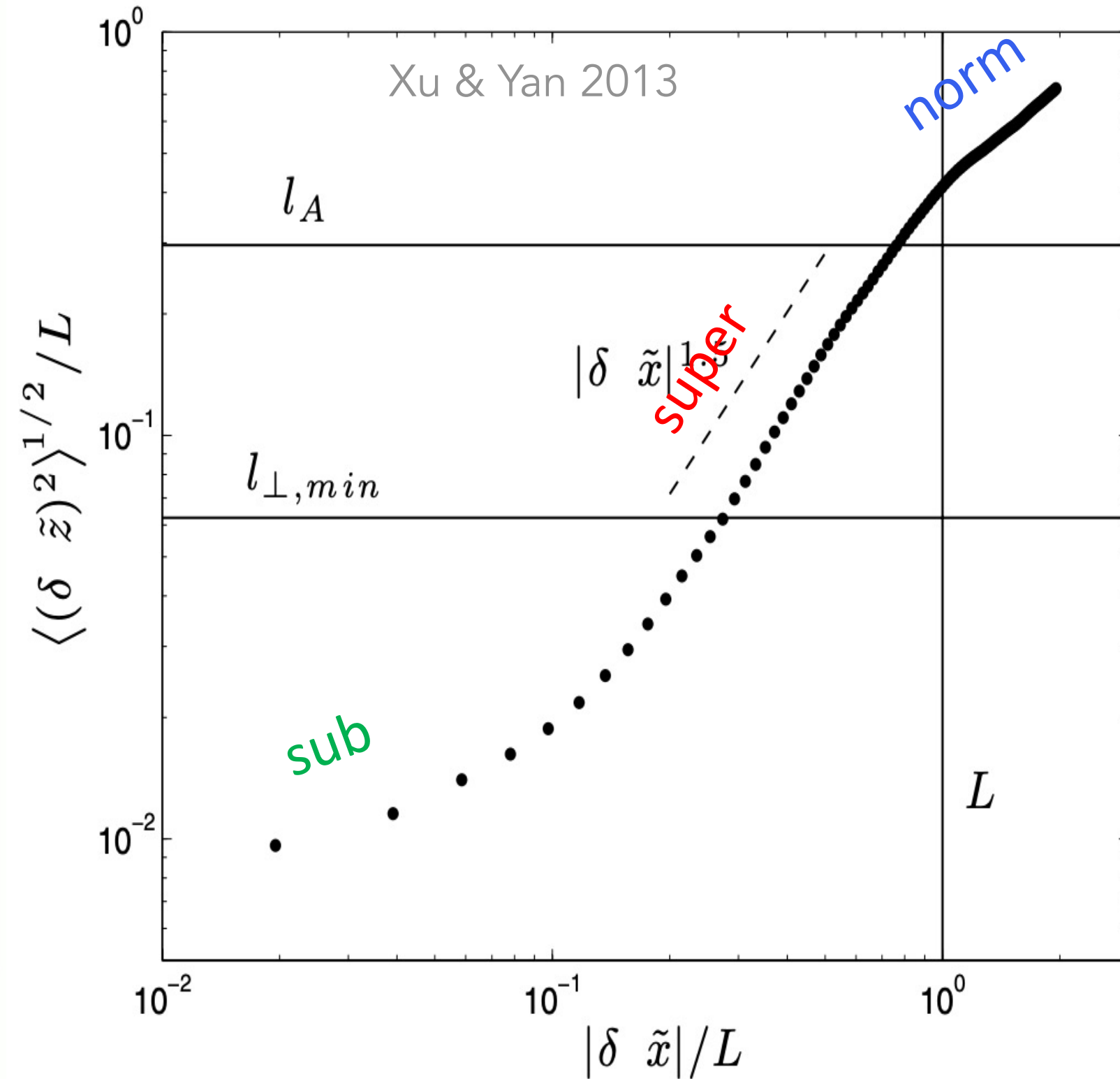
perpendicular diffusion in external MHD turbulence

- maximum $\kappa_{\perp} = R_{gyr}c \approx 10^{21}$ cm²/s from pitch-angle scattering => perpendicular diffusion due to B line diffusion
- B line perpendicular diffusion
- normal diffusion at large scales (for $s > l_A = L_{inj}M_A^{-3}$ for $M_A > 1$ and $s > L_{inj}$ for $M_A < 1$)
- super diffusion in the turbulence inertial range

magnetic fields



CR particles

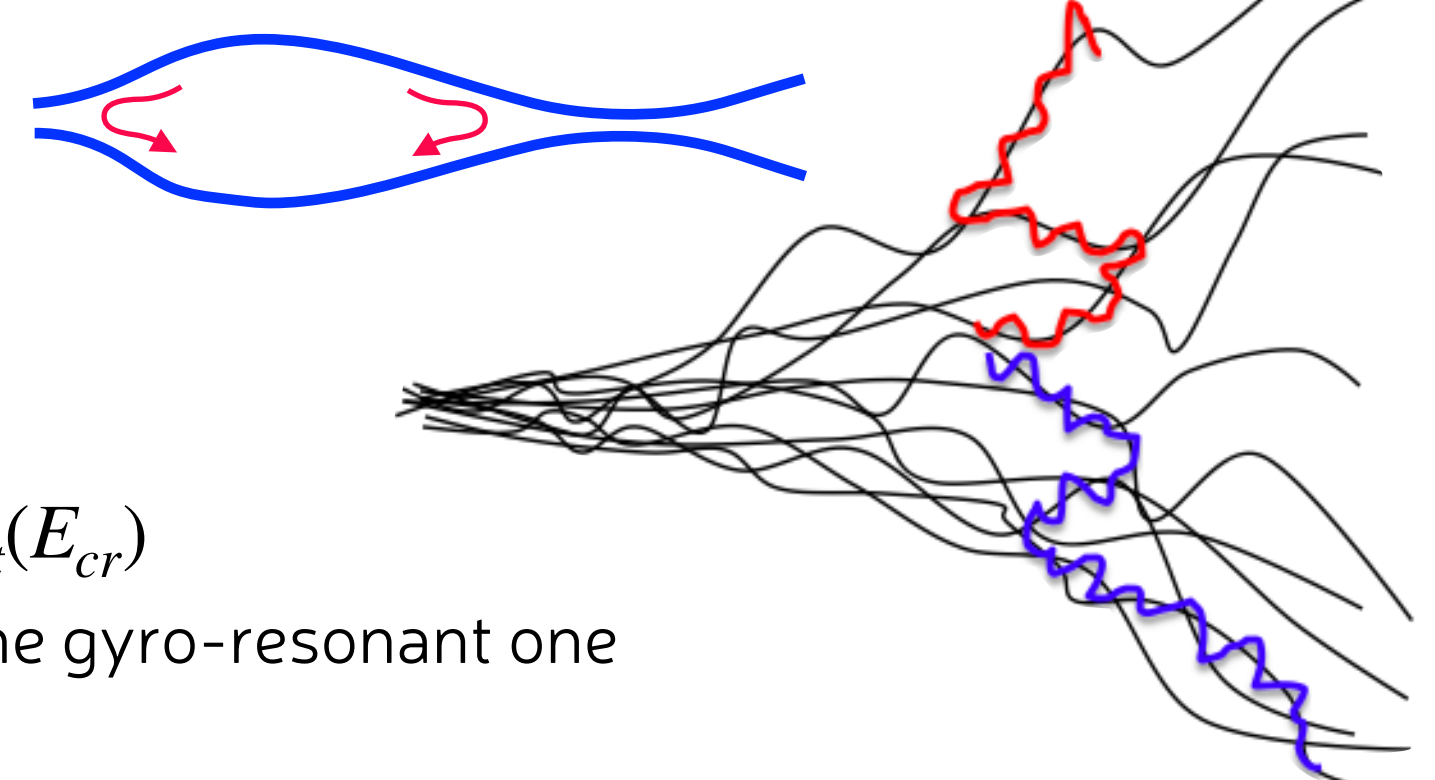


- if CR scattering mean free path along B $\lambda_{\parallel} < L_{inj}$ (as for GeV-TeV CRs in the ISM): $\langle y_{cr\perp}^2 \rangle \propto t^{3/2}$
- if $\lambda_{\parallel} > L_{inj}$: $\langle y_{cr\perp}^2 \rangle \propto t^3$
- $\kappa_{\perp} \propto M_A^4$

κ_{\perp} diffusion largely due to B line wandering

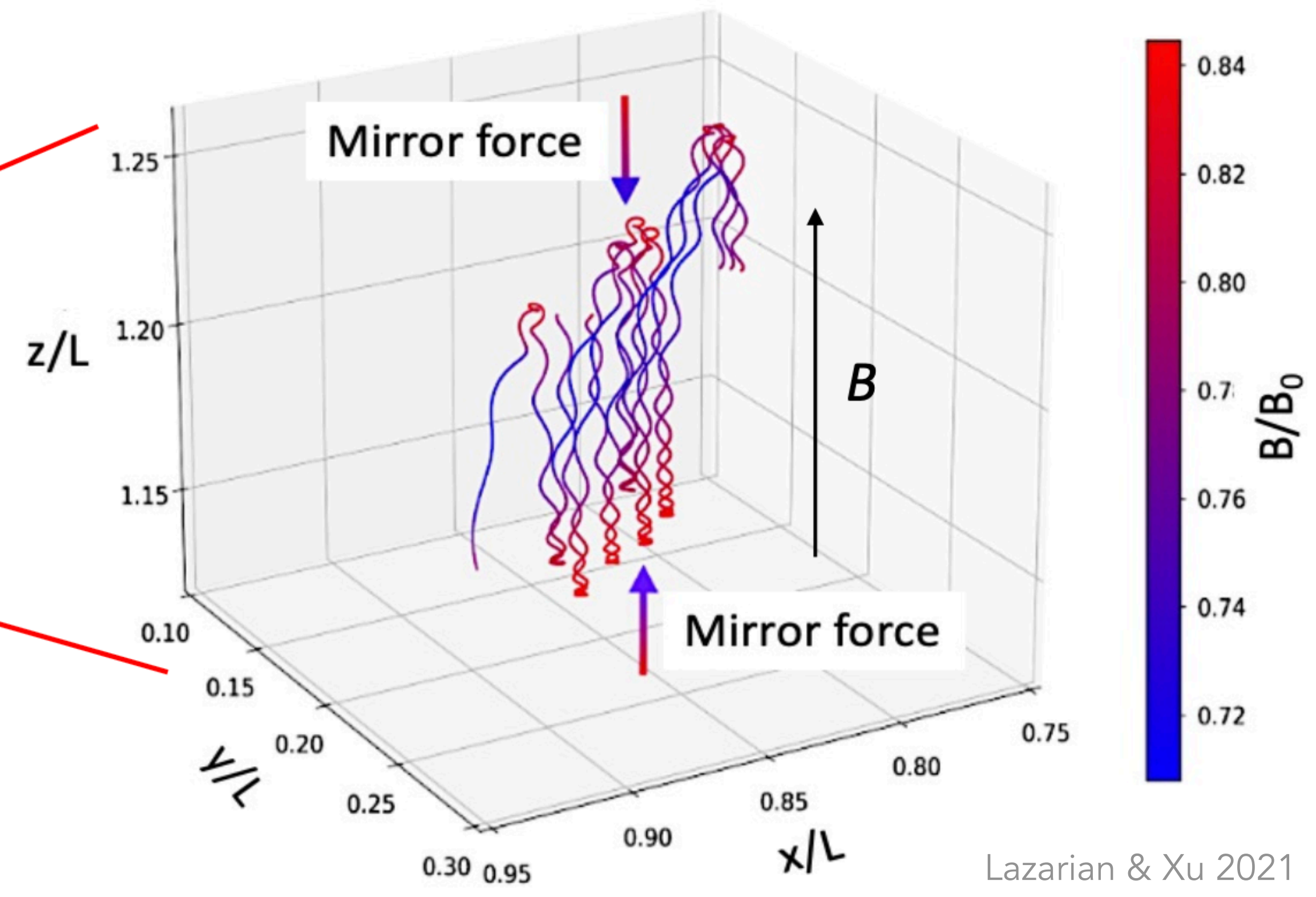
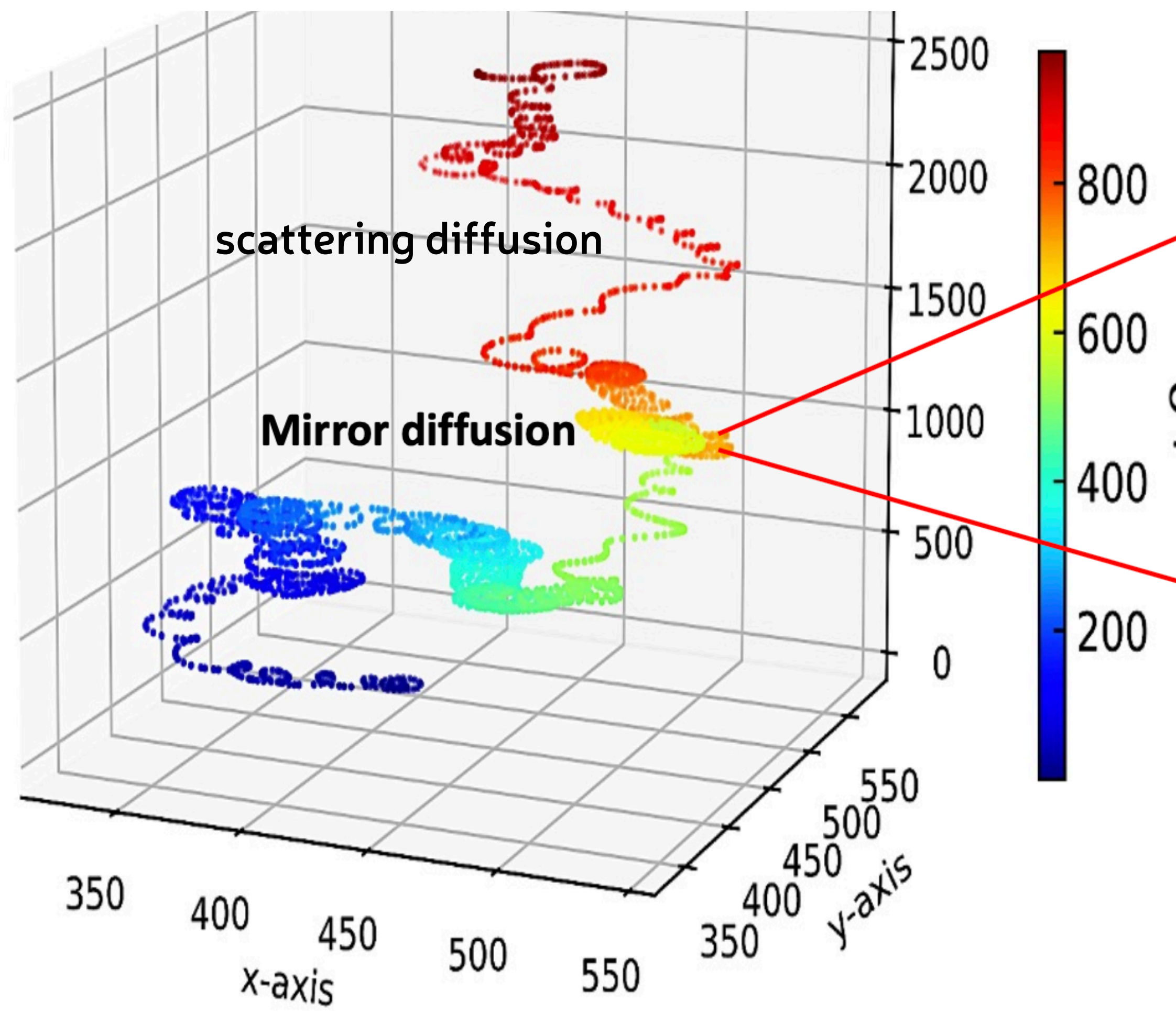
fast gyro-resonant diffusion vs. slow mirroring diffusion

- small net μ change if CR remains along the same line bundle
- but super-diffusion of B lines during the CR propagation \Rightarrow CRs follow \neq B lines after bouncing back



- **loss cone \Rightarrow reflected CRs only for large pitch angles** $\sin^2 \theta > \frac{B}{B + \delta B} \Rightarrow \mu < \mu_{crit}(B) \Rightarrow \mu < \mu_{crit}(E_{CR})$

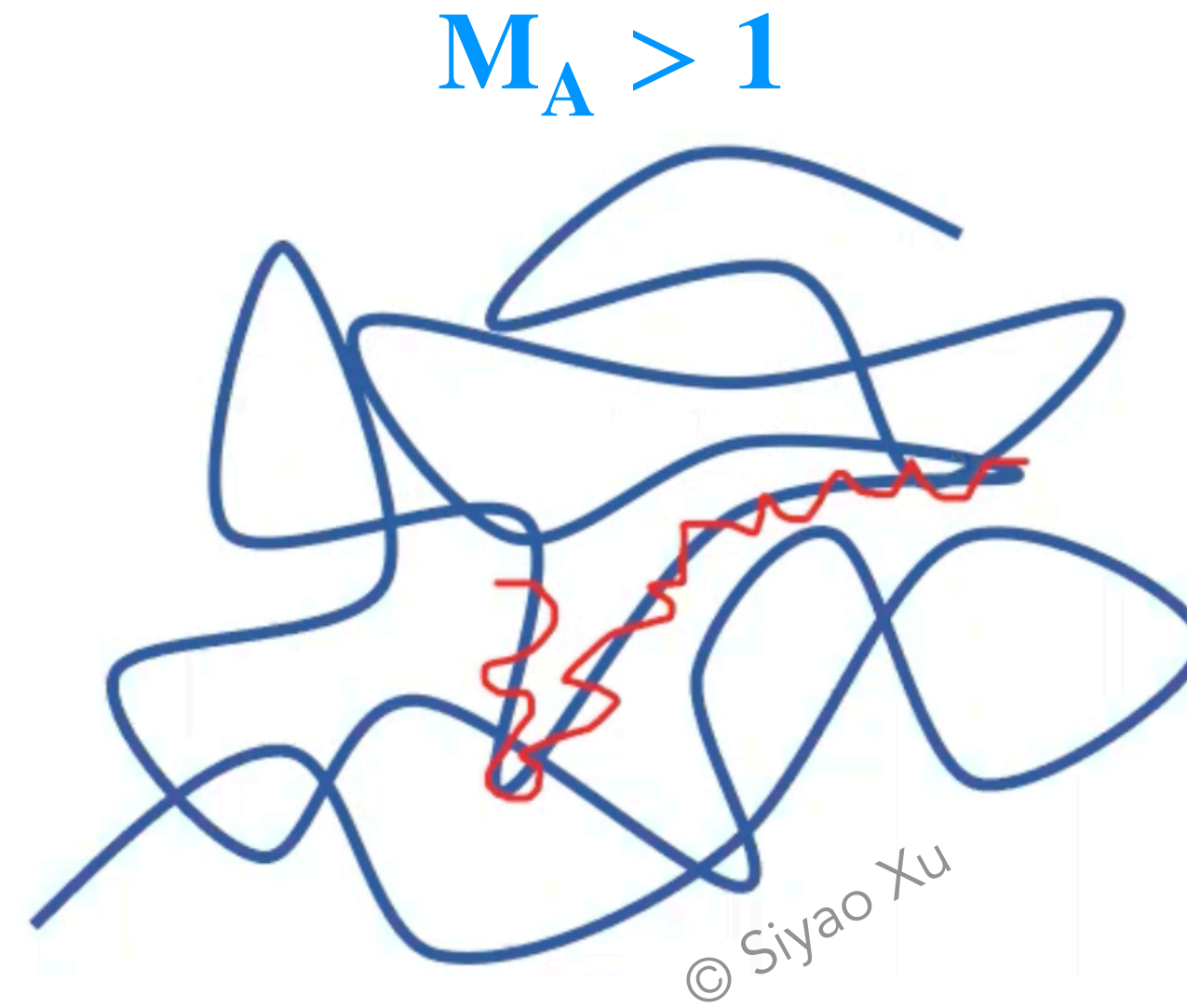
- gyro-resonant scattering at low pitch angles populates the large-pitch angle domain for mirror diffusion: $\mu_{crit}(E_{cr})$
- mirror scattering for only small fraction of the CR population \Rightarrow the average $\kappa_{||}$ of the CR population close to the gyro-resonant one



CR diffusion in tangled magnetic fields

- in super-Alfvénic turbulence, gas turbulent motions drag B lines in complex twists

$$M_A^2 = \frac{\frac{1}{2} \rho_H \delta v_{H,rms}^2}{B^2 / (2\mu_0)} = \frac{e_{kin,turb}}{e_B}$$



- **free gyration** around B lines induces an effective diffusion in space

- mean free path = coherence length of B

$$l_{mfp} = l_A = L_{inj} M_A^{-3}$$

- slows down CRs **in addition to** the gyro-resonant scattering

- important in

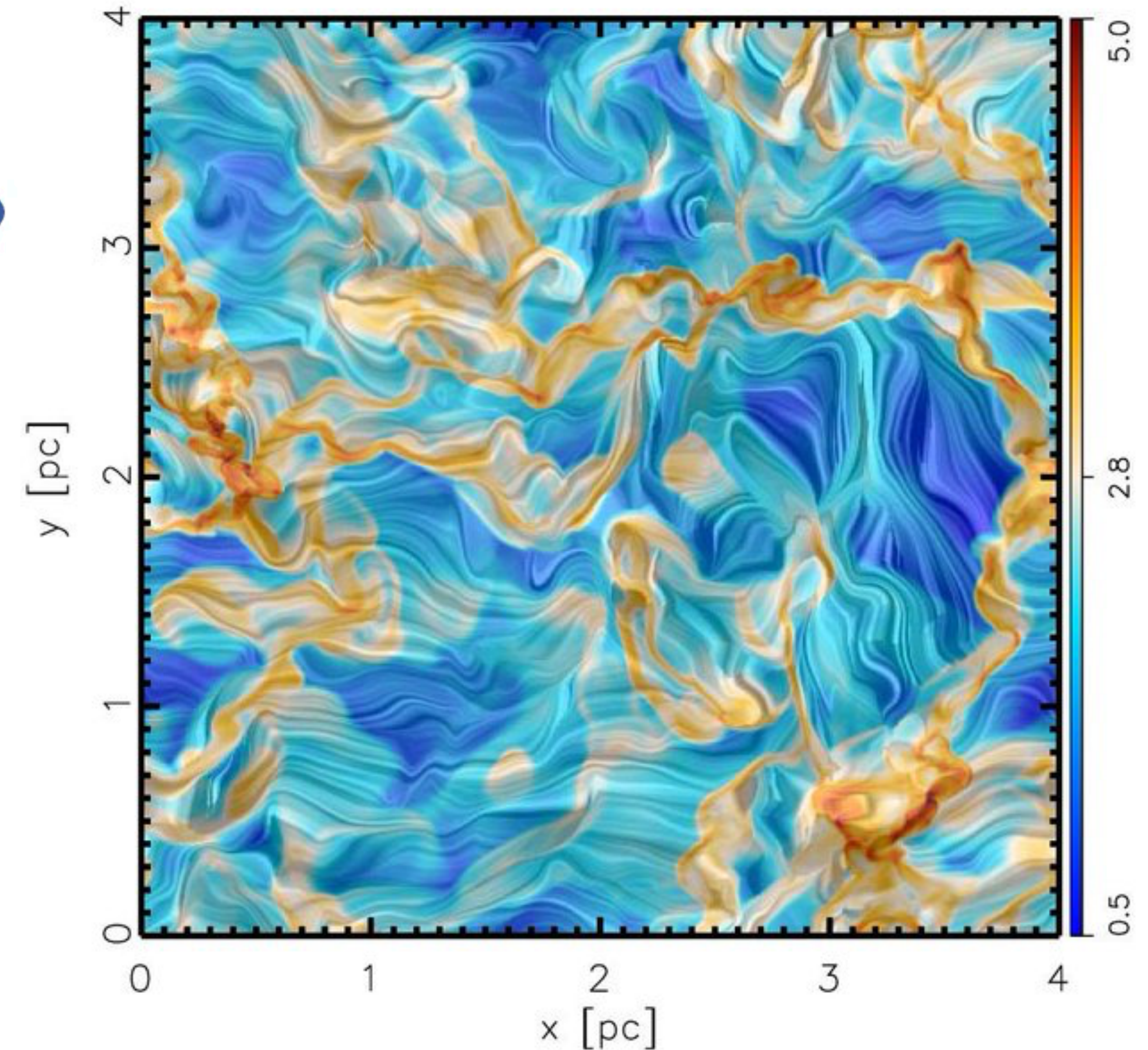
- low-B environments
- molecular clouds
- starburst environments

Krumholz+ 2020

Sampson+ 2022

Soler & Hennebelle 2017

$[\log_{10}(n/cm^{-3})]$



which waves
scatter CRs ?

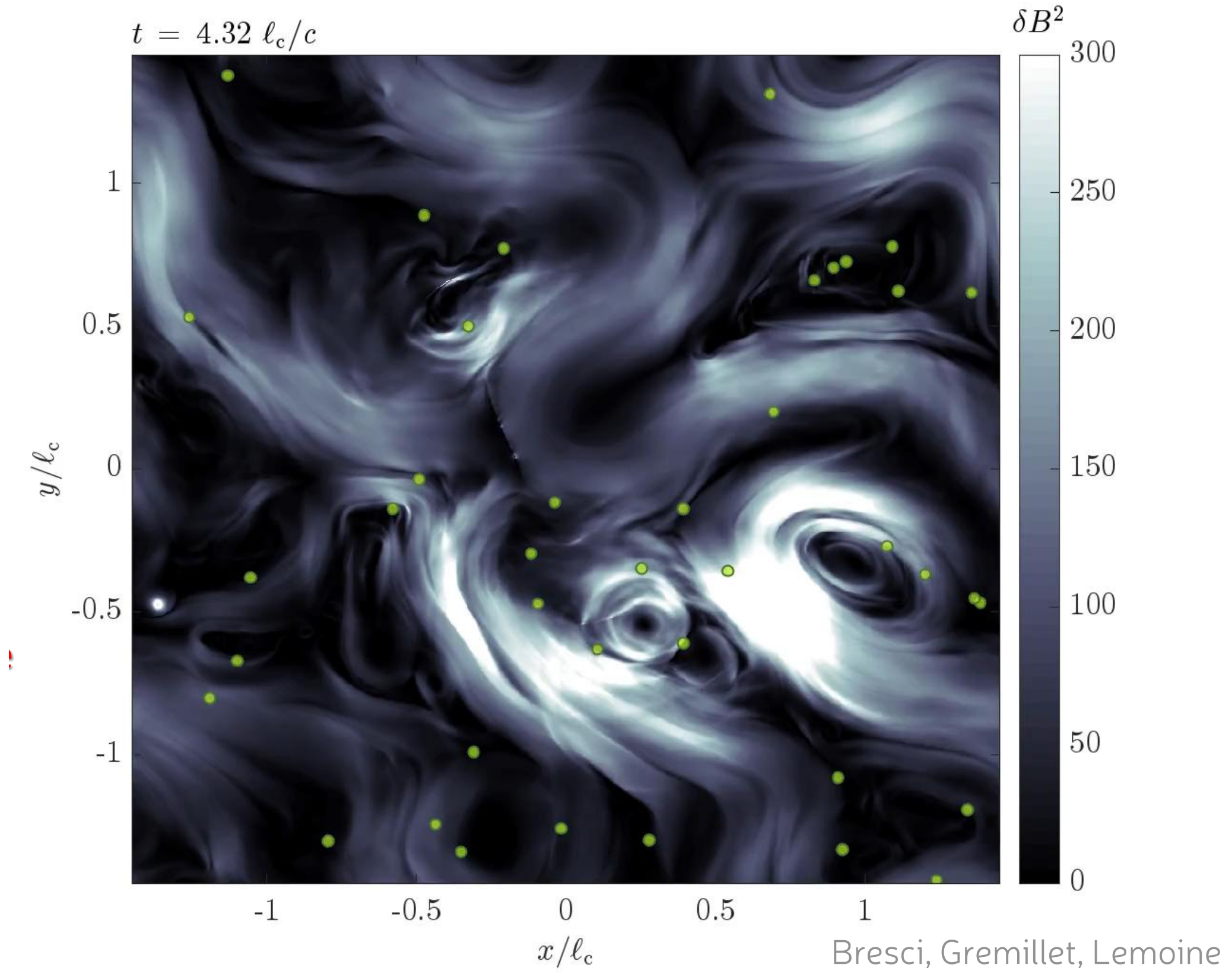
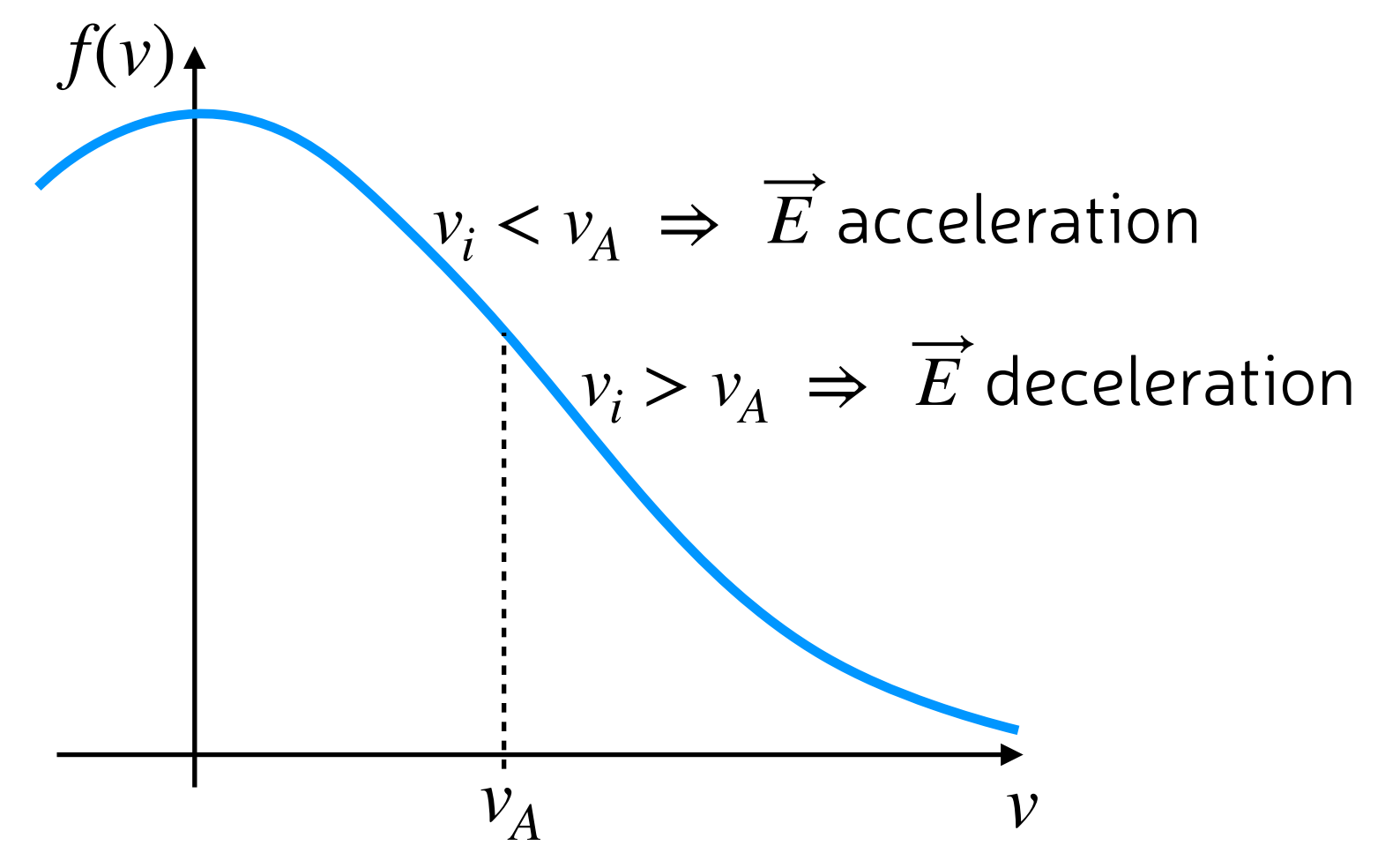


damping of MHD waves

- Landau damping because the wave \vec{E} field tends to synchronise the ions
 - more accelerated than decelerated ions => wave damping
- non-linear Landau damping by ions in the beat wave formed by 2 almost-co-propagating waves
 - mirror force acceleration for $v_i \approx v_{beat}$
- turbulent damping : shearing of two counter-propagating MHD eddies
 - efficient if crossing time \approx turnover time
 - induces the energy cascade to smaller scale
 - depends on M_A and scale
- ion-neutral damping
 - ion-neutral momentum transfer in collisions, but also neutral viscosity
 - dominant in neutral gas phases (WNM, CNM, DNM, H₂)

Landau 1946

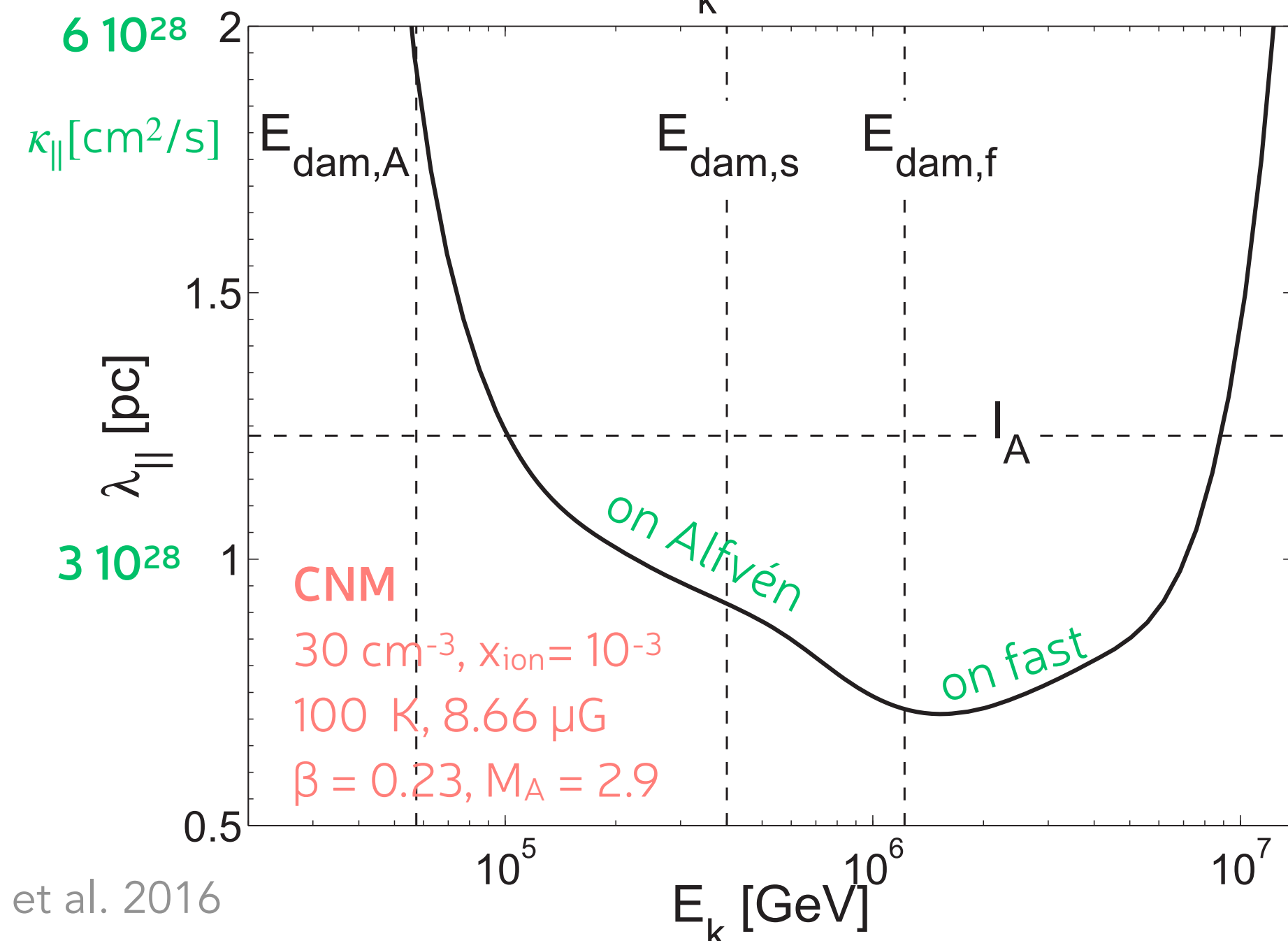
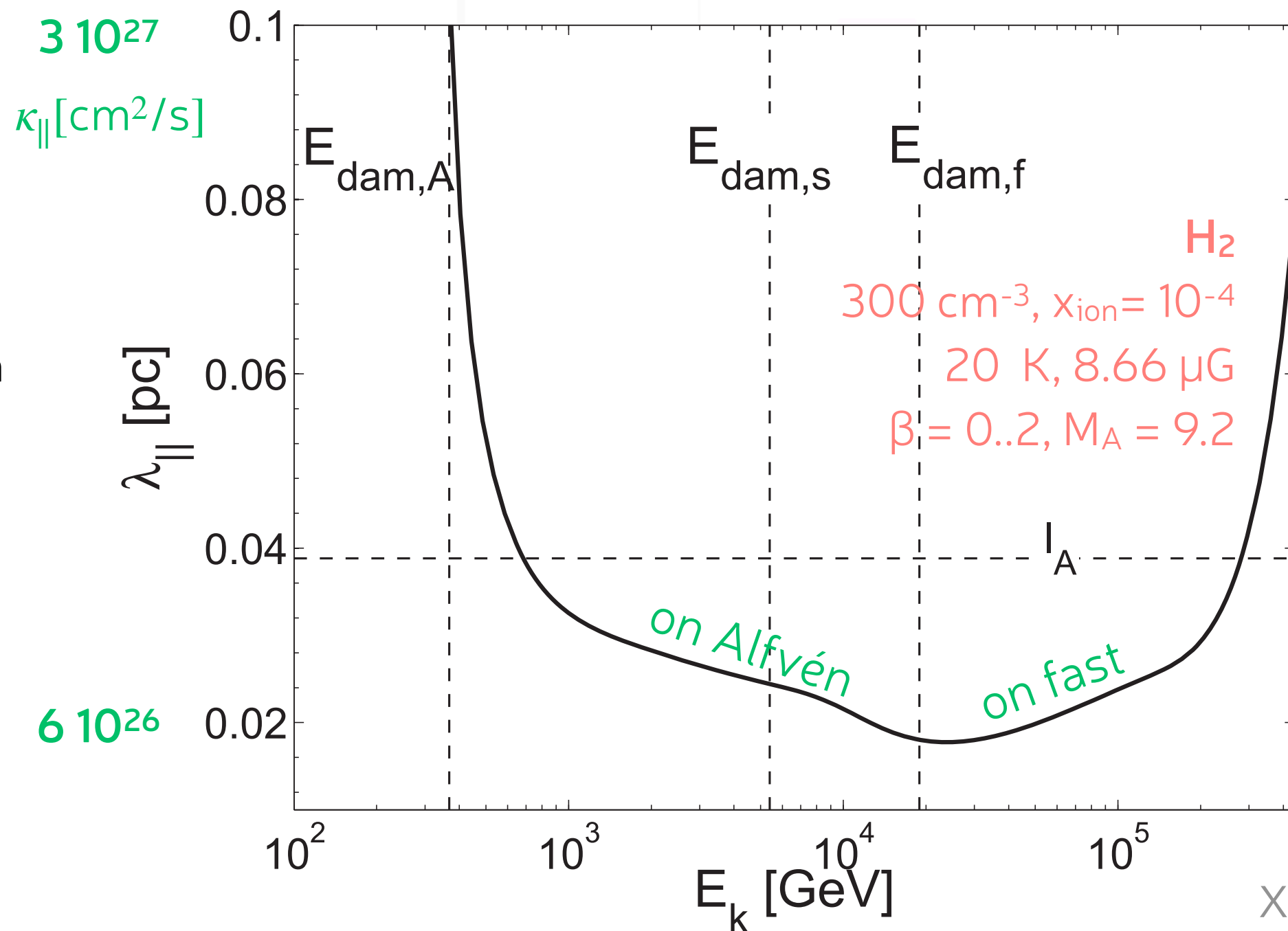
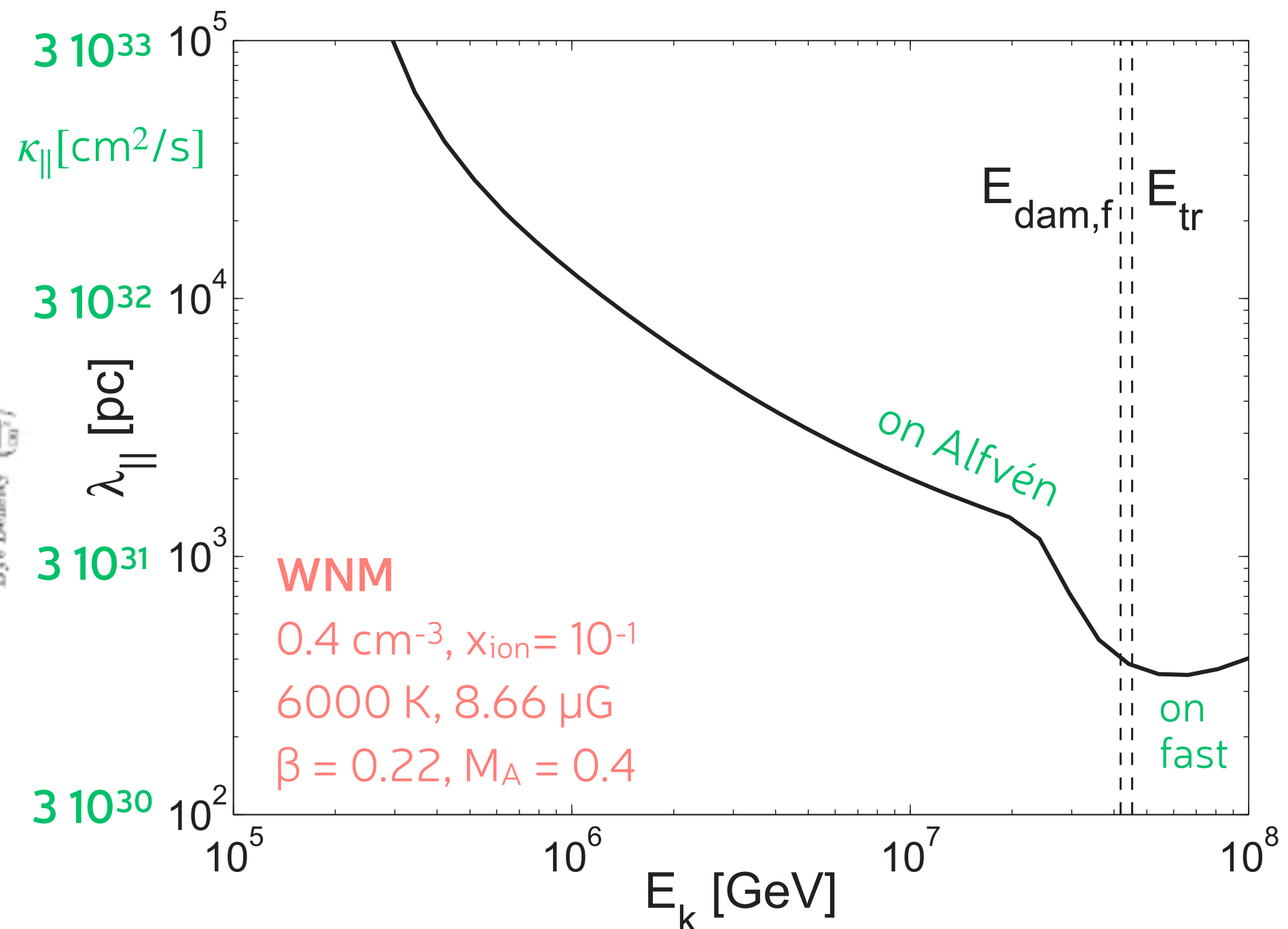
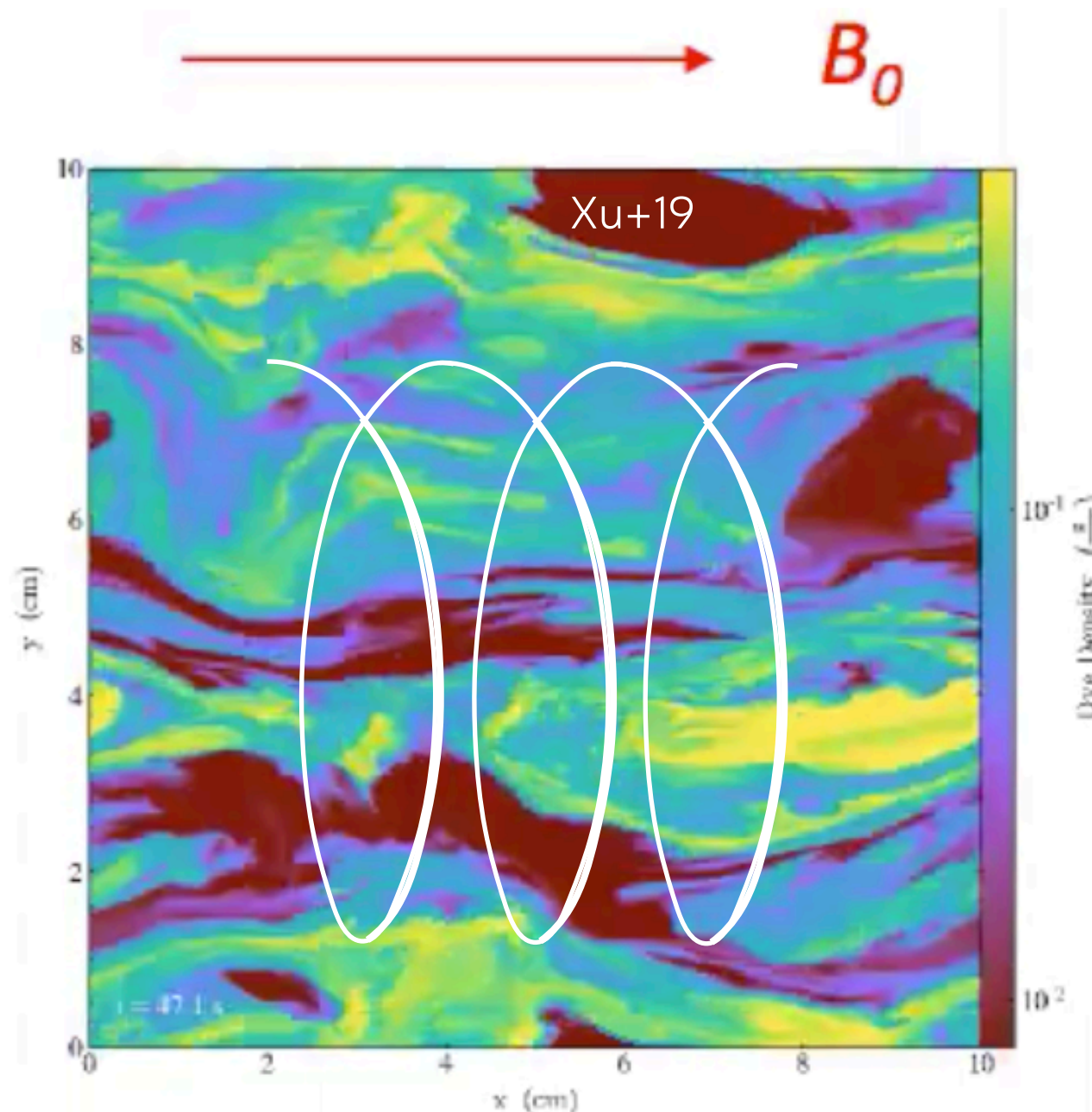
Goldreich & Sridhar 1995



scattering on pre-existing MHD turbulence

- inefficient scattering on anisotropic Alfvén modes
- small scattering efficiency preserved at small scales from the isotropic fast modes (but $\leq 20\%$ of MHD turbulence energy, if not damped)
- small role of slow modes
- ion-neutral damping for scales such that $E_k < E_{\text{dam}}$
 - ◆ Alfvén modes $E_{\text{dam,A}}$
 - ◆ slow modes $E_{\text{dam,s}}$
 - ◆ fast modes $E_{\text{dam,f}}$
- very fast diffusion in the WNM for all Galactic CRs
- slow diffusion in $\text{H}_2 > \text{TeV}$
- 2nd-order Fermi (re)acceleration

inefficient scattering for CRs $< 10 \text{ TeV}$ outside the Galactic halo

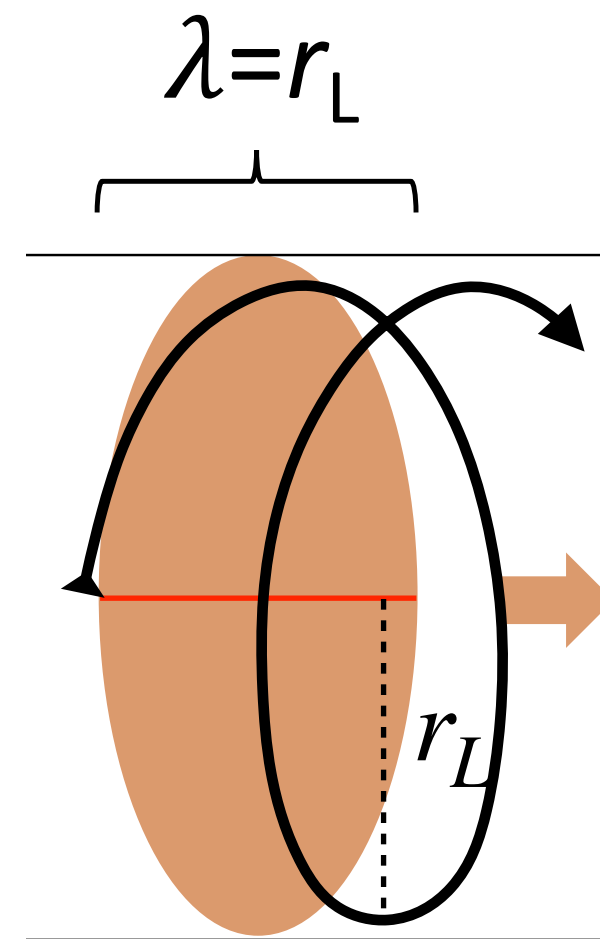


scattering on self-excited waves

$$\Omega_0 = \Omega_{class} = \gamma \Omega_{gyr}$$

- gyro-resonance: $k_{\parallel} v_{\parallel} - \omega_r \approx k_{\parallel} v_{\parallel} = \Omega_{gyr}$
- co-propagating wave excited by the **streaming instability**
 - if **locally anisotropic CR distribution**: $\Gamma_{grow} > 0$ if $\frac{\partial f}{\partial \mu} > 0$
 - excited by the **number density of all CR** with rigidity $> B/k$
- relation between CR anisotropy and spatial density gradient
 - if $f(p) = f_0(p) + \mu f_1(p) + \frac{1}{2} \mu^2 f_2(p)$ (small anisotropy)
 - relation $\frac{\partial f_1}{\partial \mu} = -\frac{v}{v_{sc}} \frac{\partial f_0}{\partial s}$ Zweibel 2013
- efficient pitch-angle scattering because $\lambda \sim R_{gyr}$
 - if strong coupling => CR isotropisation in the Alfvén wave frame => **advection at v_A down CR pressure gradients**

$$\mathbf{v}_{st} \rightarrow -\frac{\mathbf{B} \cdot \nabla \mathbf{P}_{CR}}{|\mathbf{B} \cdot \nabla \mathbf{P}_{CR}|} \mathbf{v}_A^{ion}$$



- if moderate coupling: faster diffusion (larger κ_{\parallel})

- no 2nd-order Fermi (re)acceleration

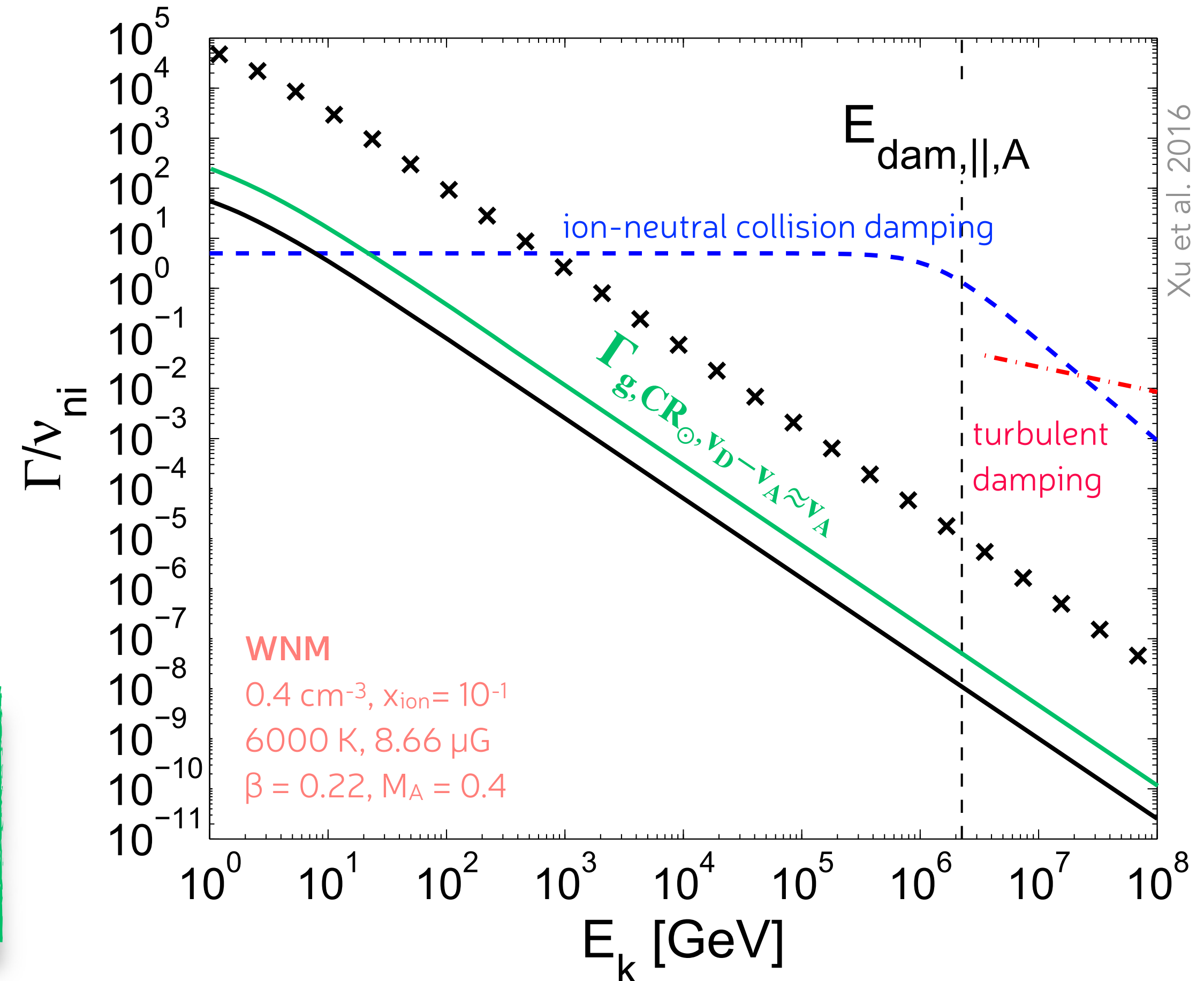
- CRs exert a force on the gas $-\nabla_{\parallel} \mathbf{P}_{CR}$
- CRs heat the gas $\text{rate} \propto \mathbf{v}_A^{ion} \cdot \nabla_{\parallel} \mathbf{P}_{CR}$

\approx efficient scattering for CRs $\lesssim 100$ GeV in the weakly ionised gas

$$\Gamma_{grow}(k) = \frac{\pi^2 q^2 v_A}{2 ck} \int \frac{v(1-\mu^2)}{cp} \left[\delta\left(\mu + \frac{m\Omega_0}{kp}\right) + \delta\left(\mu - \frac{m\Omega_0}{kp}\right) \right] \frac{\partial f}{\partial \mu} p^2 dp d\mu d\phi$$

resonance condition
for 2 circular polarisations

Kulsrud & Pearce 1969
Kulsrud & Cesarsky 1971

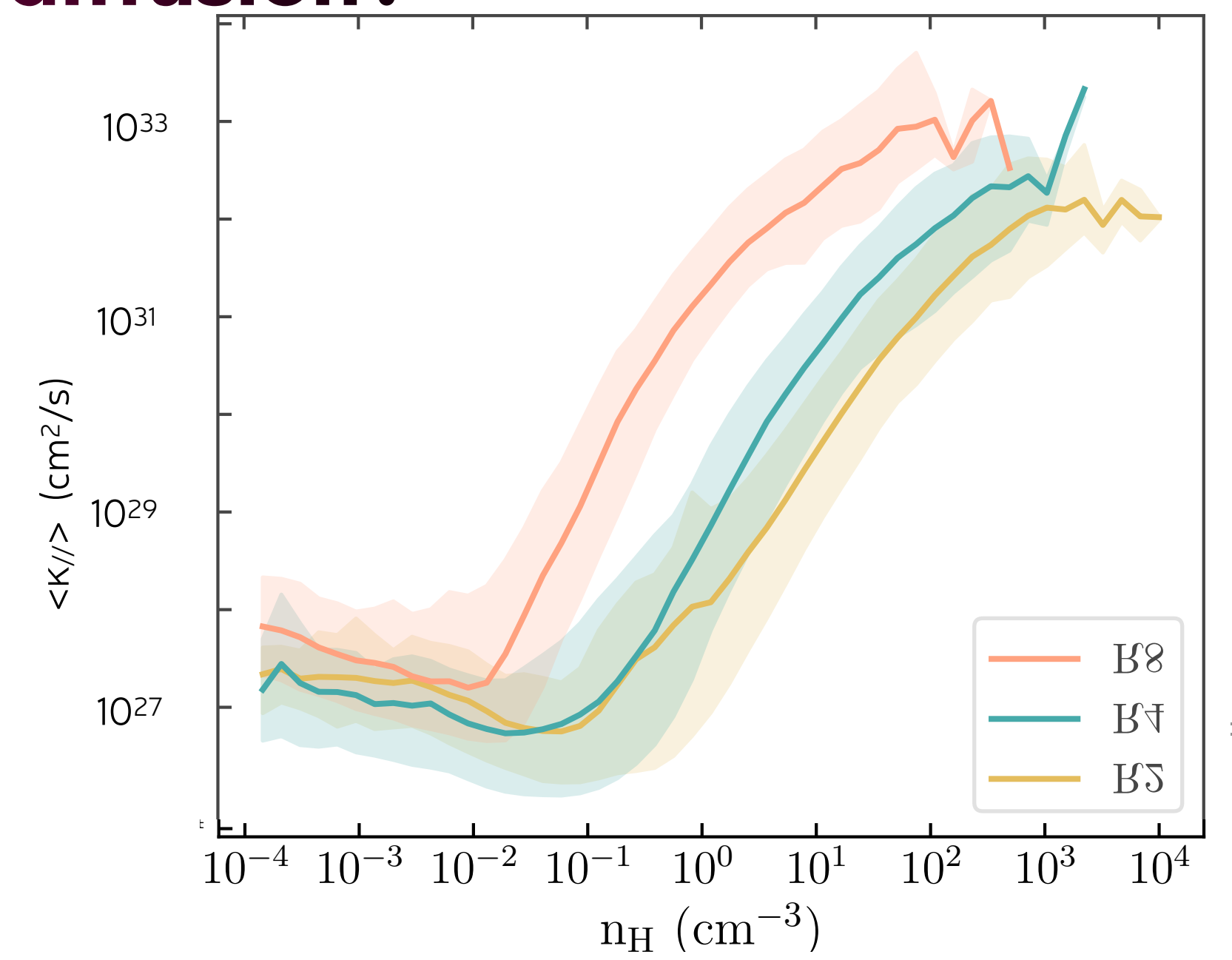
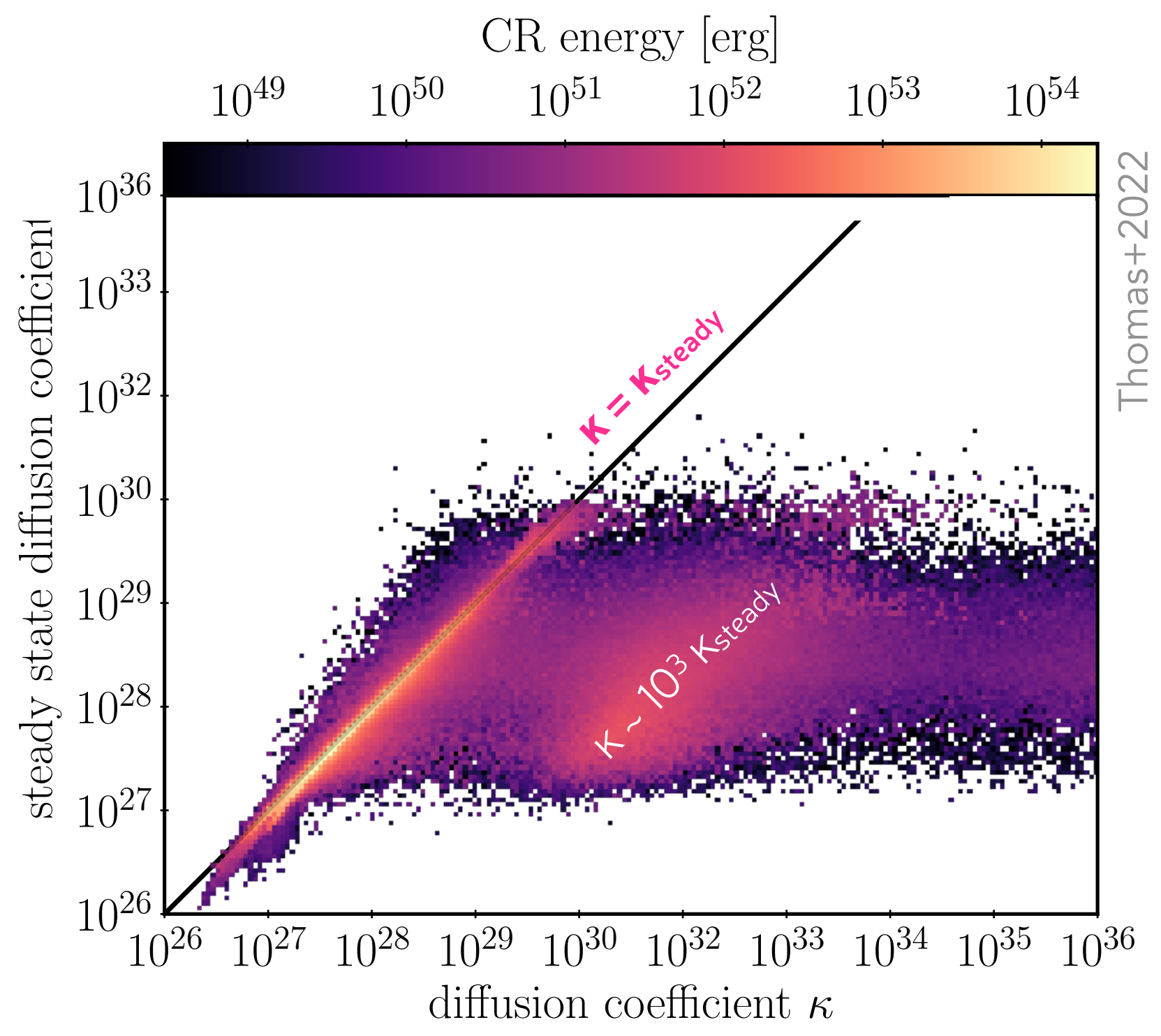


how fast do
cosmic rays travel ?



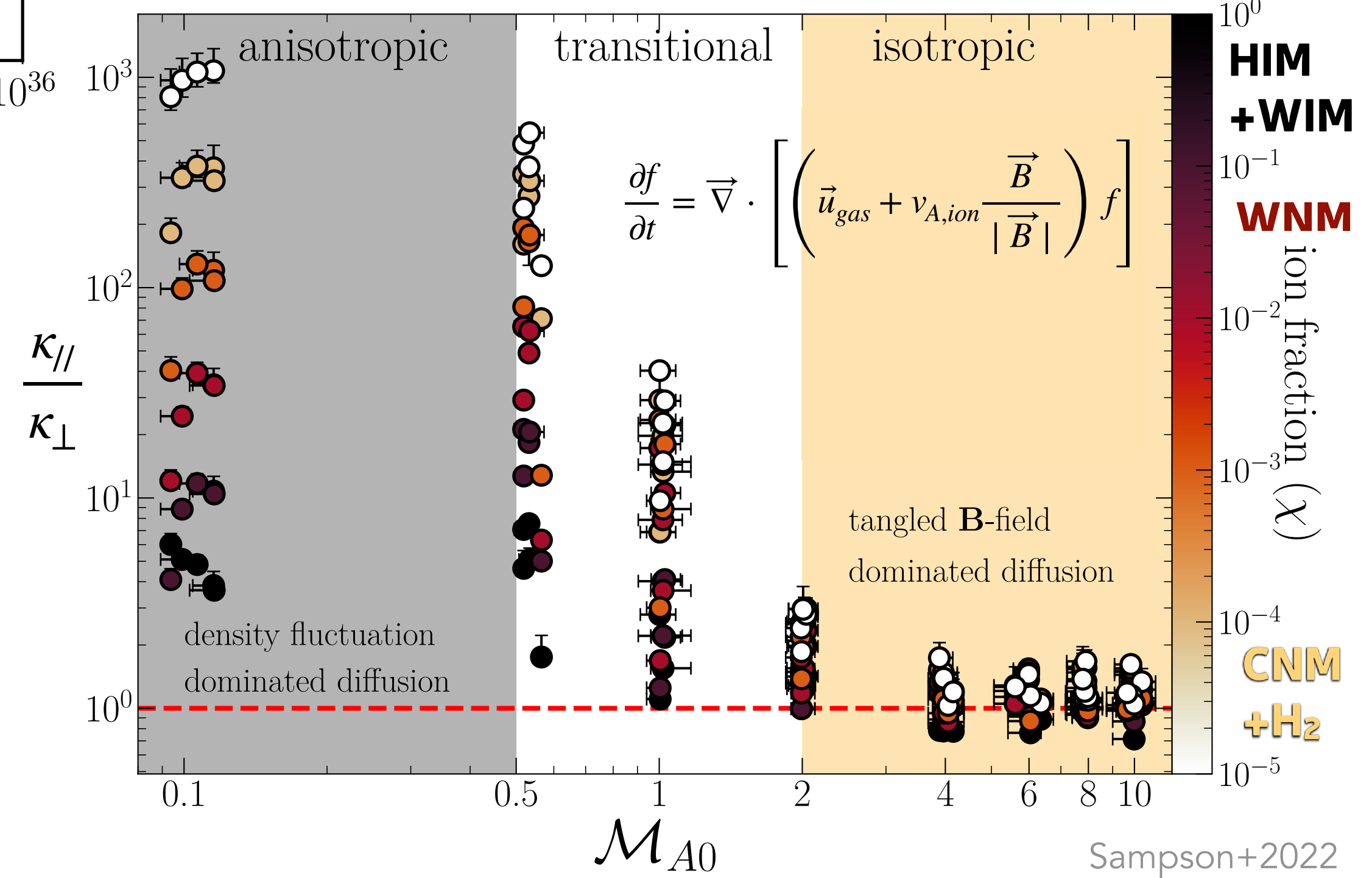
how fast, uneven, anisotropic is diffusion?

- if self-streaming transport
- steady-state approximation often holds
 - + Alfvén-wave dark regions where $\vec{B} \perp \vec{\nabla} P_{CR}$
- κ_{\parallel} variations by 50 to 1000 in multi-phase ISM



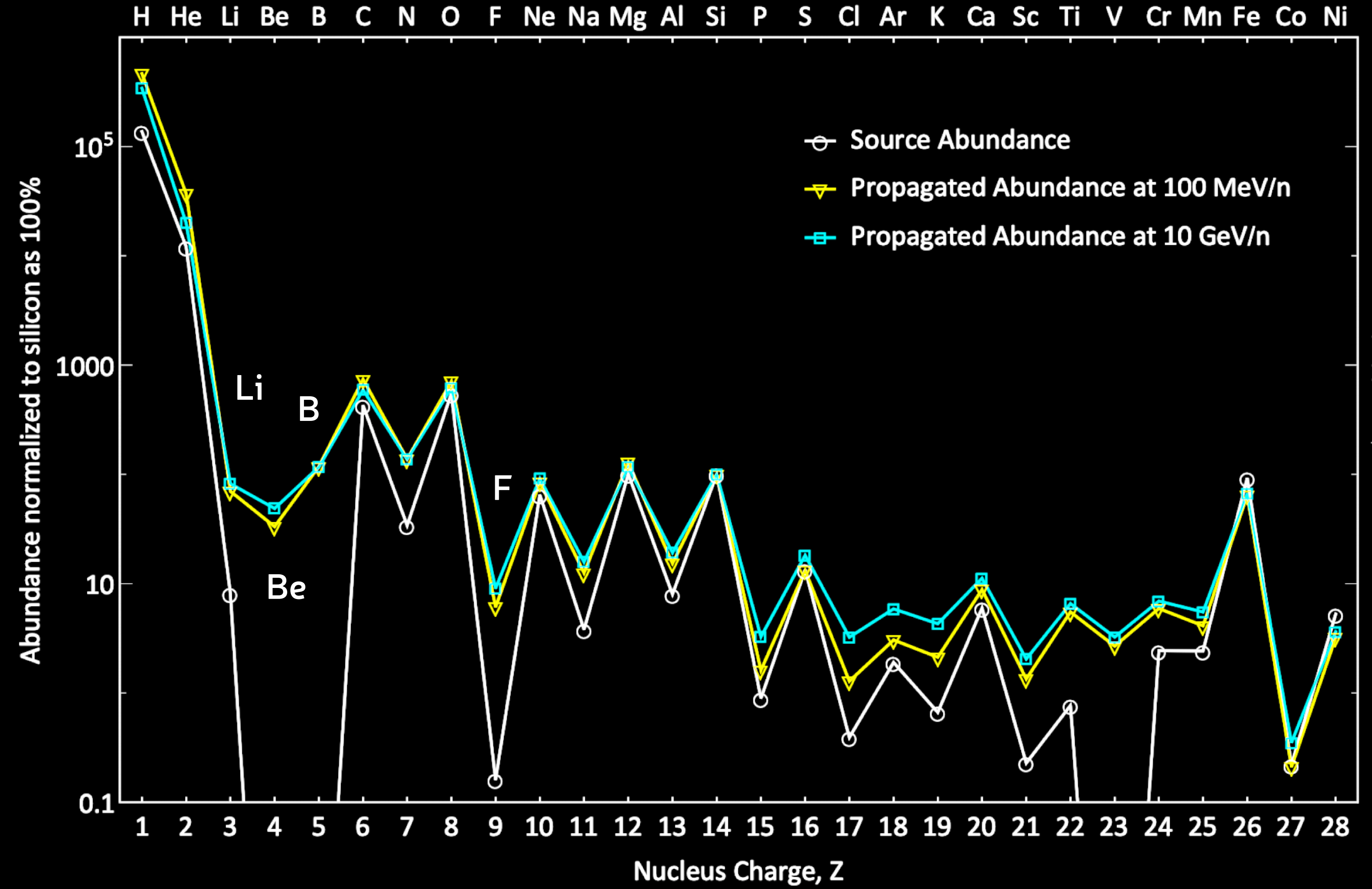
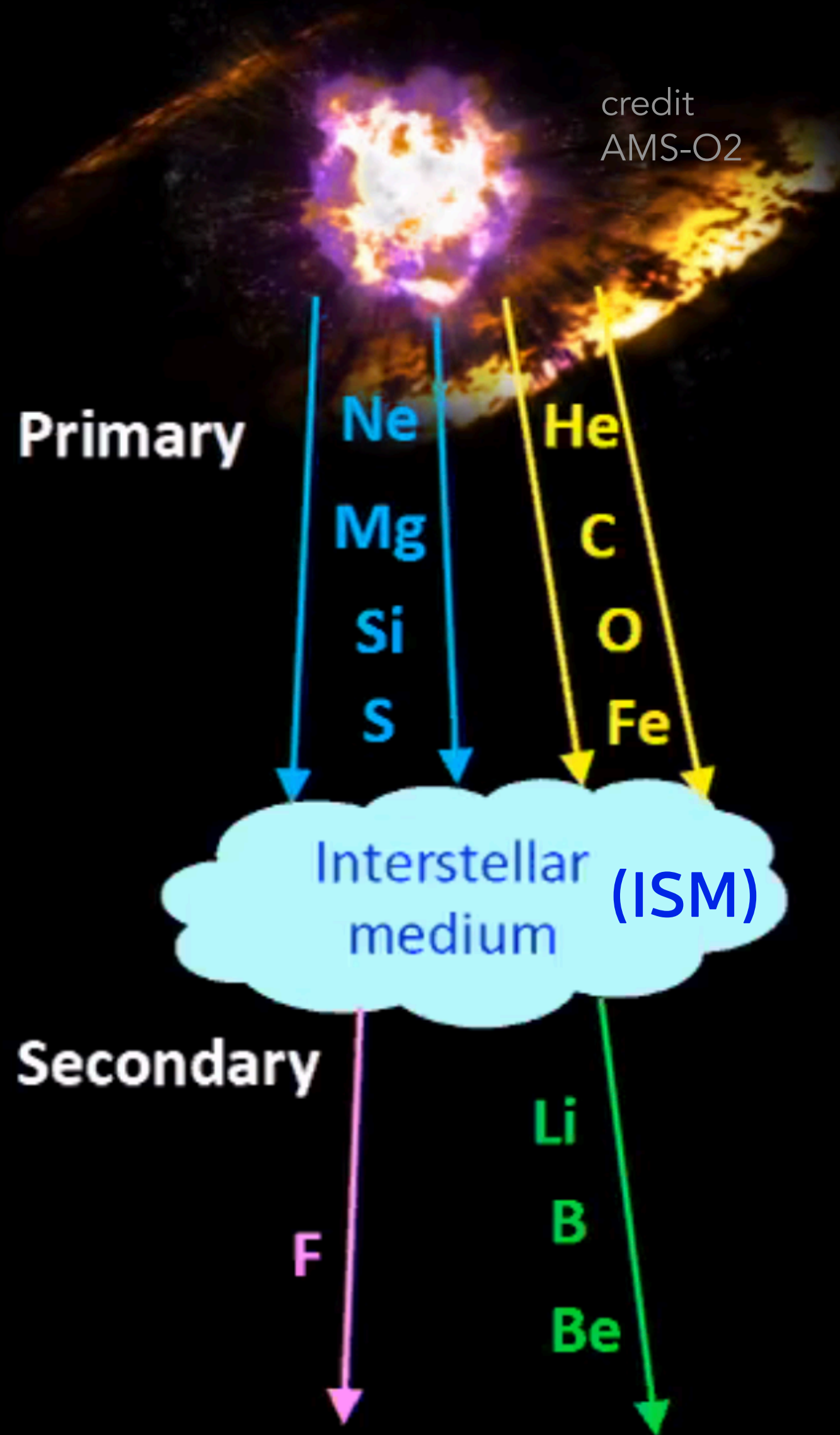
- if self-streaming CR transport with waves and CRs fully coupled
 - diffusion anisotropy varies with M_A and ionisation fraction
 - super-diffusion perpendicular to B, but also often along B

highly uneven & (an)isotropic IF self-excited scattering



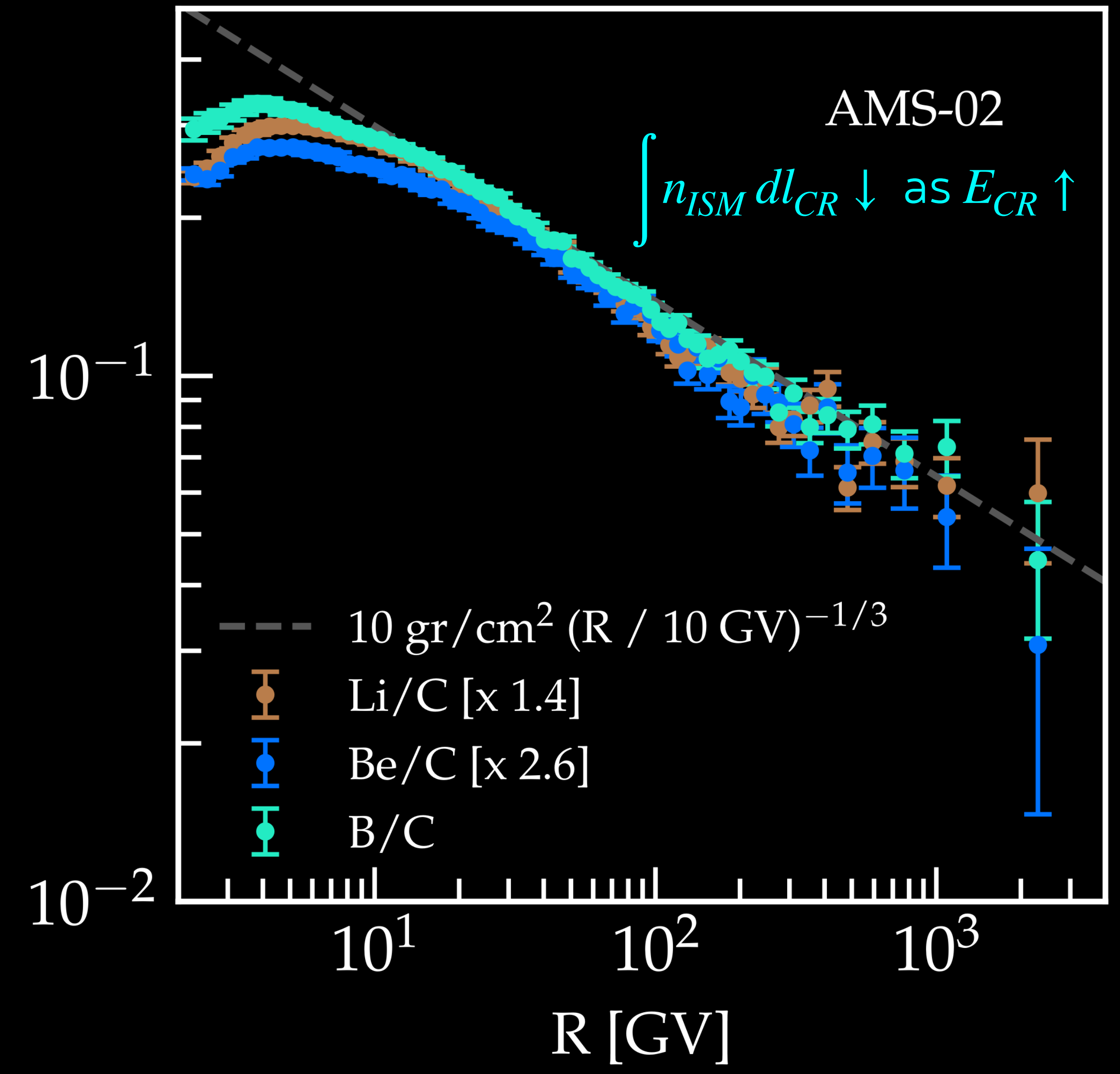
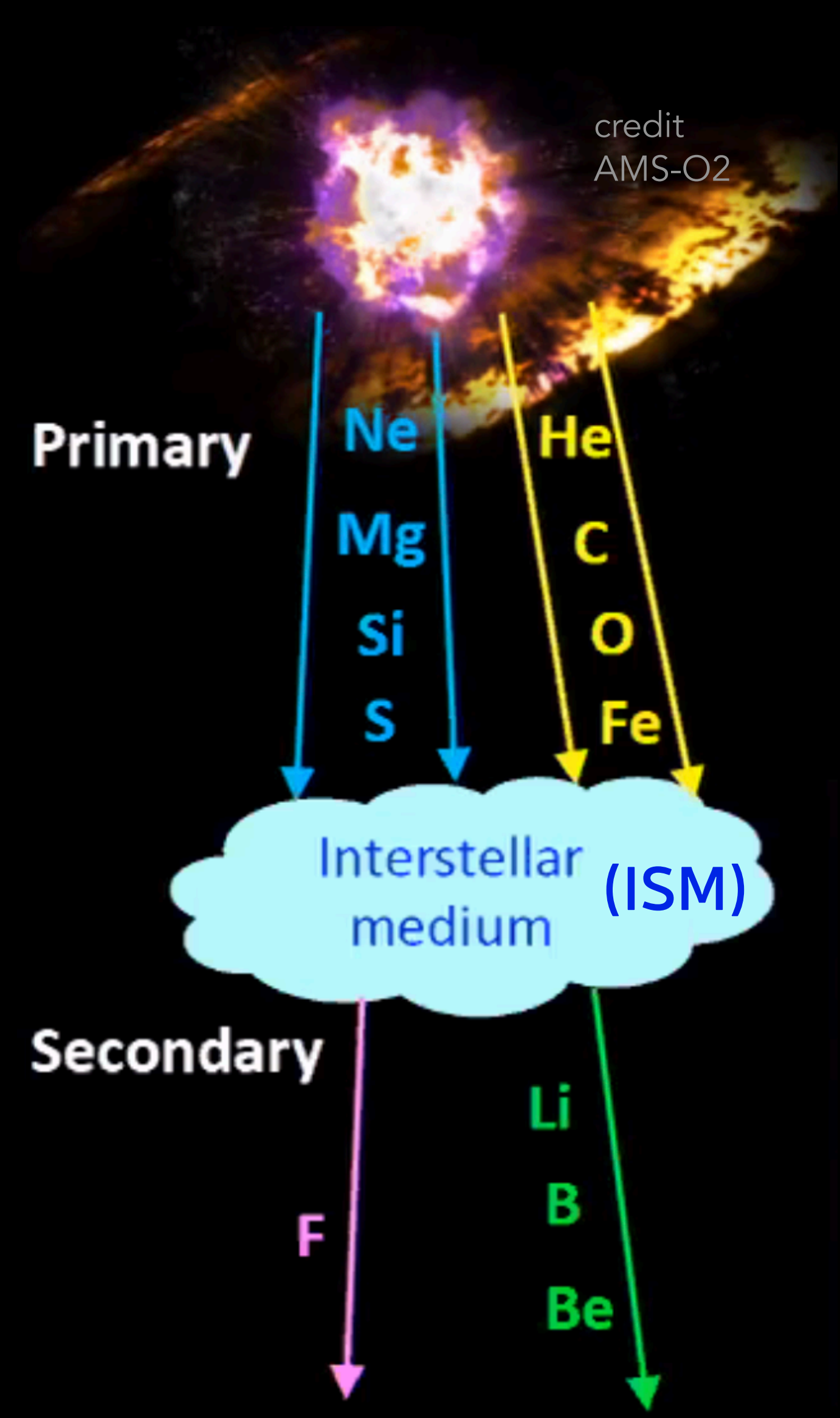
cosmic-ray composition vs. solar abundances

- 99% nuclei (~ 89% protons, ~ 10% He, ~ 1% heavier nuclei) + 1% electrons
- spallation reaction products in the interstellar medium



cosmic-ray composition vs. solar abundances

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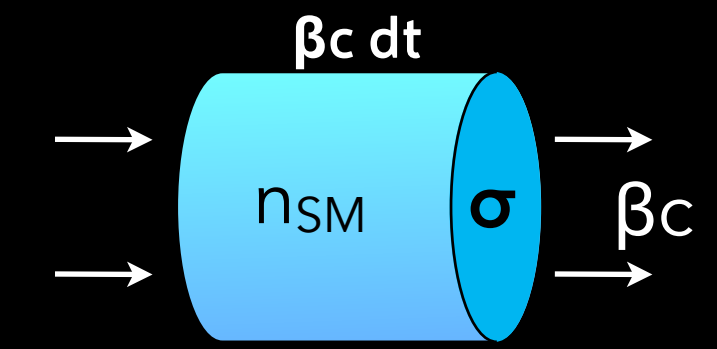


simplest leaky box model

- steady state between source input and loss + escape

$$\frac{M_a(p)}{T_{sp}(p)} + \frac{M_a(p)}{T_{esc}(p)} = Q_a(p)$$

- ISM grammage crossed before escape: $X(p) = n_{ISM} \beta(p) c T_{esc}(p)$



$$n_{ISM} \sigma \beta c dt = 1$$

- spallation reactions in the ISM

$$Q_2 = \frac{dM_2}{dt} = n_{ISM} \sigma_{1 \rightarrow 2} \beta c M_1$$

$$T_{sp2} = (n_{ISM} \sigma_{2 \rightarrow 3} \beta c)^{-1}$$

- secondary source input

- secondary spallation losses

$$\text{steady state} \Rightarrow M_2 \left[T_{sp2}^{-1} + T_{esc}^{-1} \right] = M_2 \left[n_{ISM} \sigma_{2 \rightarrow 3} \beta c + T_{esc}^{-1}(p) \right] = Q_2 = n_{ISM} \sigma_{1 \rightarrow 2} \beta c M_1$$

$$\frac{H^2}{\kappa(p)} = T_{esc}(E) \propto \kappa(p)^{-1}$$

- 2dary/1ary ratio

$$\frac{M_2(p)}{M_1(p)} = \frac{\sigma_{1 \rightarrow 2}}{\sigma_{2 \rightarrow 3} + X^{-1}(p)}$$

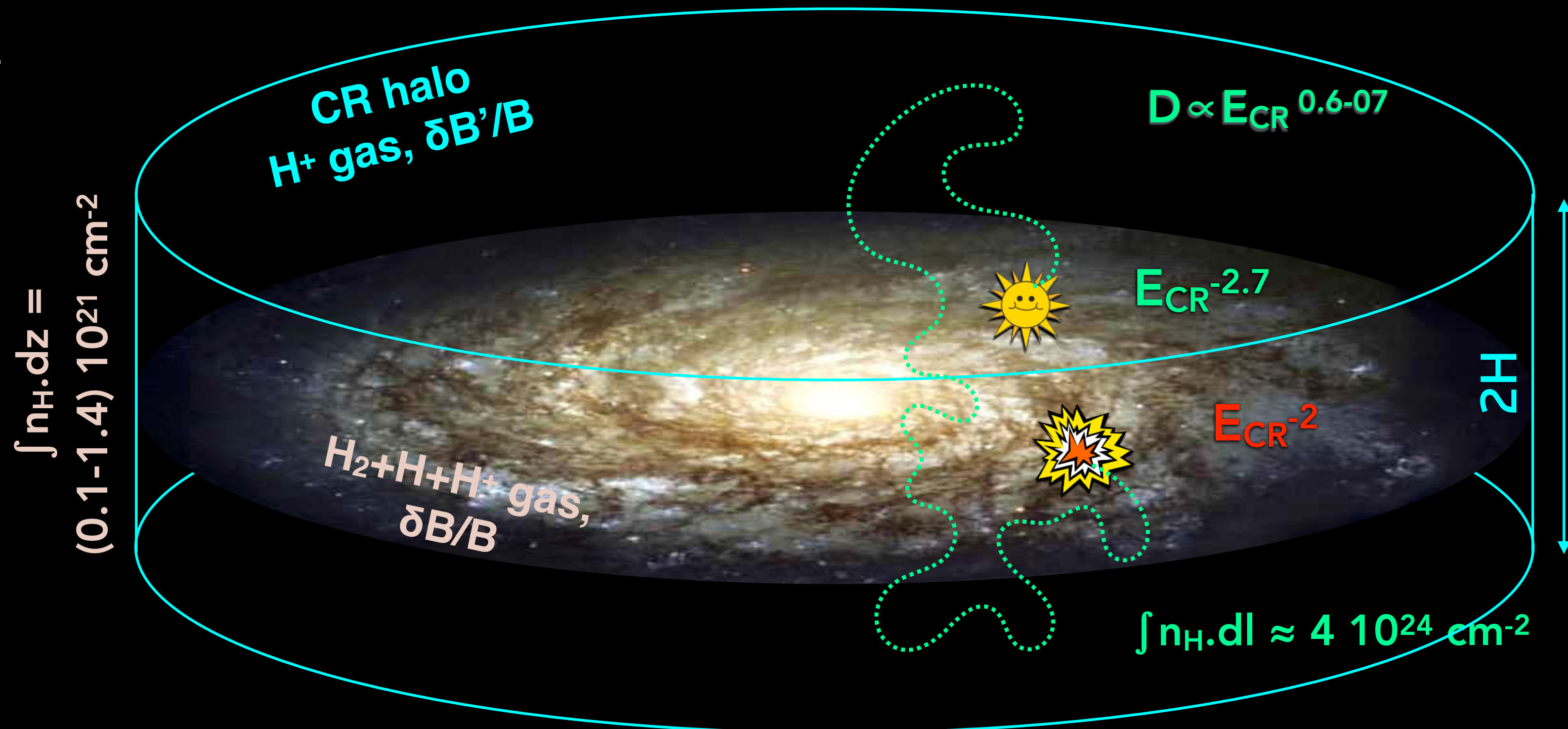
$$\frac{M_2}{M_1} \rightarrow X(p) \propto T_{esc}(p) \propto \kappa^{-1}(p)$$

$$\frac{M_2}{M_1} \propto p^{-\delta} \Rightarrow D(p) \propto p^{\delta}$$

- $X \approx 10 \text{ g/cm}^2$ or $N_H \approx 4 \cdot 10^{24} \text{ cm}^{-2}$

- radioactive secondaries : CR clocks

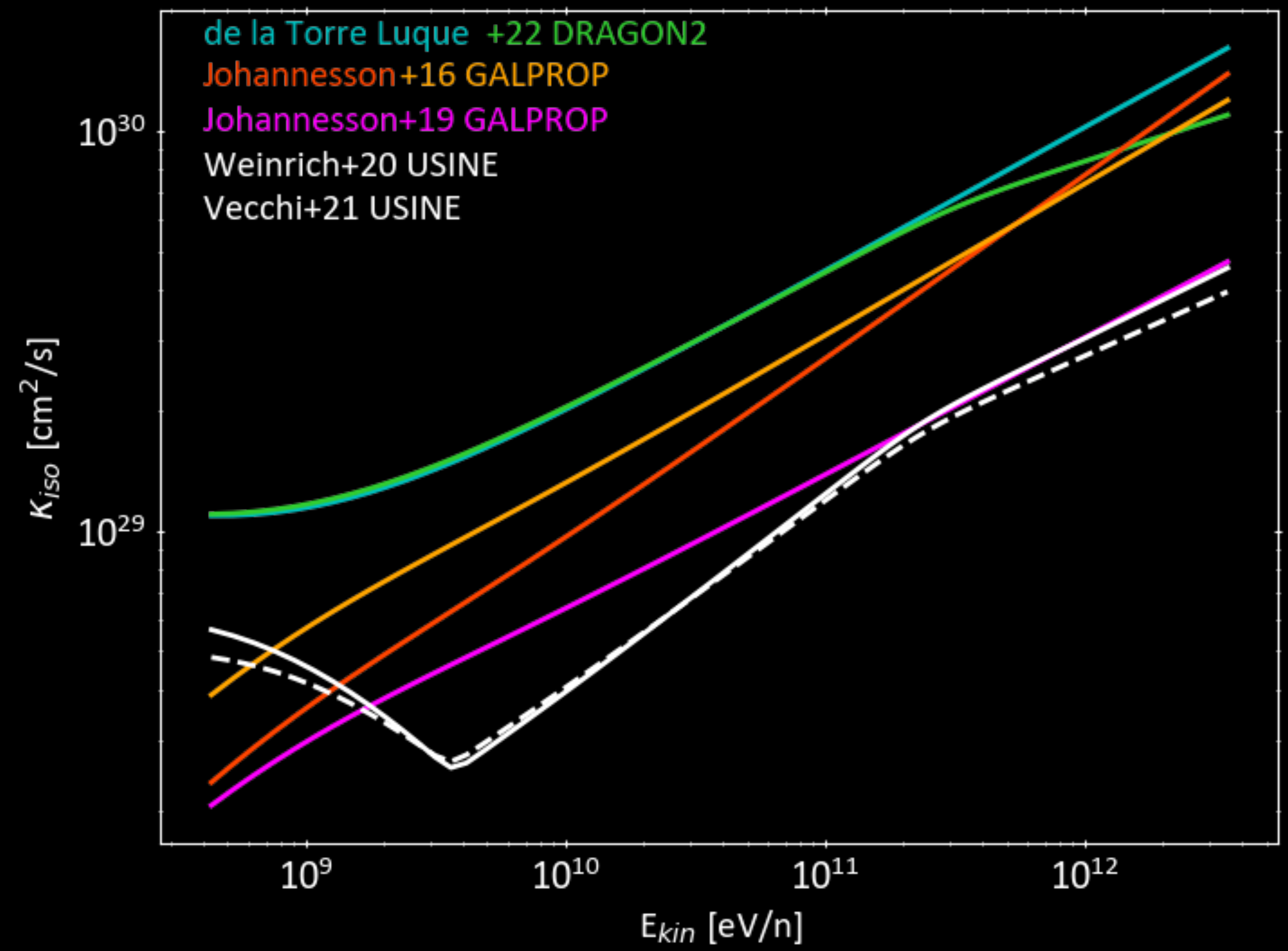
- $T_{esc} \approx 10\text{-}20 \text{ Myr}$



1D - 2D - 3D diffusion codes

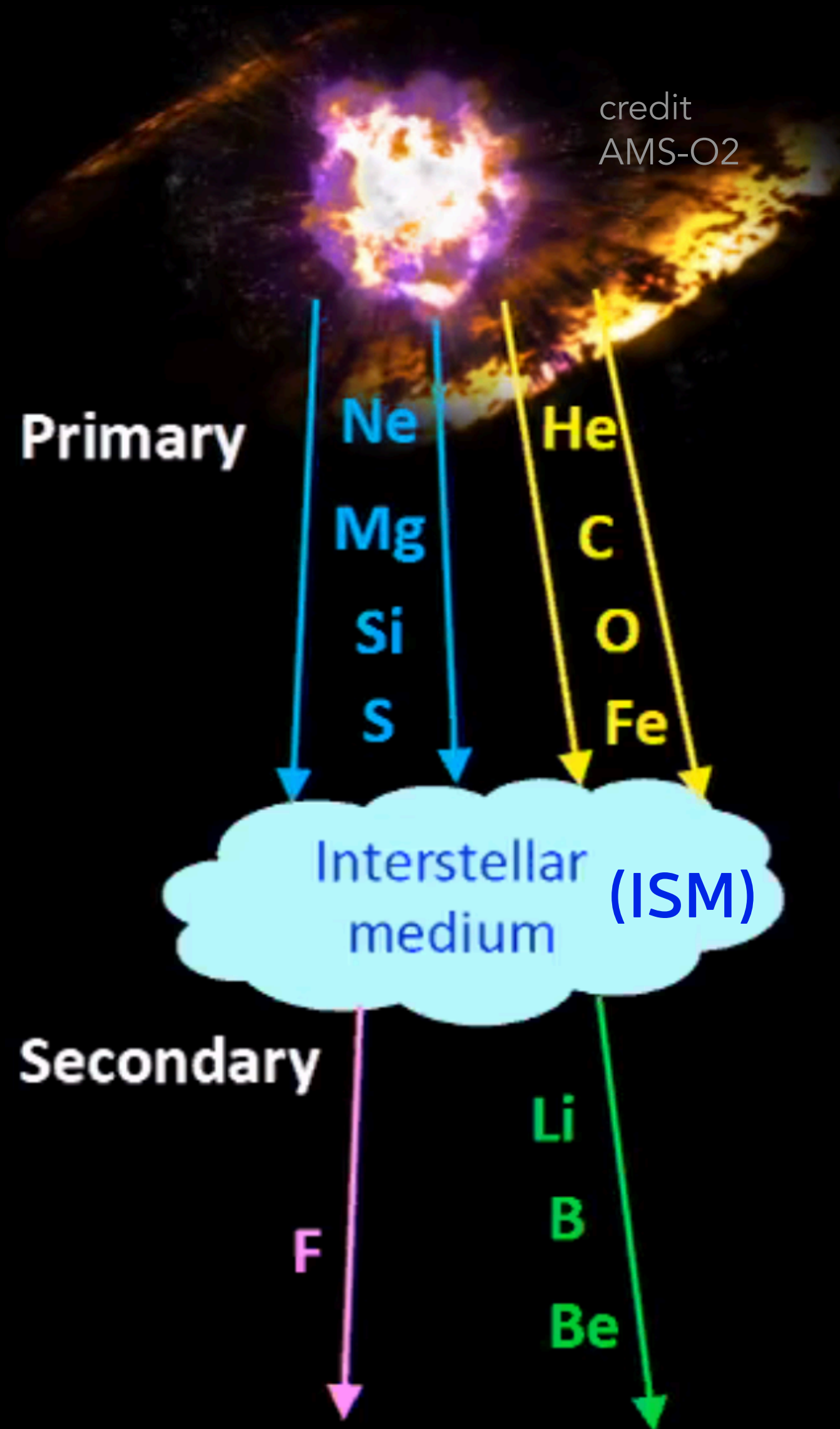
- mean uniform diffusion coefficient in the Milky Way

$$\kappa(\text{GeV}/n) \approx 10^{28-29} \text{ cm}^2/\text{s}, \quad l_{\text{scat}} \approx 3\kappa/c \sim 1 \text{ pc}$$

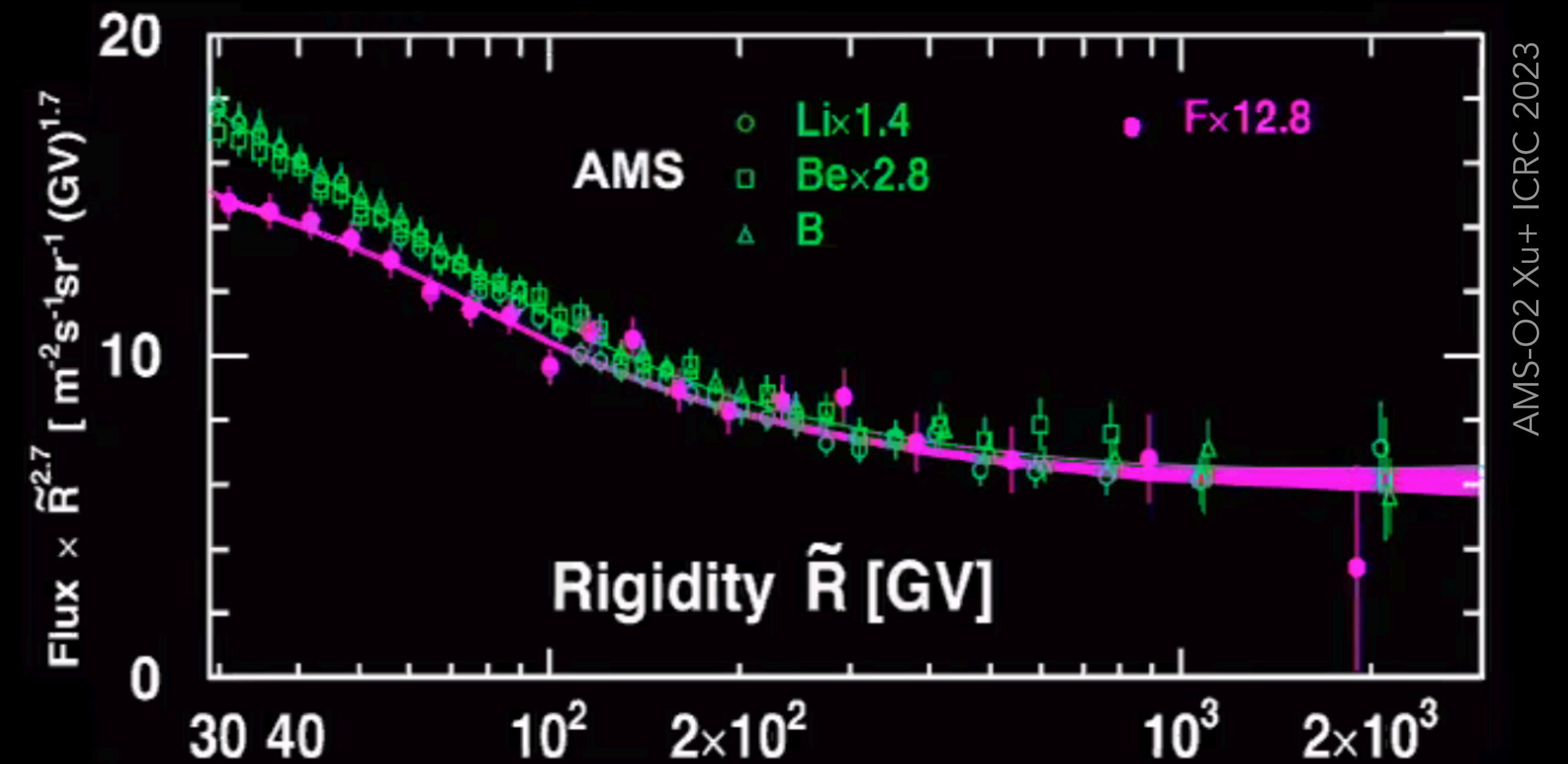
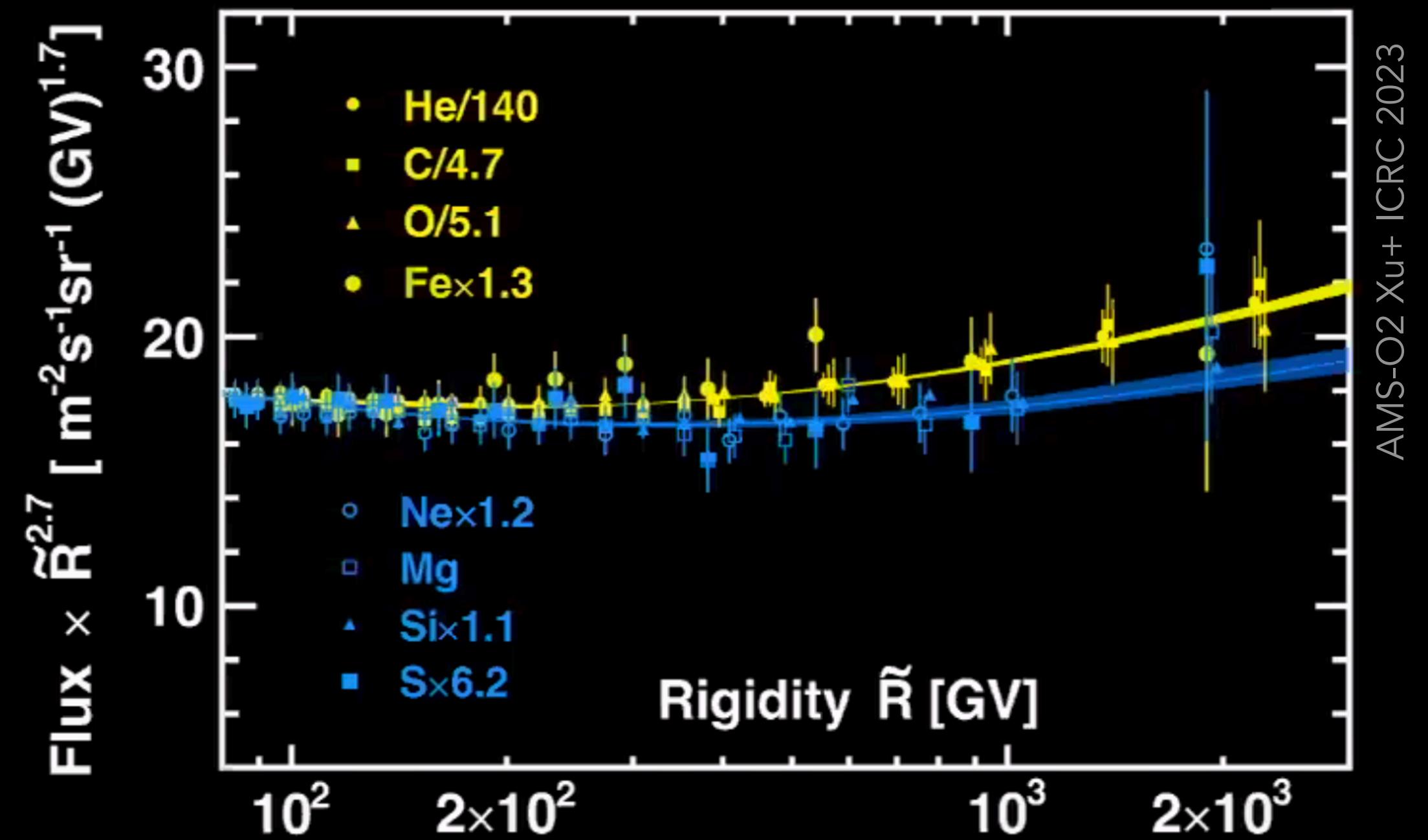


cosmic-ray composition vs. solar abundances

- but 2 classes of CR primaries, with secondary contamination



- but 2 classes of secondaries



total cosmic-ray power

- total power \geq GeV
- from spallation residence time Δt_{cr} and grammage $X_{cr} \sim \rho_{ISM} c \Delta t_{cr}$

Dogiel+2002

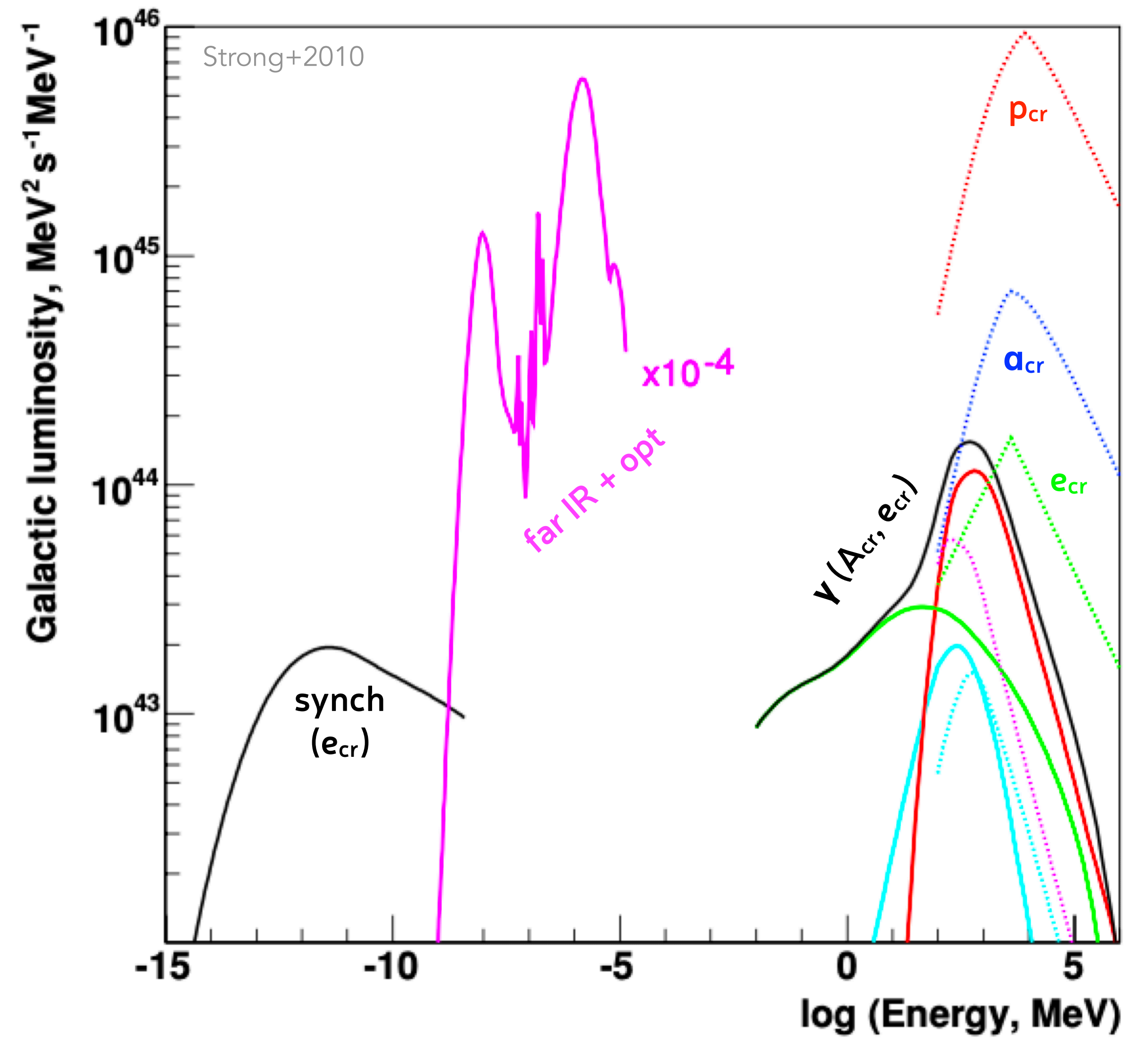
$$P_{cr} \sim \frac{E_{CR}}{\Delta t_{cr}} = \frac{u_{cr} V_{gal}}{\Delta t_{cr}} = \frac{u_{cr} V_{gal} \rho_{ISM} c}{X_{cr}} = \frac{u_{cr} c M_{ISM,gal}}{X_{cr}}$$

- $M_{ISM} = 10^{10} M_{\odot} \approx 2 \cdot 10^{40} \text{ kg}$, $X_{cr} \approx 10^2 \text{ kg/m}^2$

$$P_{cr} \approx 10^{34} \text{ W}$$

- total Milky Way CR power from GALPROP diffusion model = $(0.7 - 0.8) 10^{34} \text{ W}$

10% of the total power of supernova explosions in the Milky Way

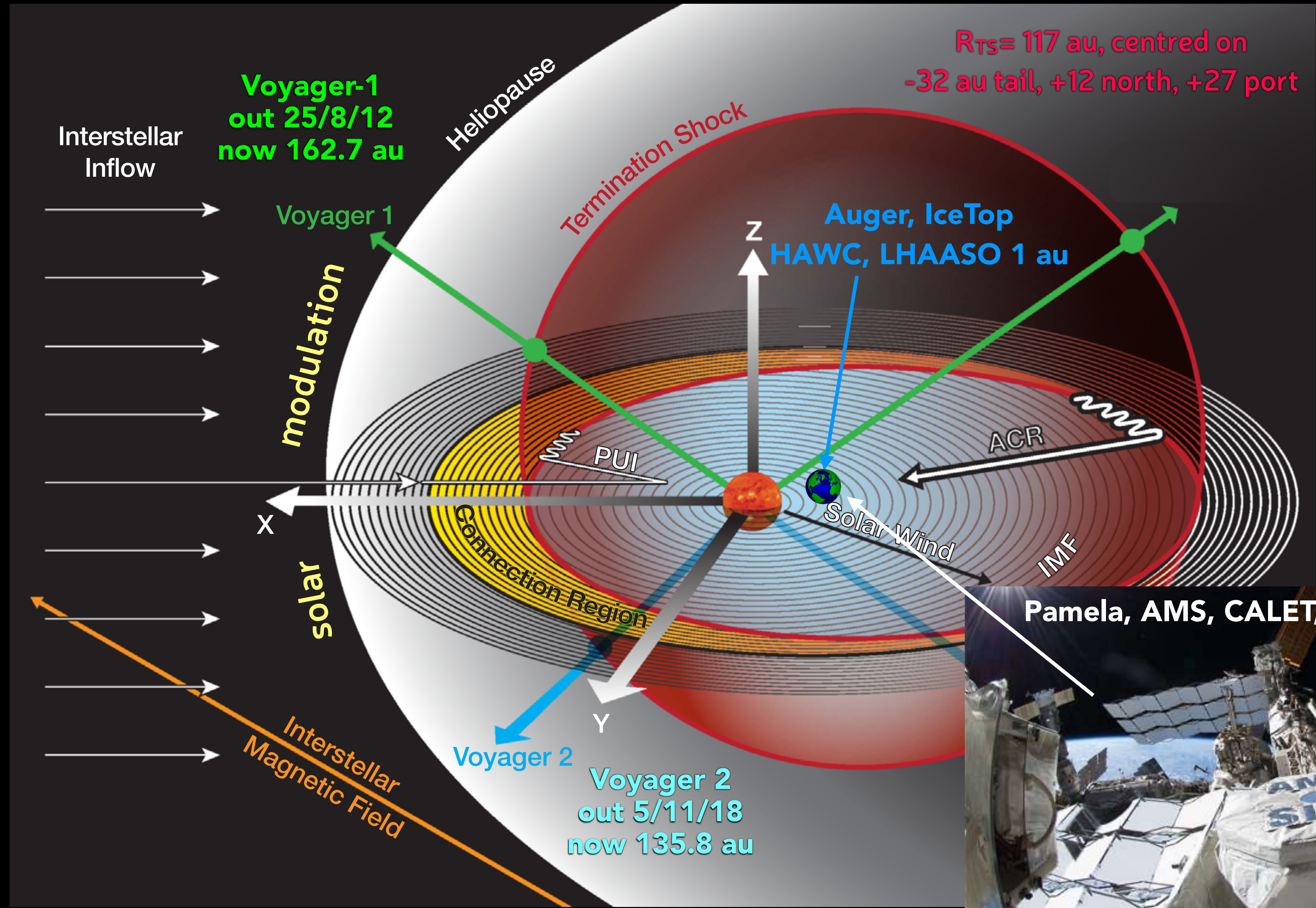


wicked data



outer-space collection

McComas+ 2019

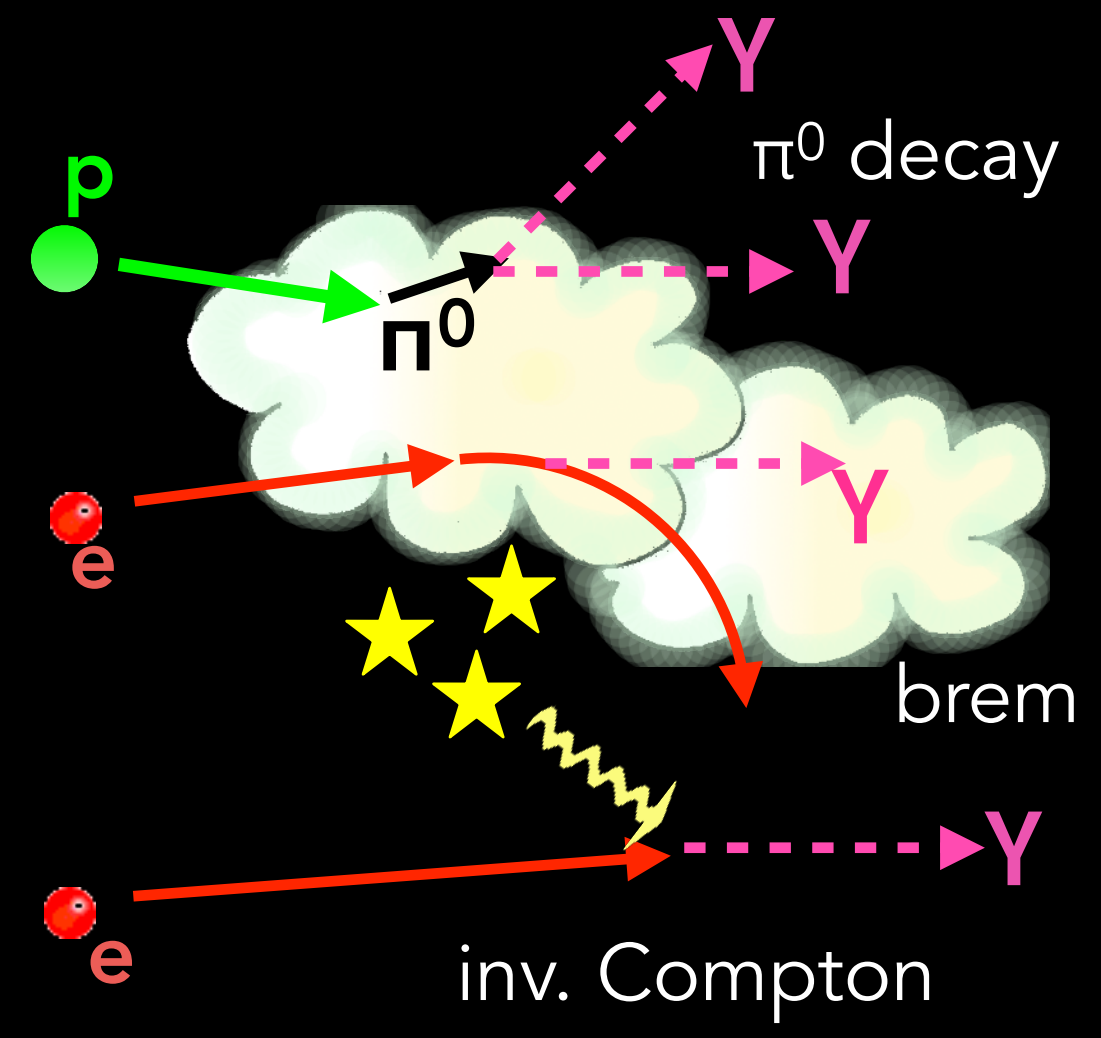


$R_{TS} = 117$ au, centred on
-32 au tail, +12 north, +27 port

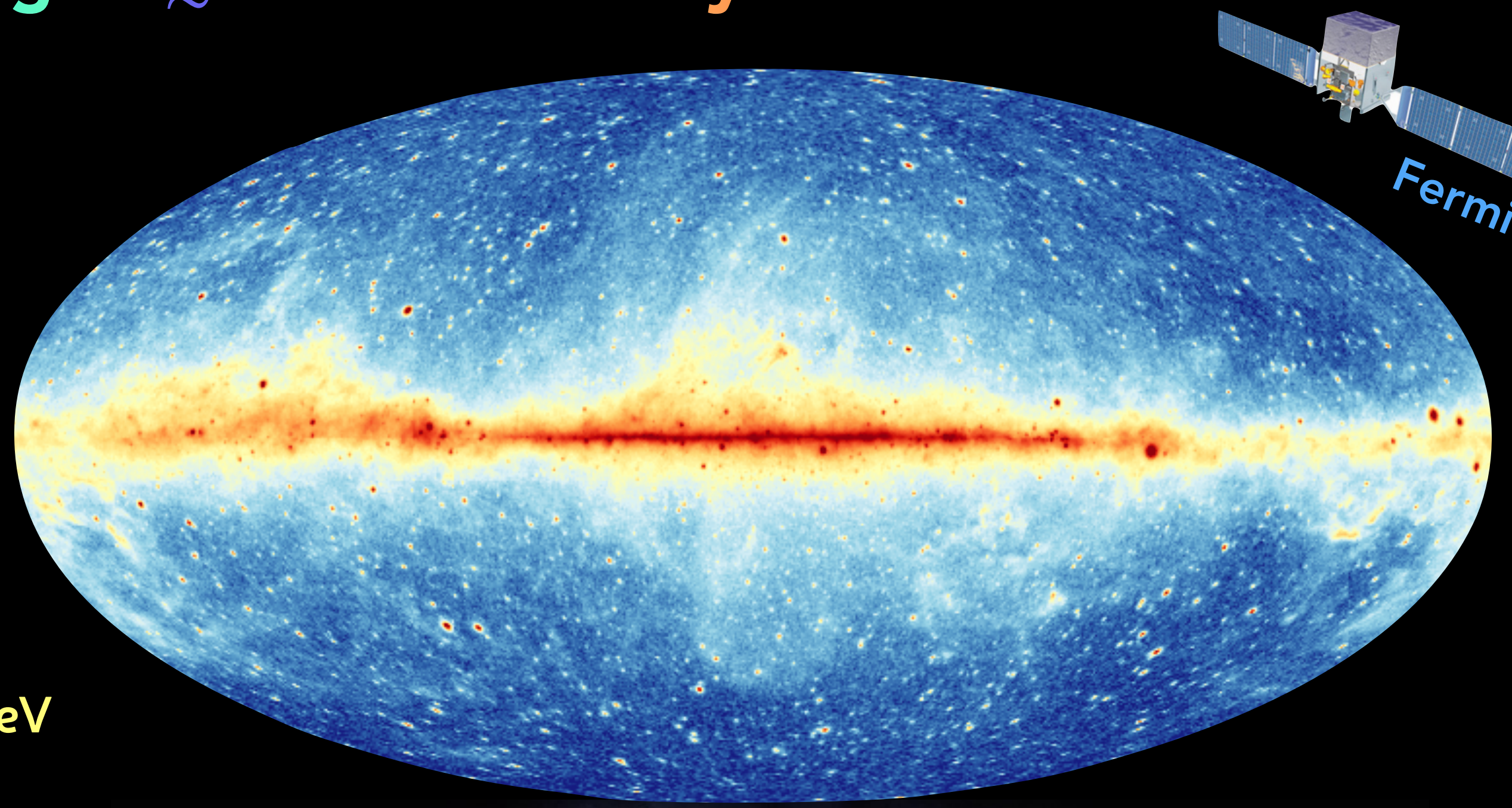
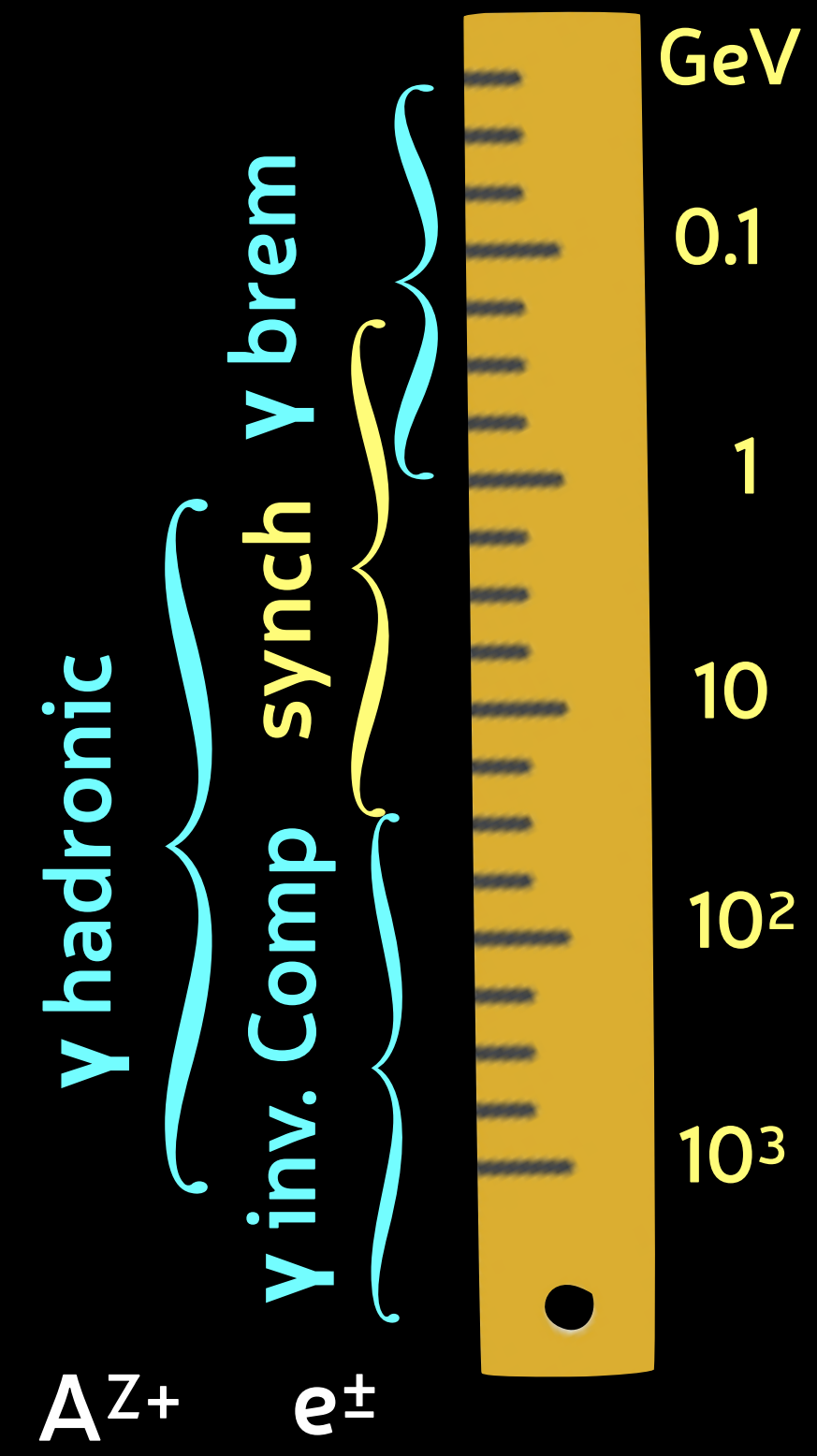
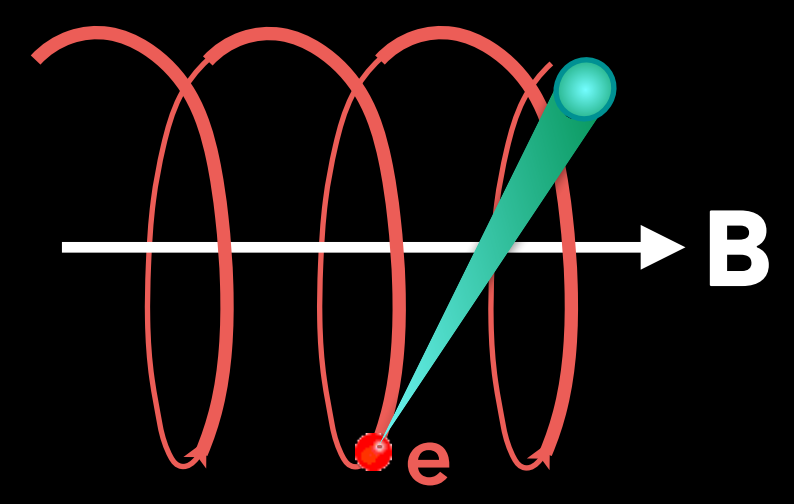


remote sensing of \gtrsim GeV cosmic rays

- $\Delta Z^+ + e^\pm$ probed in γ rays
- Fermi LAT $>$ GeV

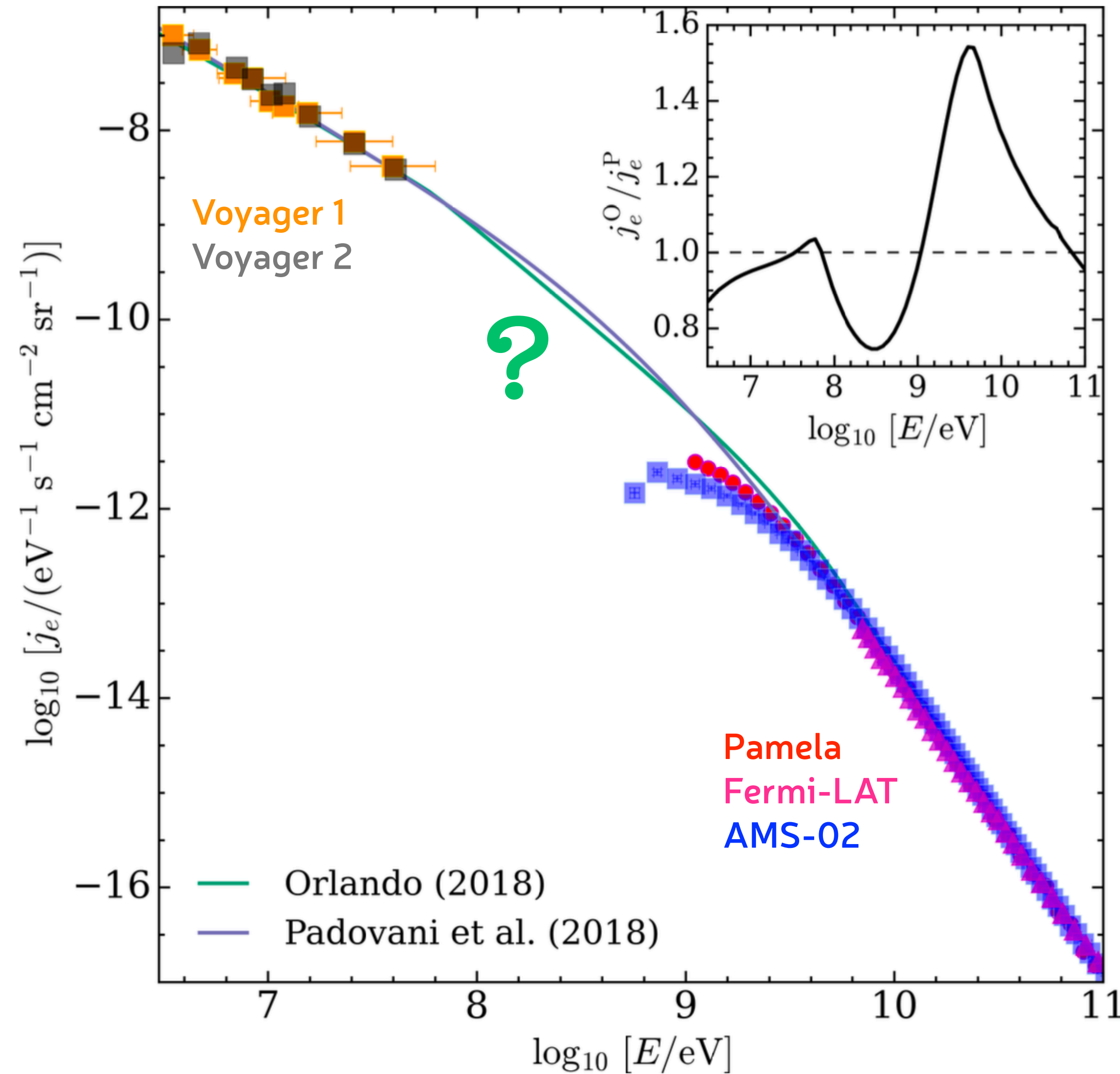


- e^\pm probed by radio synchrotron
- 30 haloes piled-up by Chan-ges



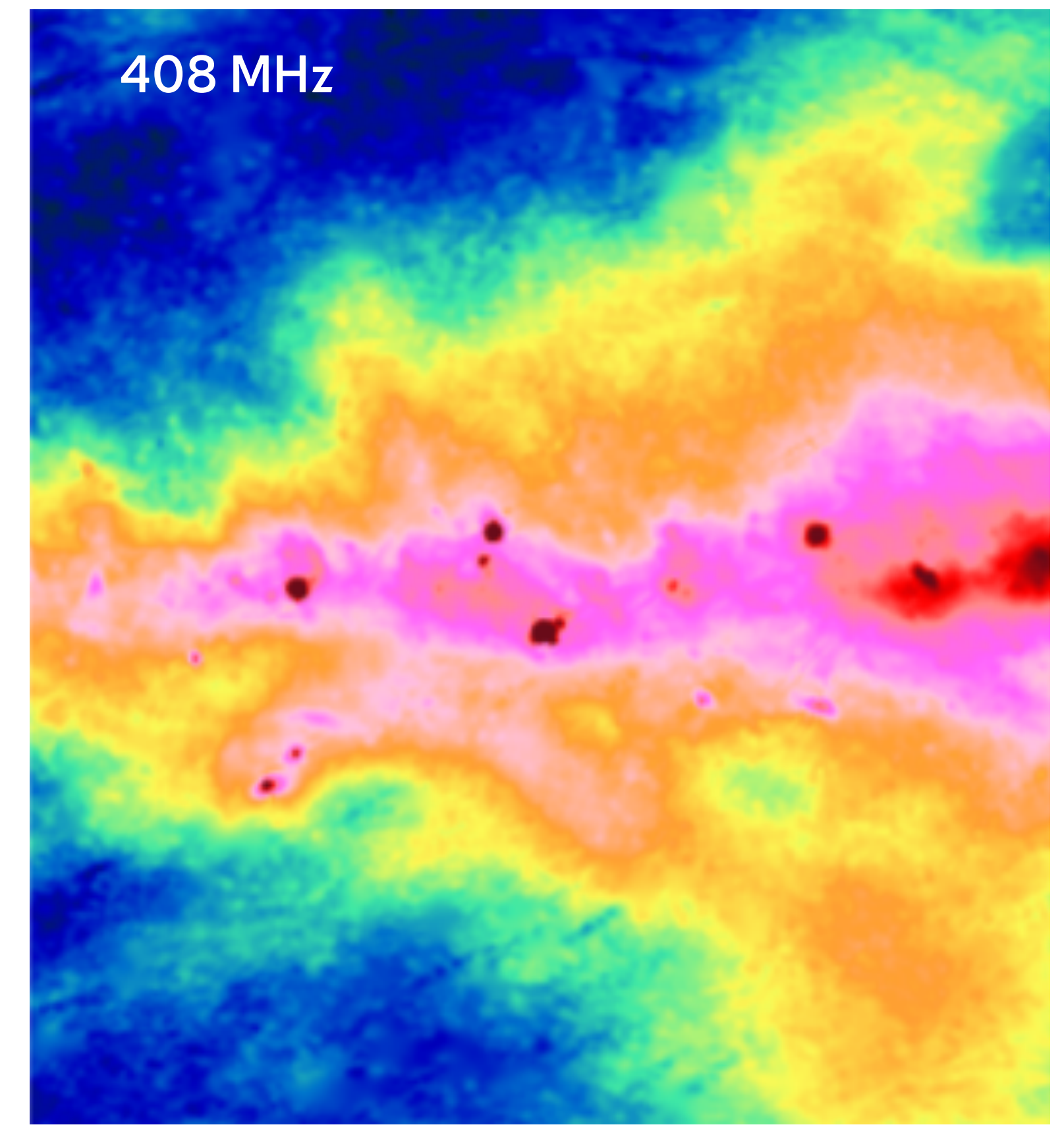
radio tracing difficulties

- $B_{\text{ISM}} \approx 2 - 20 \mu\text{G}$, $\nu_{\text{radio}} = 0.1-10 \text{ GHz} \Rightarrow 0.1 \leq E_e \leq 50 \text{ GeV}$ in the unknown spectral range where significant change in slope
- B_{\perp} variations along the line of sight and in the telescope beam



if $n(E_e) = \kappa \left(\frac{E_e}{E_0} \right)^{-p}$

$$S_{\nu} \propto \int \kappa B^{\frac{1+p}{2}} \nu^{\frac{1-p}{2}} dl$$



radio tracing problem

- collapse of “elongated” clouds along B with $h_{\parallel} > R_{\perp}$ and mass $M \propto \rho R^2 h$
- virial equilibrium $c_s^2 \propto \Phi_g \propto \rho h^2$ and magnetic flux: $BR^2 = cte \Rightarrow B \propto c_s \rho^{1/2}$
- equipartition between magnetic and kinetic (thermal+turbulent) energy densities: $\frac{B^2}{2\mu_0} \propto \rho \sigma_v^2 \Rightarrow B \propto \sigma_v \rho^{1/2}$
- why don't we see the dense clouds in synchrotron emission?

