

Protoplanetary Disks

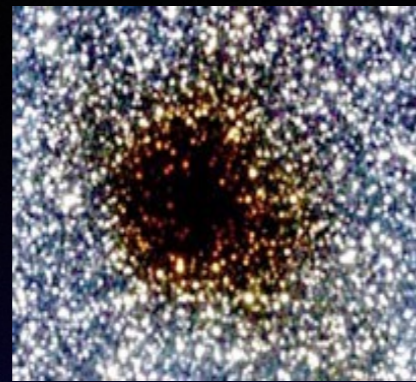
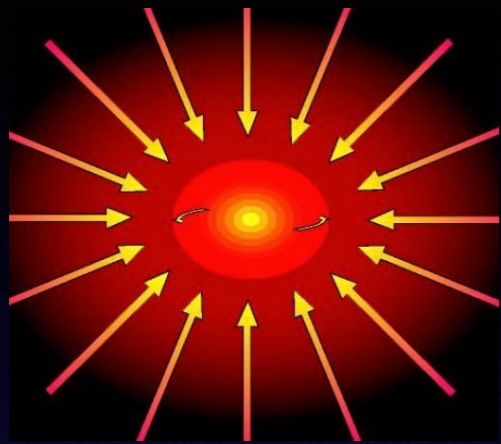
(the dirty job part I)

Leonardo Testi - UniBo
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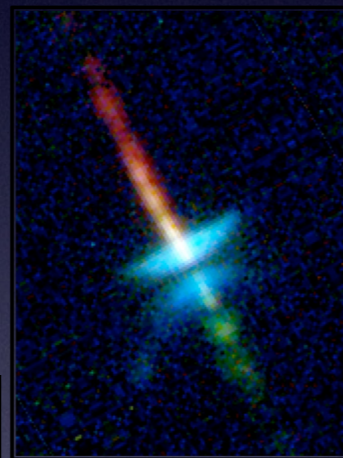
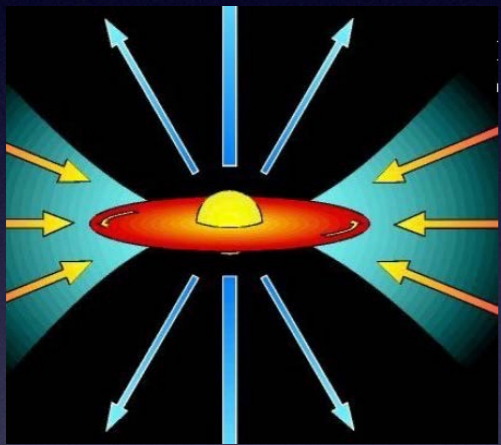
- Most of the focus will be on Class II disks
- How we determine the key properties of these systems
- Stellar masses and ages
- Disk physical parameters
- Evolution of the disk and its constituents



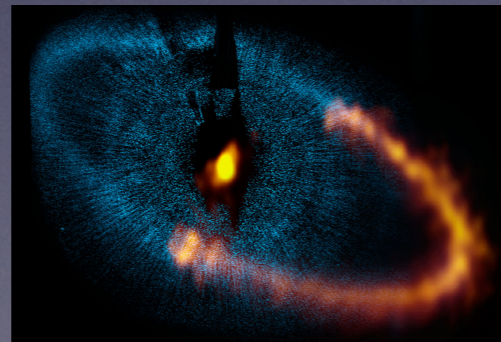
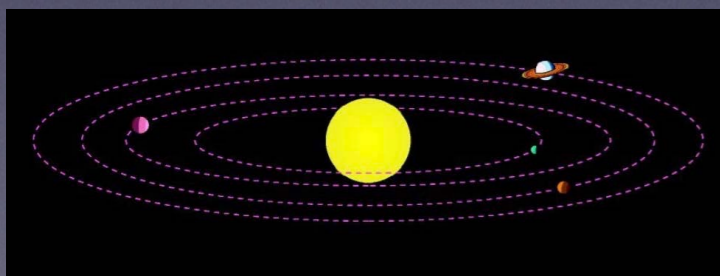
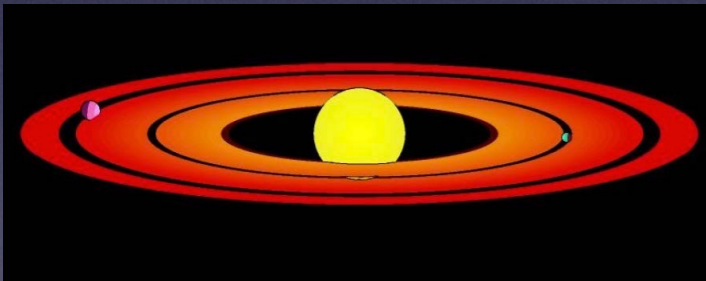
From Cores to Planetary Systems



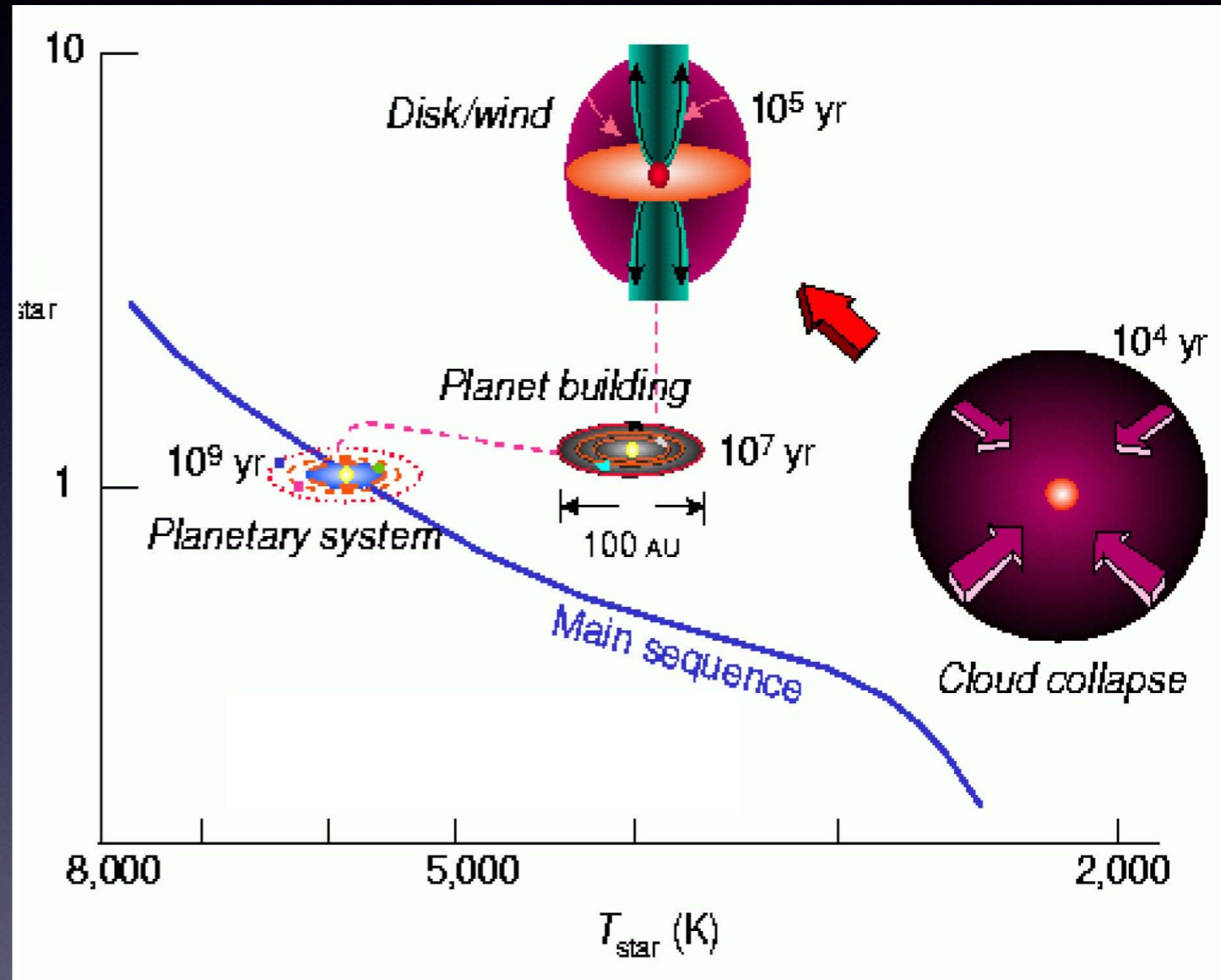
Core



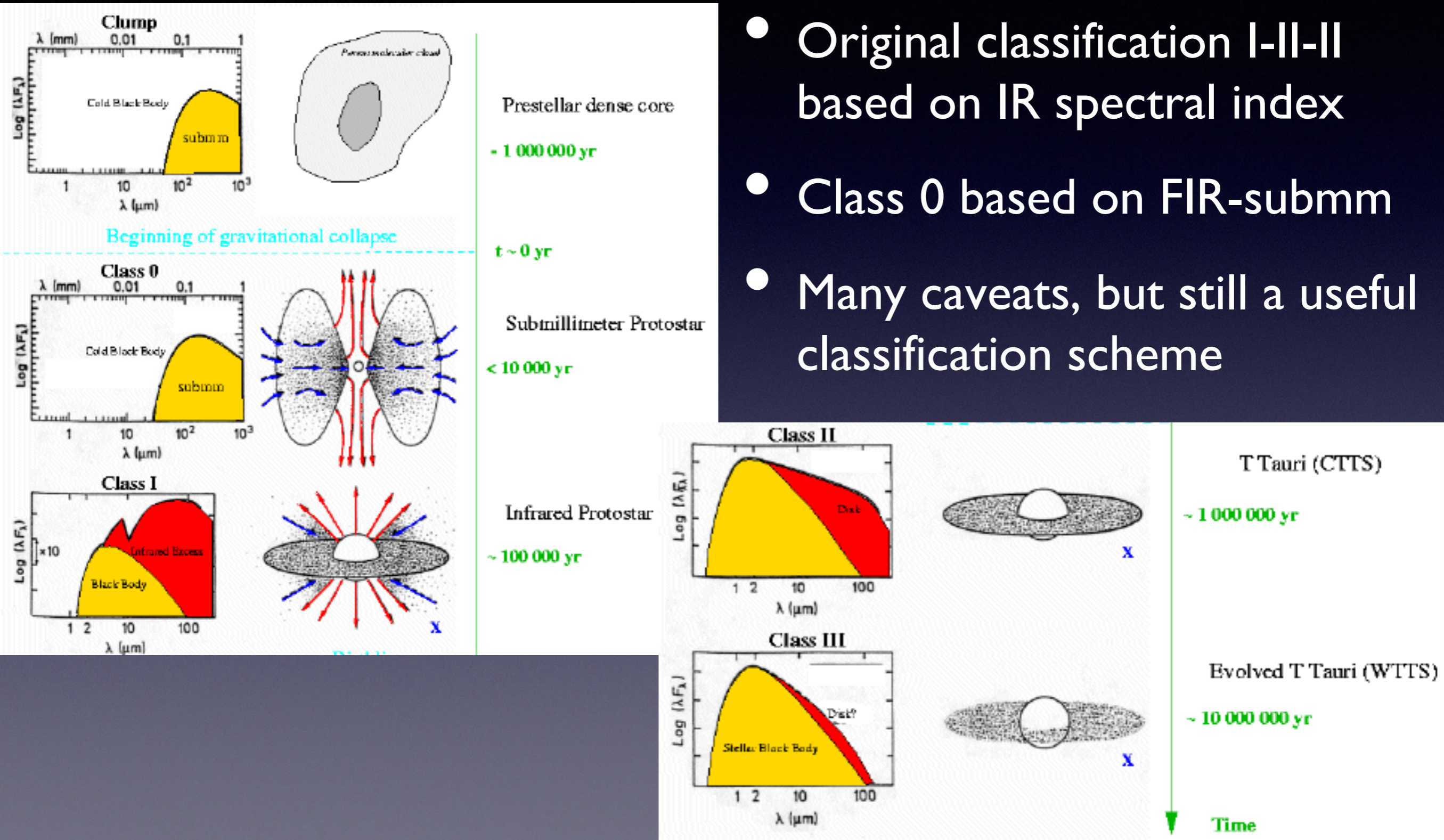
Disk



Debris Disk

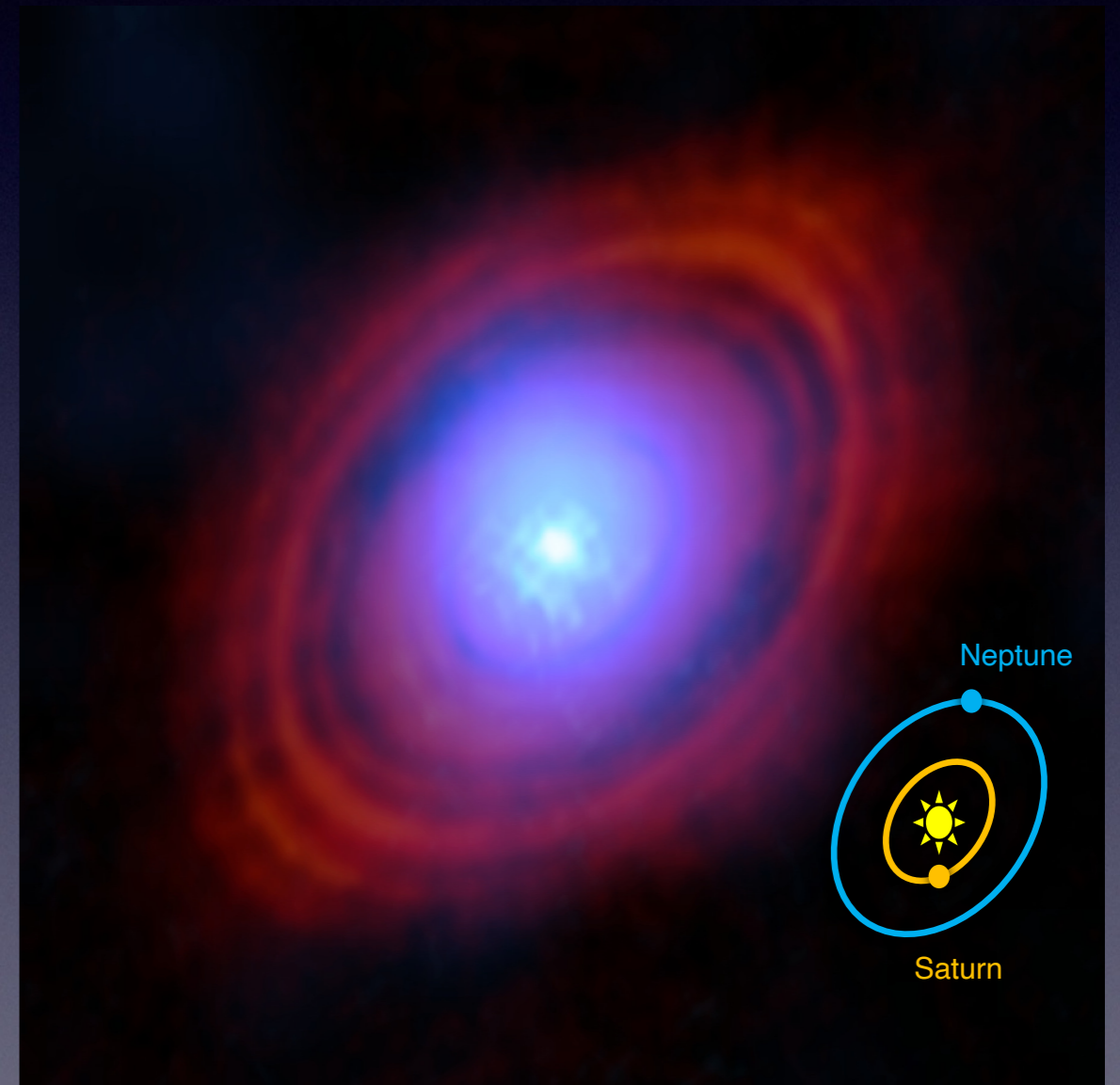
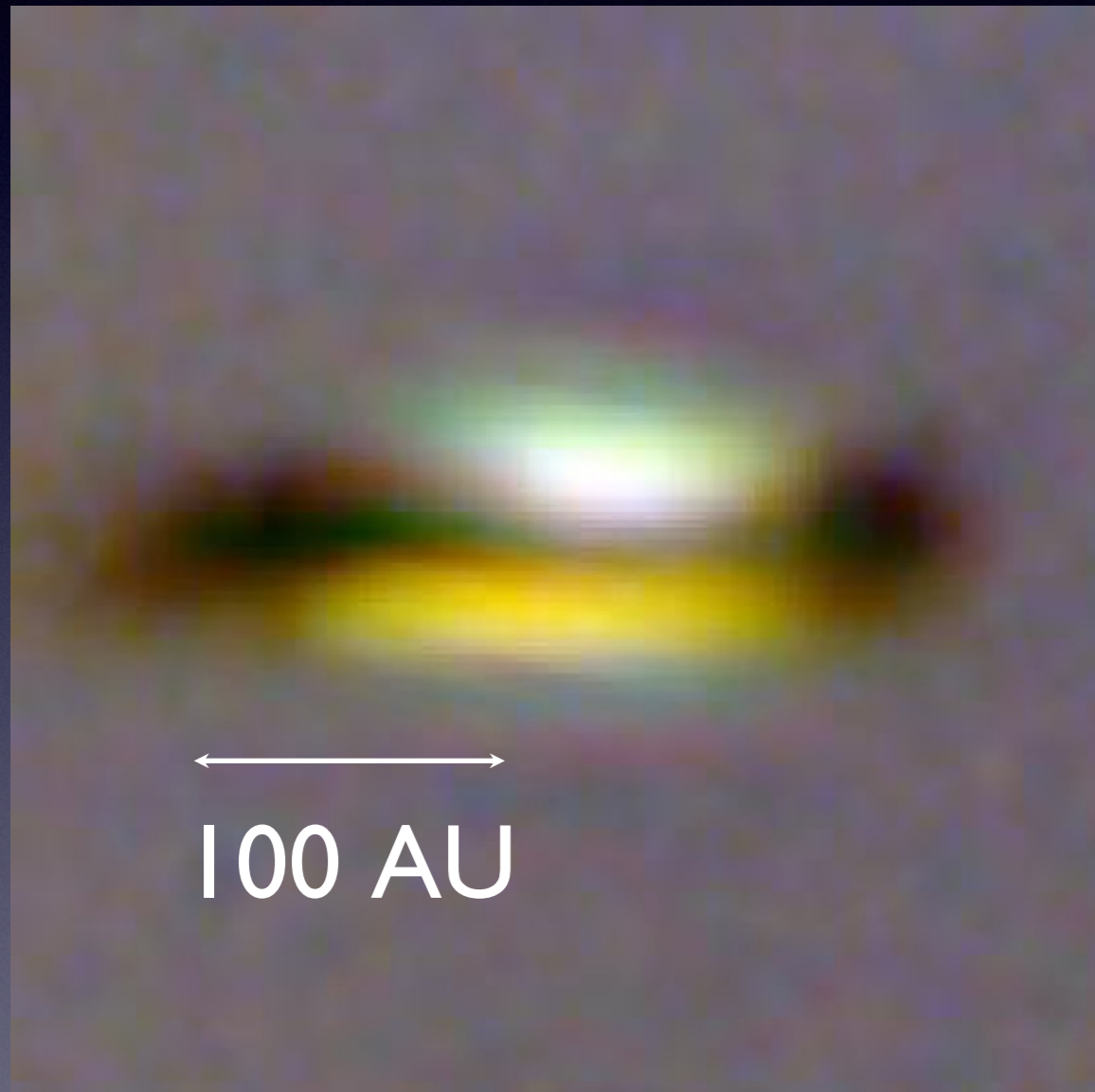


YSO SED classification



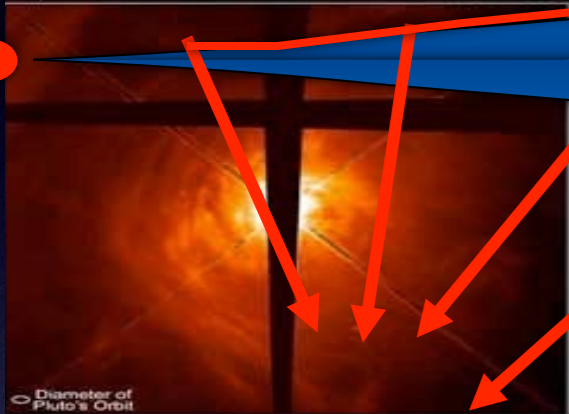
- Original classification I-II-III based on IR spectral index
- Class 0 based on FIR-submm
- Many caveats, but still a useful classification scheme

Protoplanetary disks



Flared disks: which observations probe what?

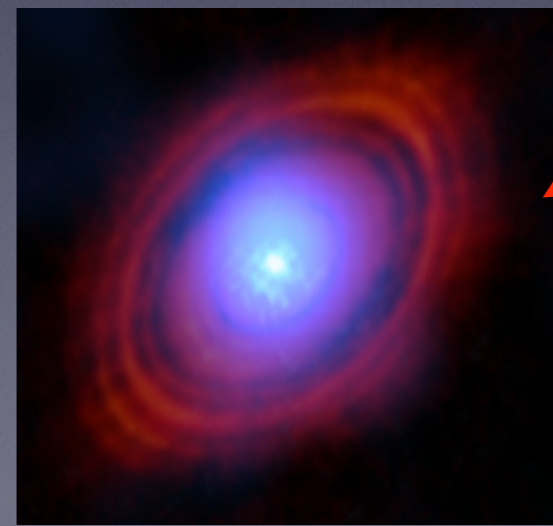
Scattered light



Mid-IR imaging

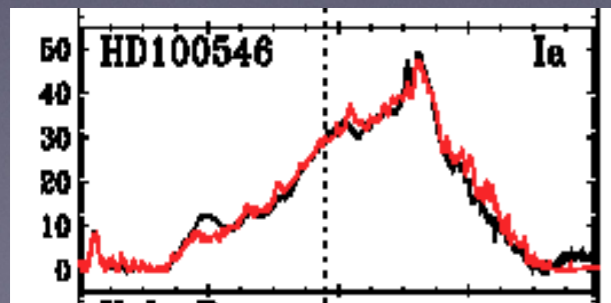


Submm/radio:
Entire Disk



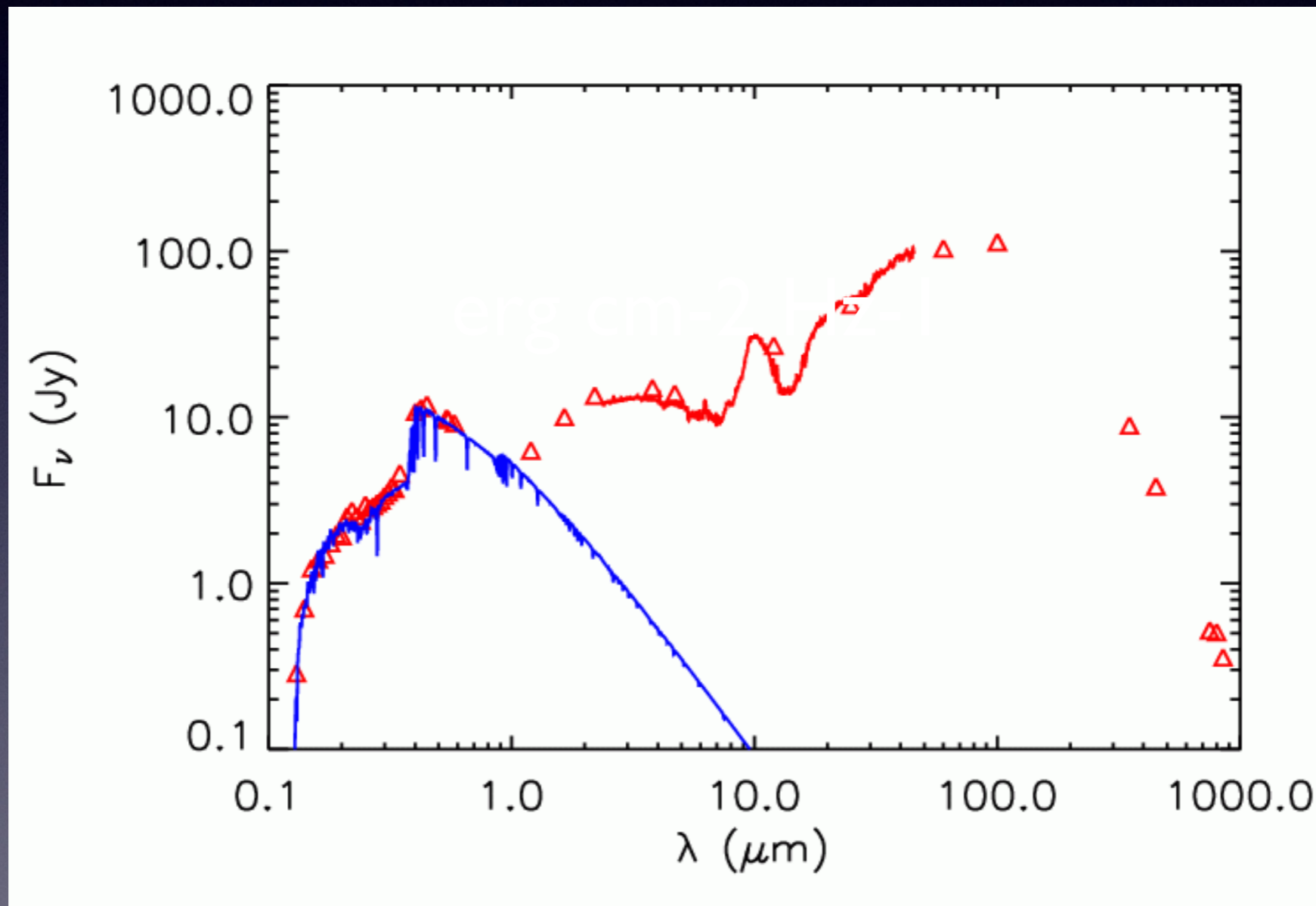
IR Spectroscopy

PAH Emission



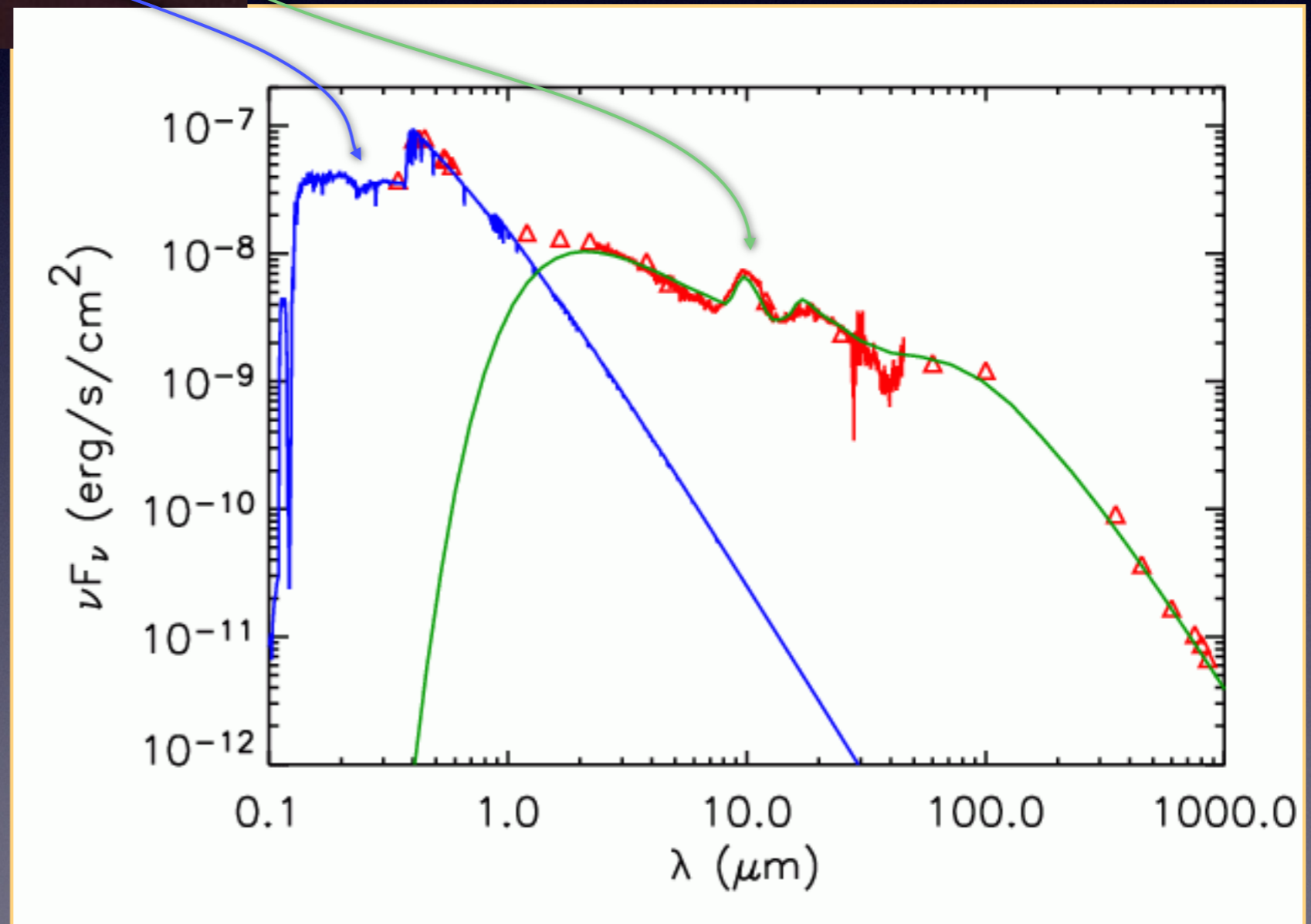
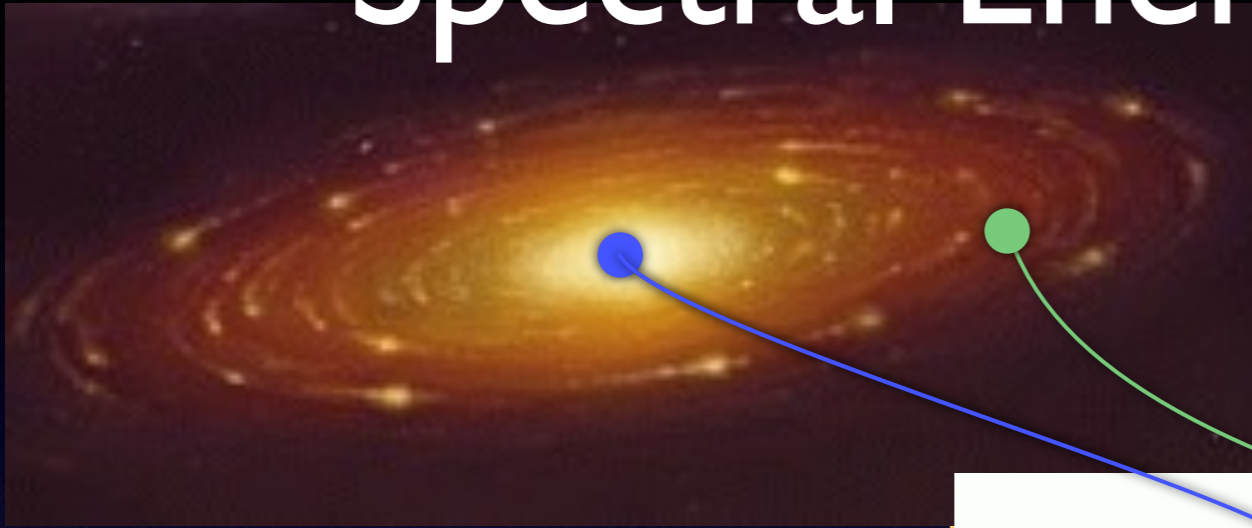
Spectral Energy Distributions (SEDs)

The SED shows the energy emitted per logarithmic wavelength interval. Plotting just the flux may be misleading:

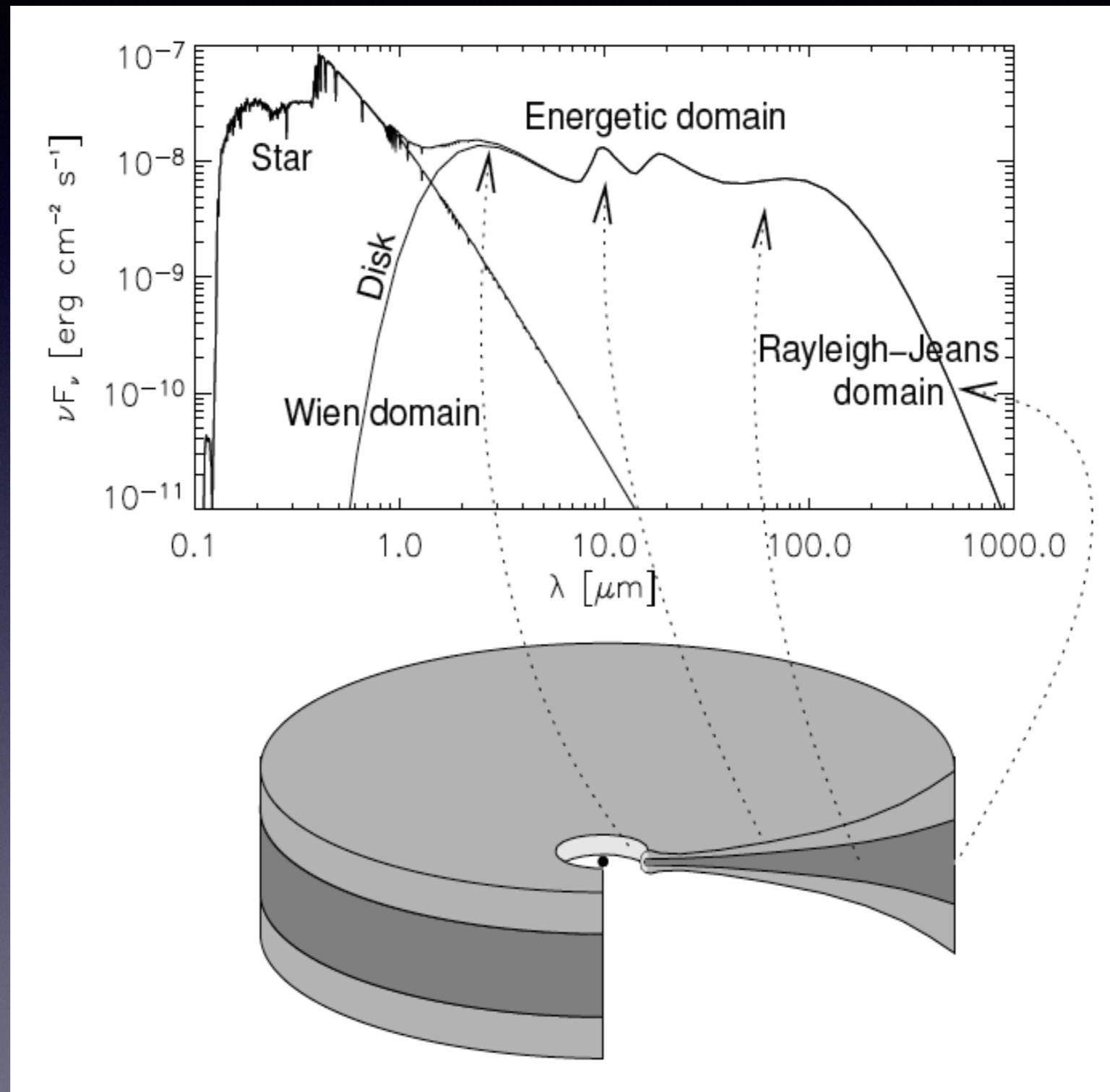


$$\text{Energy: } F_\nu d\nu = F_\nu \Delta\nu$$

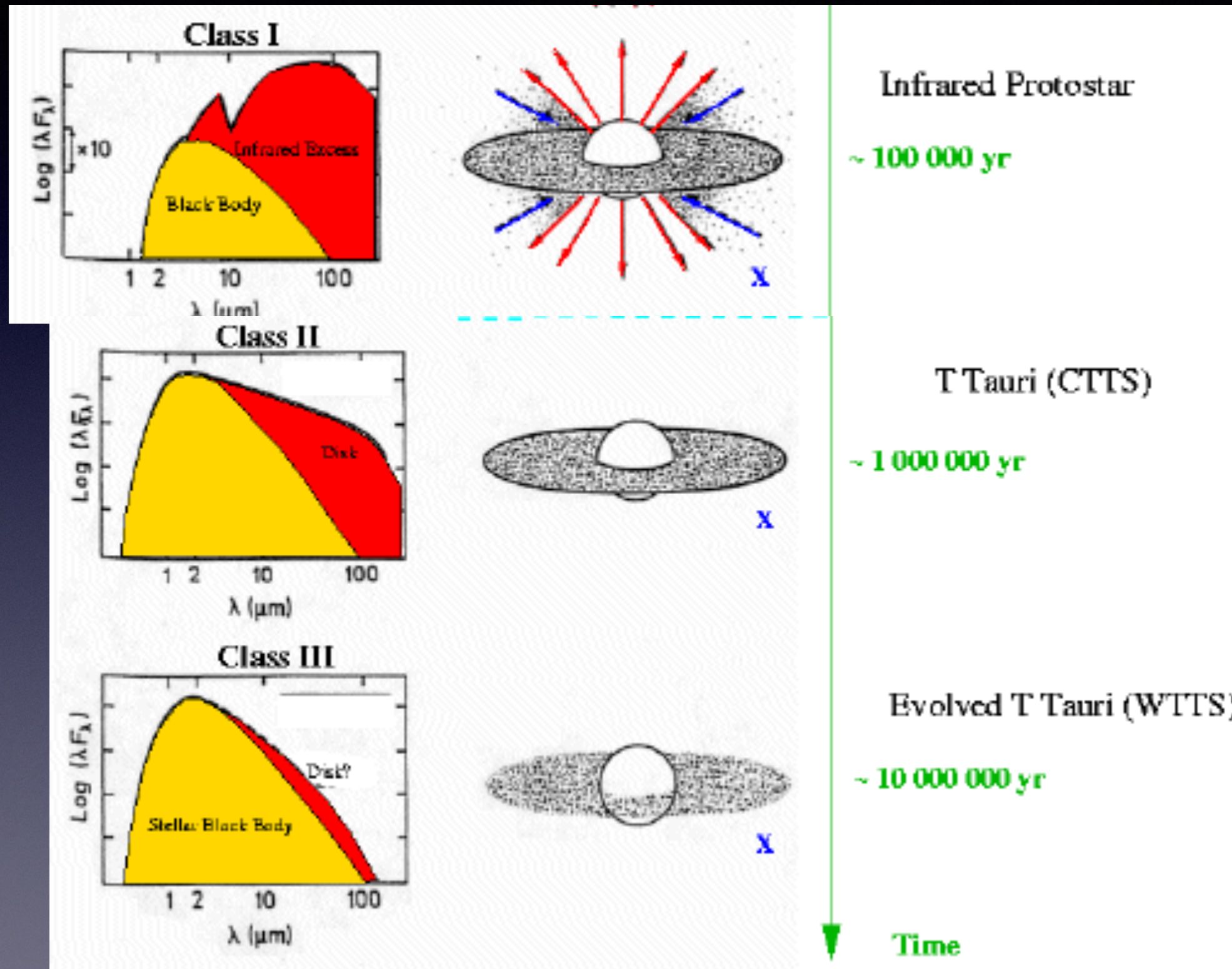
Spectral Energy Distribution



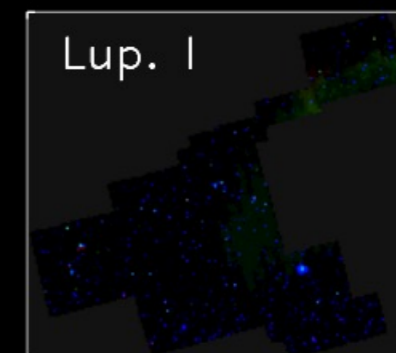
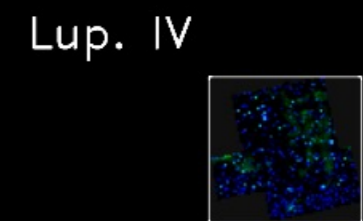
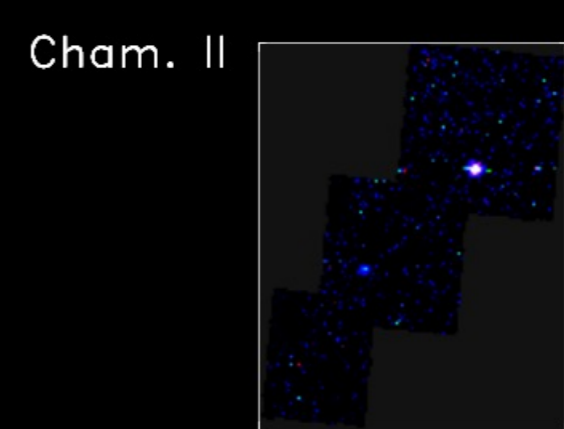
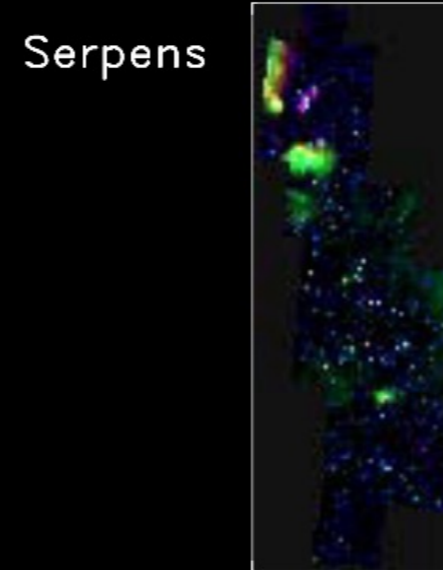
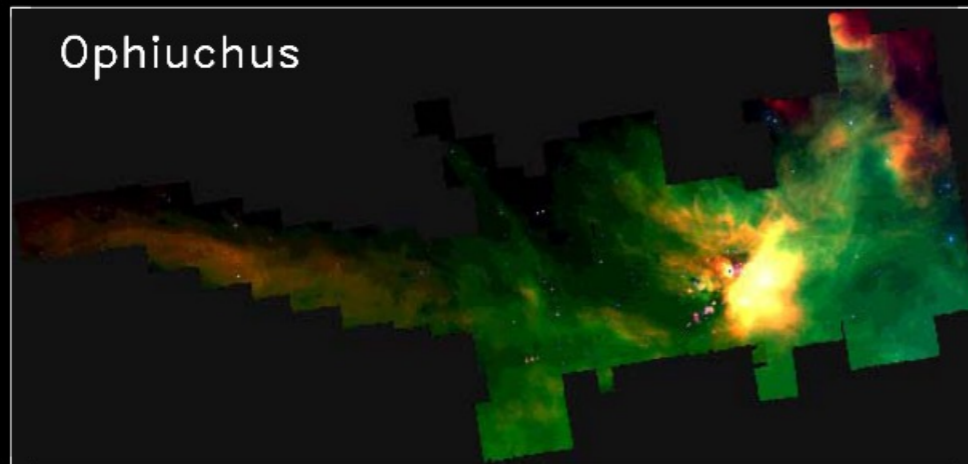
“flared” disk emission



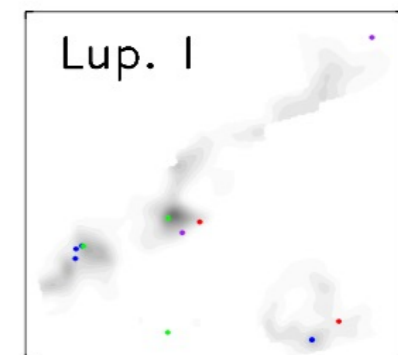
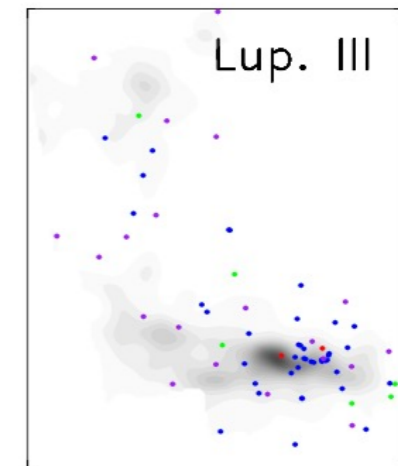
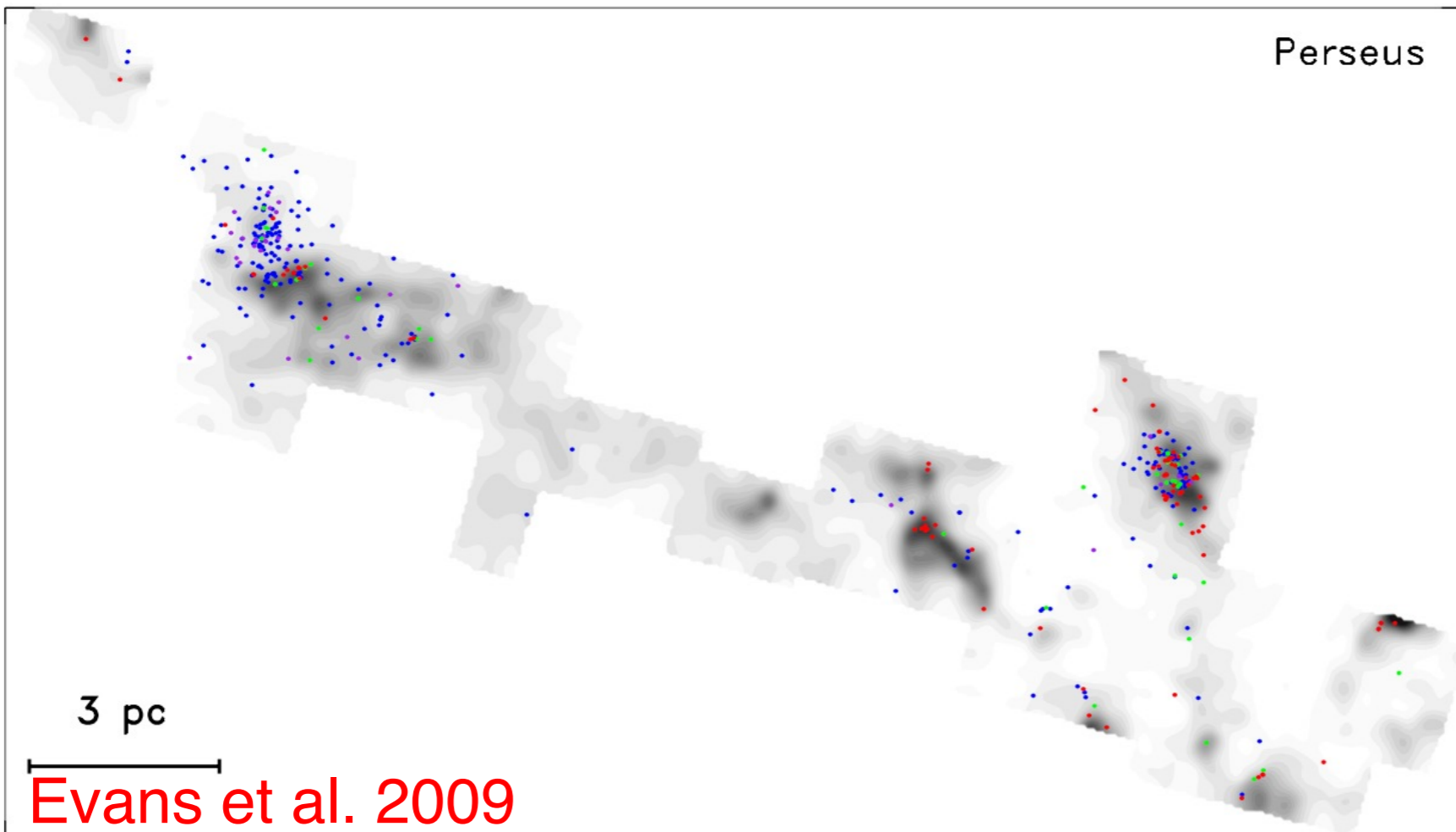
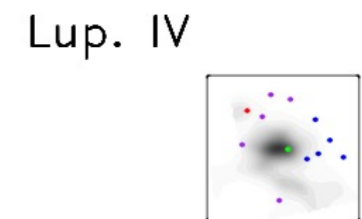
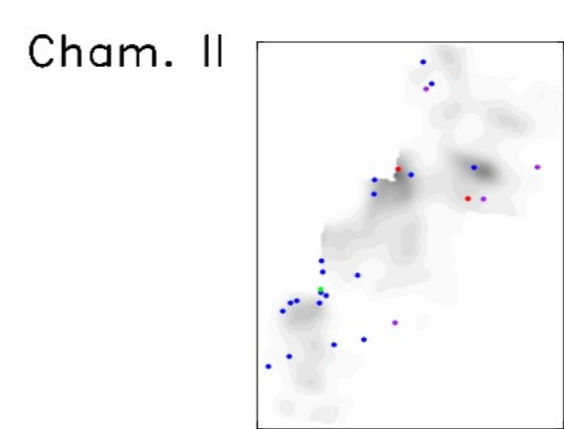
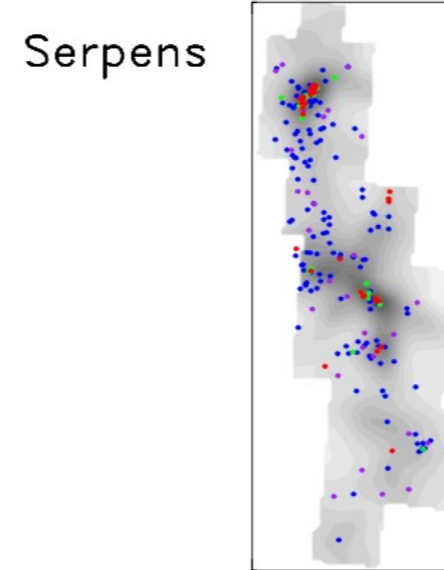
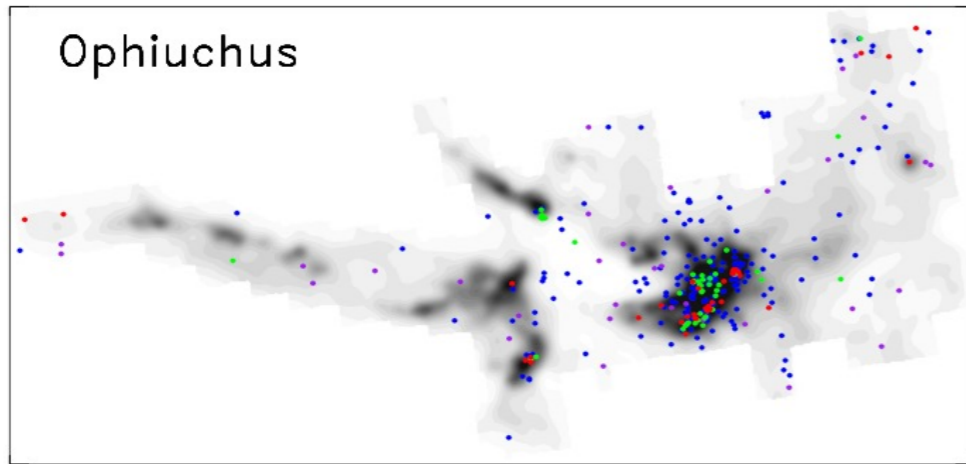
IR SED slope



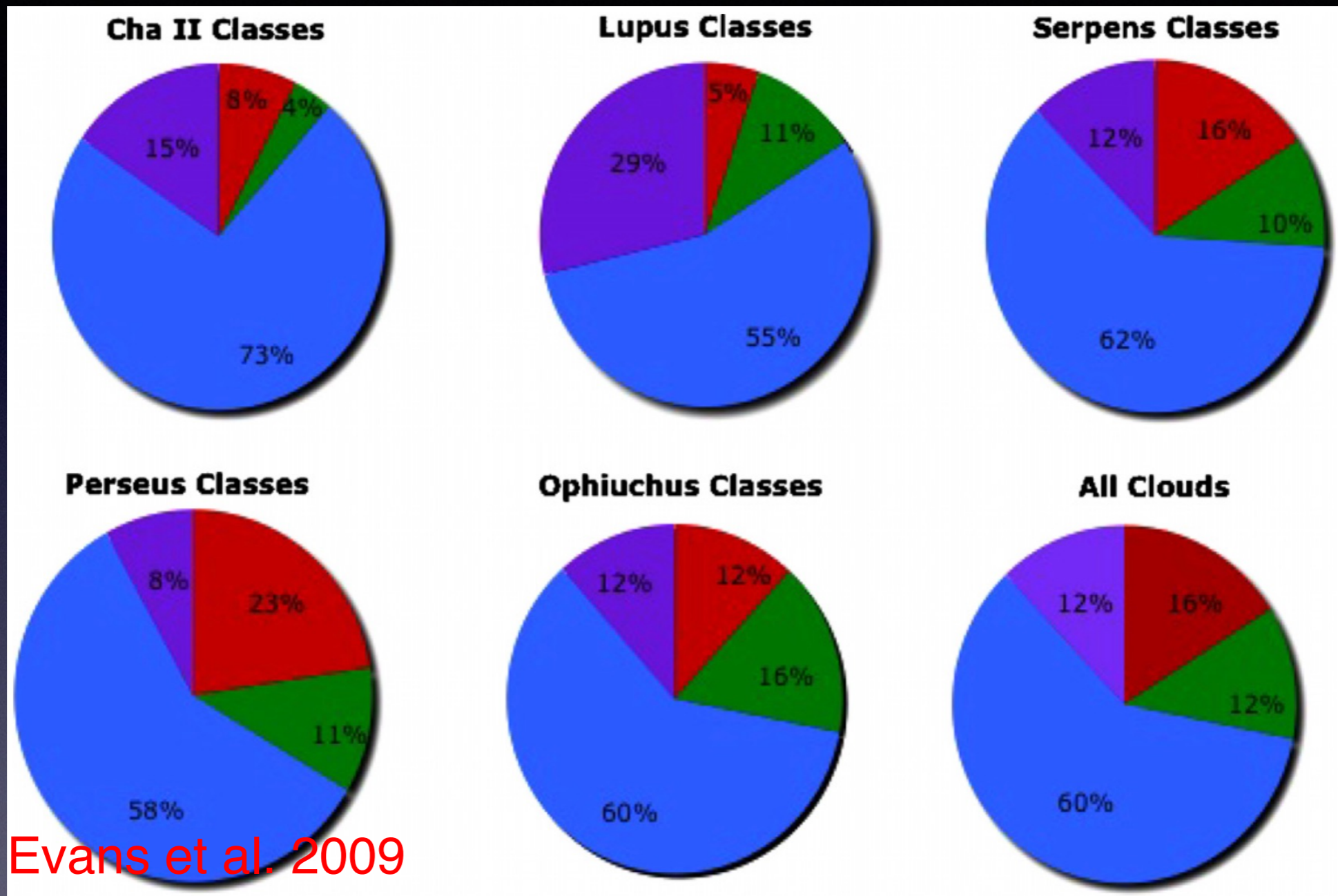
Statistics and timescales



Statistics and timescales

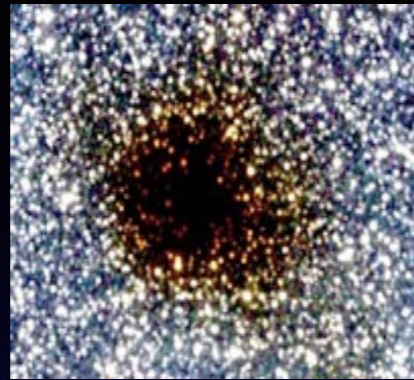
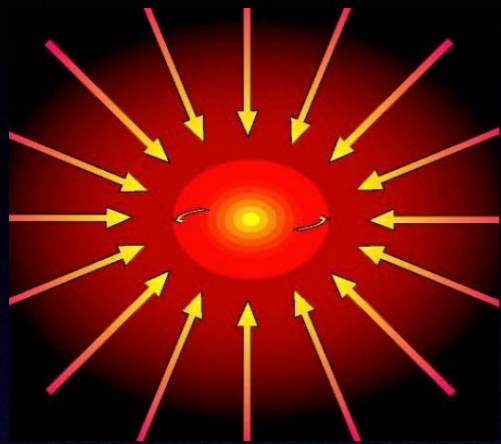


Statistics and timescales

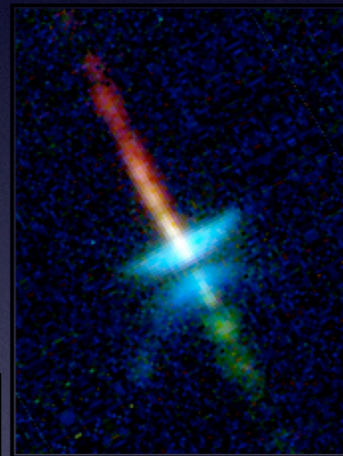
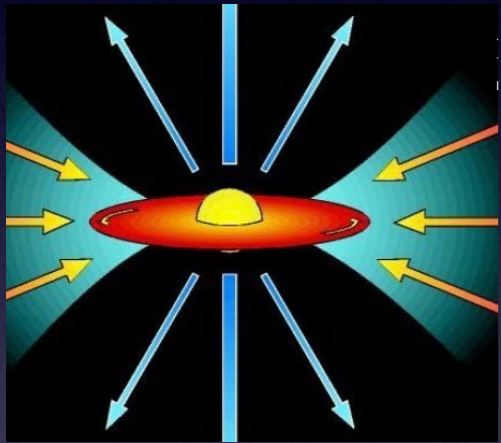


- In nearby star forming regions, we can estimate:
- very roughly $t_{II} \sim 5-10 t_I \sim 5-10 t_0$ or $\sim 10^6 \text{ yr} : \sim 10^5 \text{ yr} : \sim 10^4 \text{ yr}$

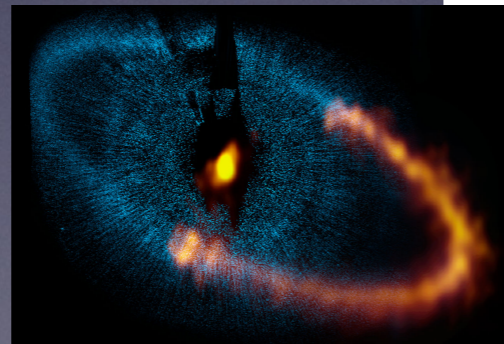
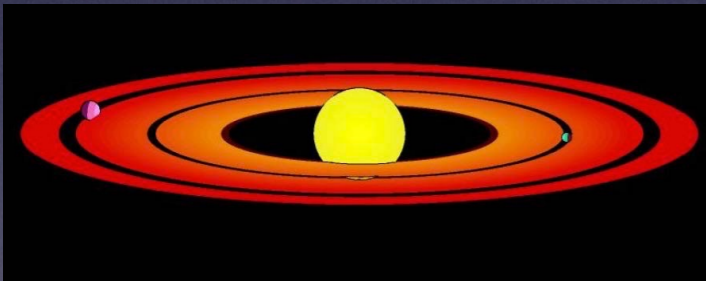
From Cores to Planetary Systems



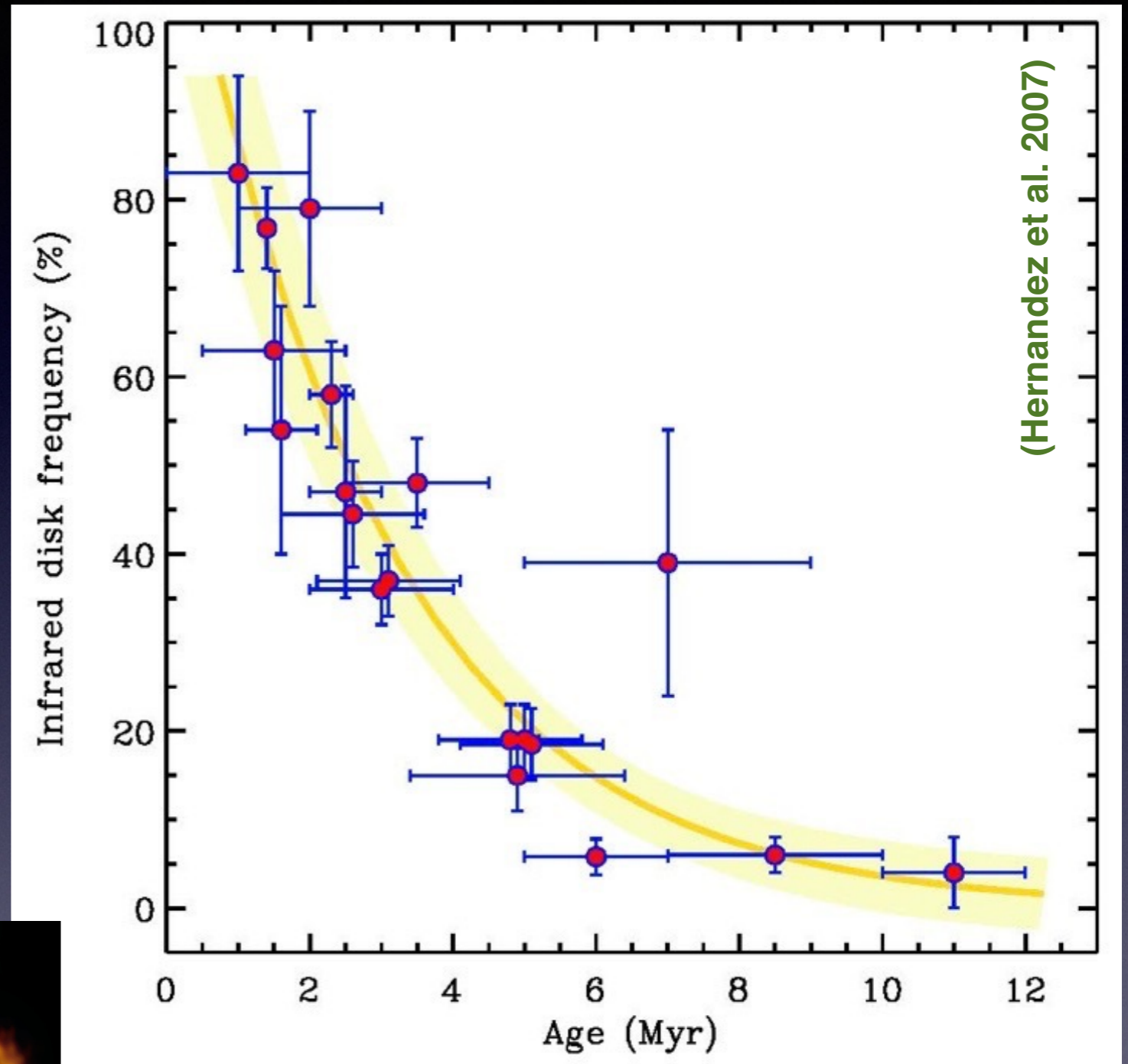
Core



Disk



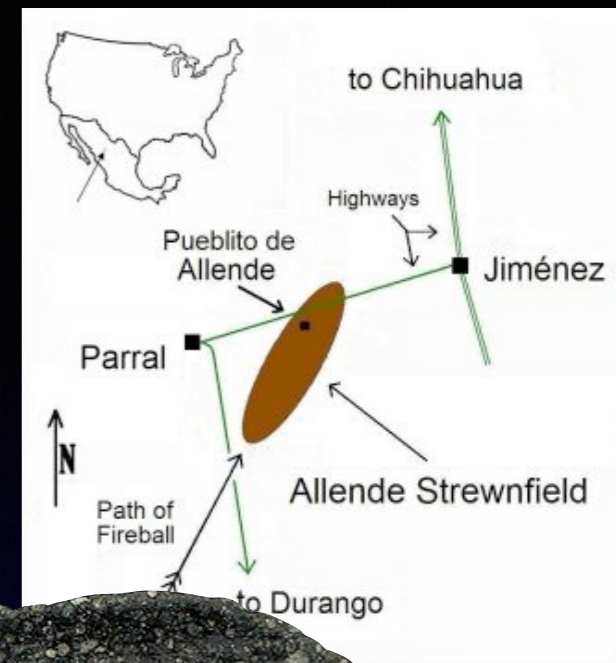
Debris Disk



(Hernandez et al. 2007)

Inner disk clearing:
e-folding time $t \sim 2-3$ Myr

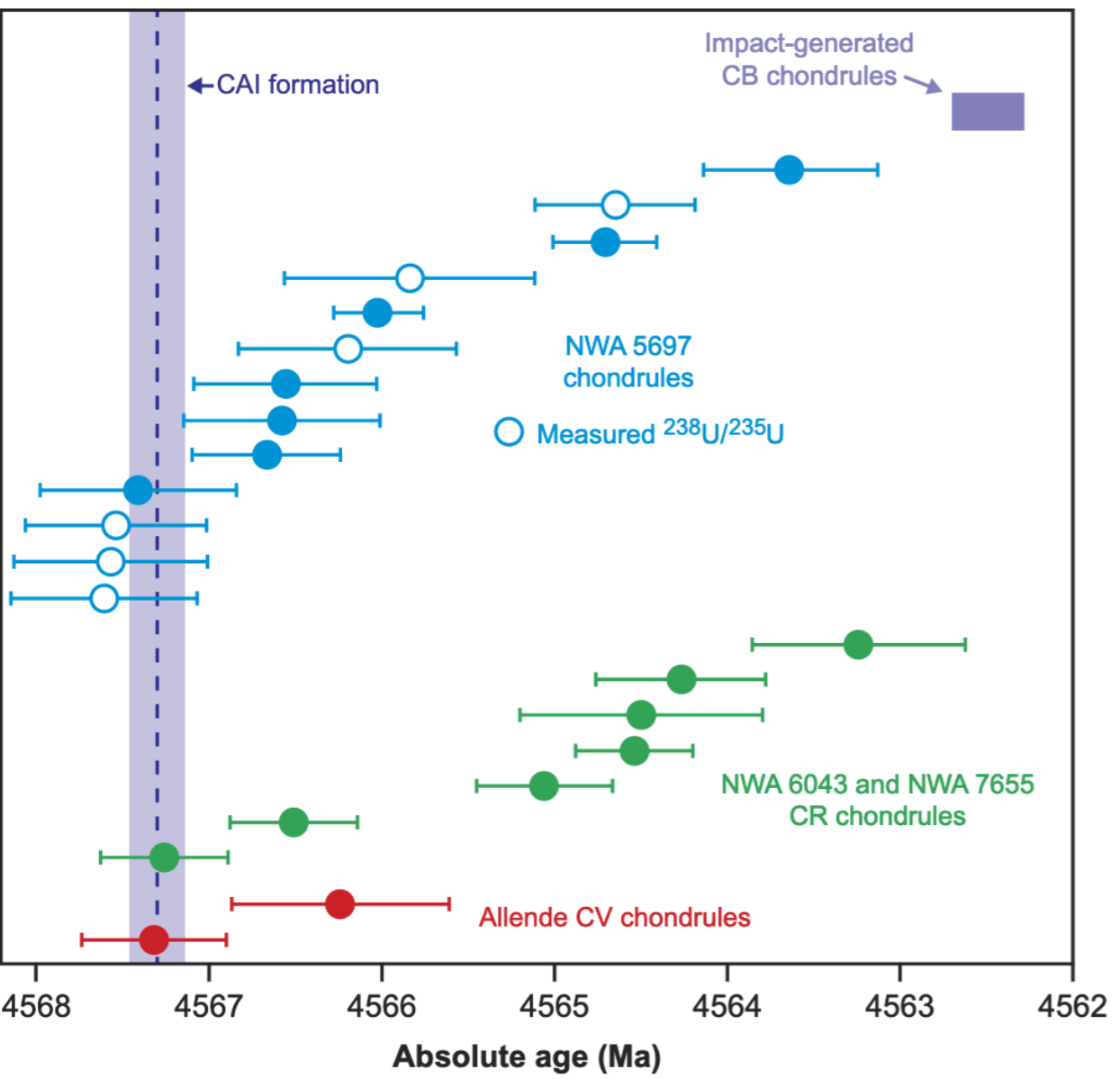
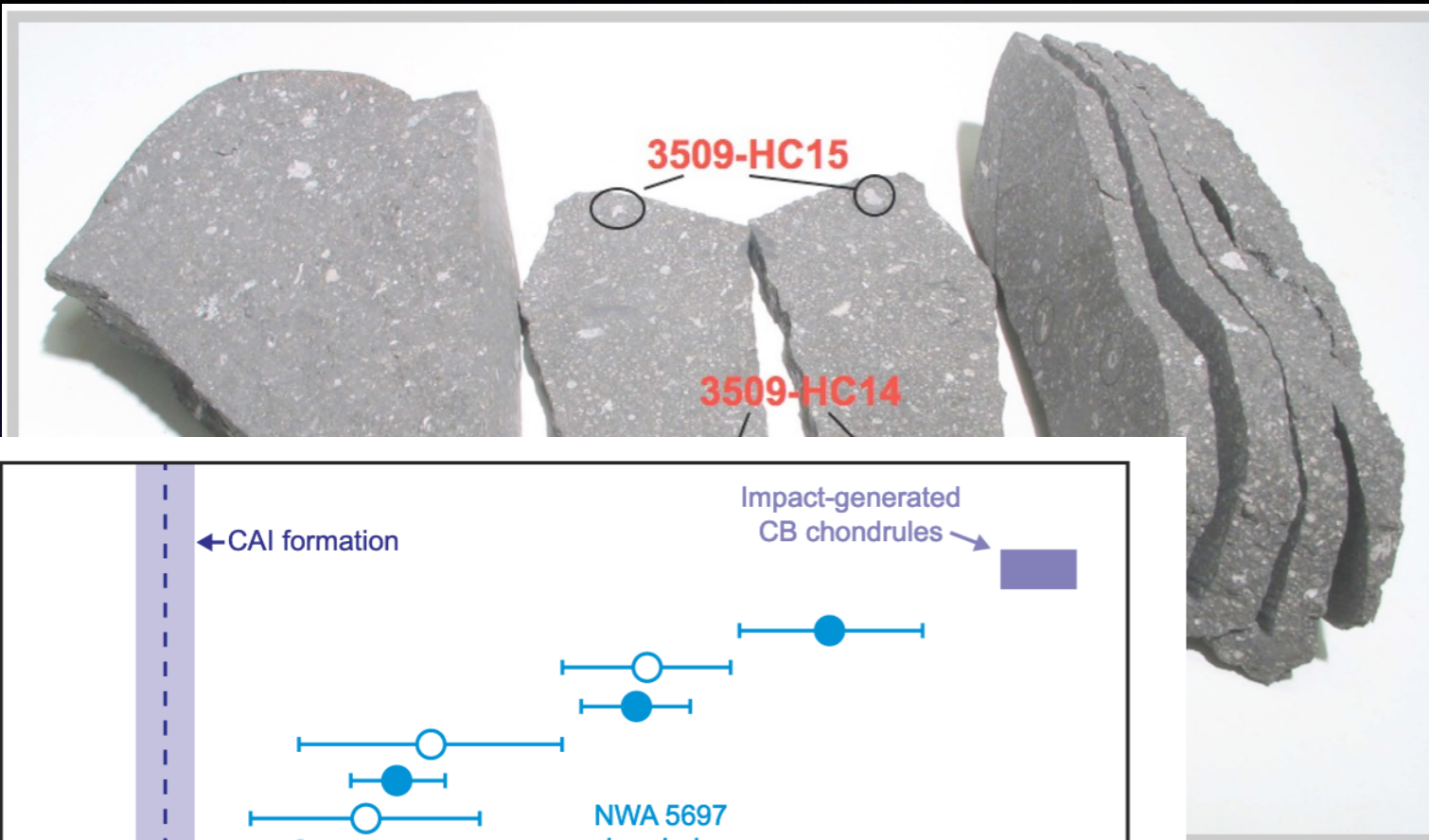
Allende meteorite



Mexico
8 Feb 1969



N



Calcium-Aluminum Inclusions (CAI)

Oldest, high-T ($> \sim 1700\text{K}$) processing, short formation phase ($< \sim 3 \times 10^5$ yr)

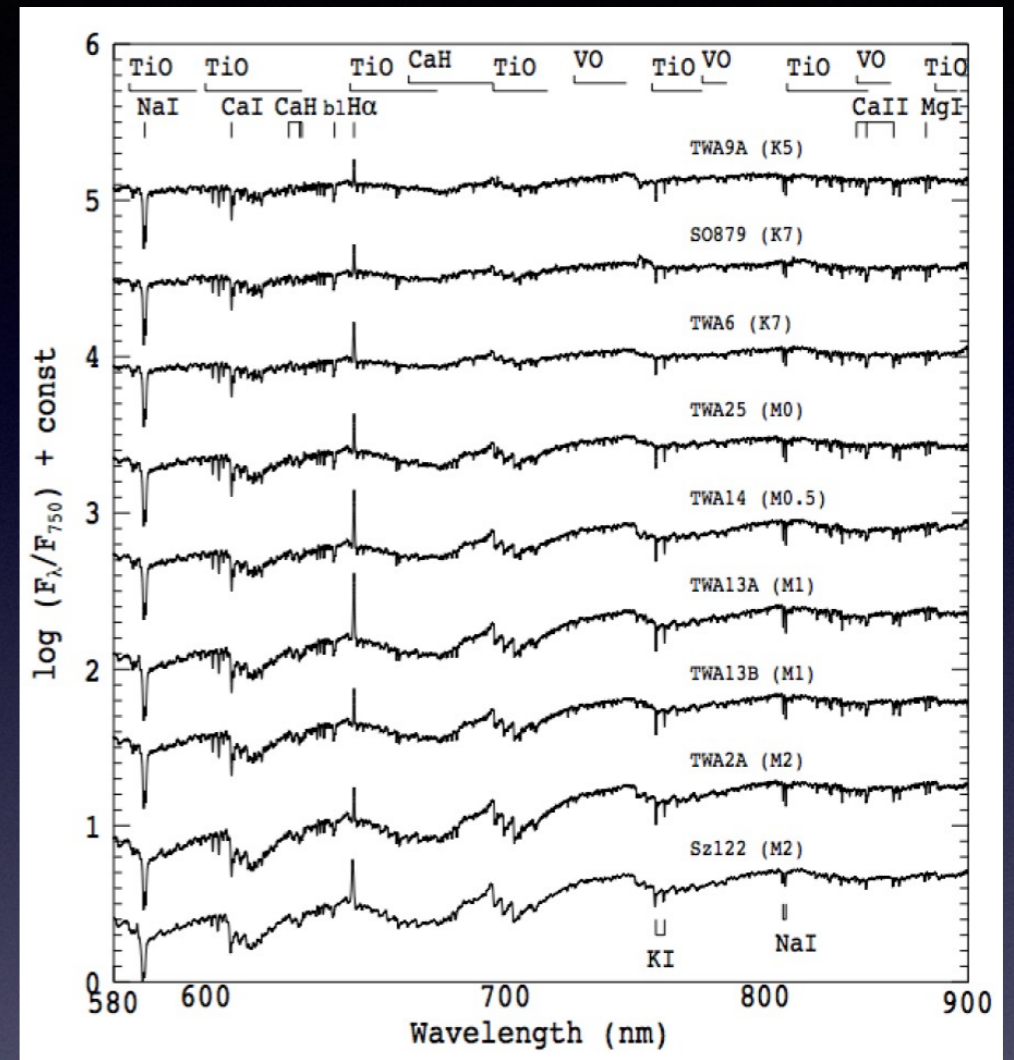
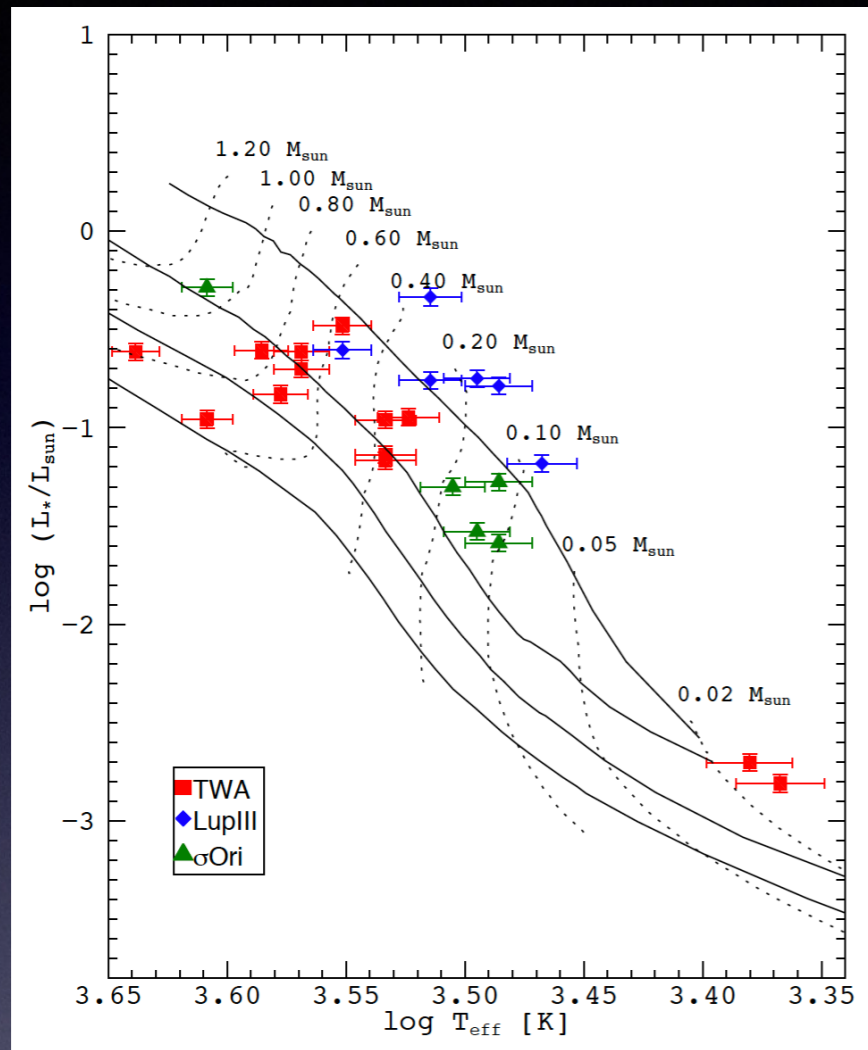
Chondrules

Formed after CAI, high-T ($\sim 2000\text{K}$) few Myr age dispersion

Matrix

sub-um particles, glue together the material

Stellar parameters

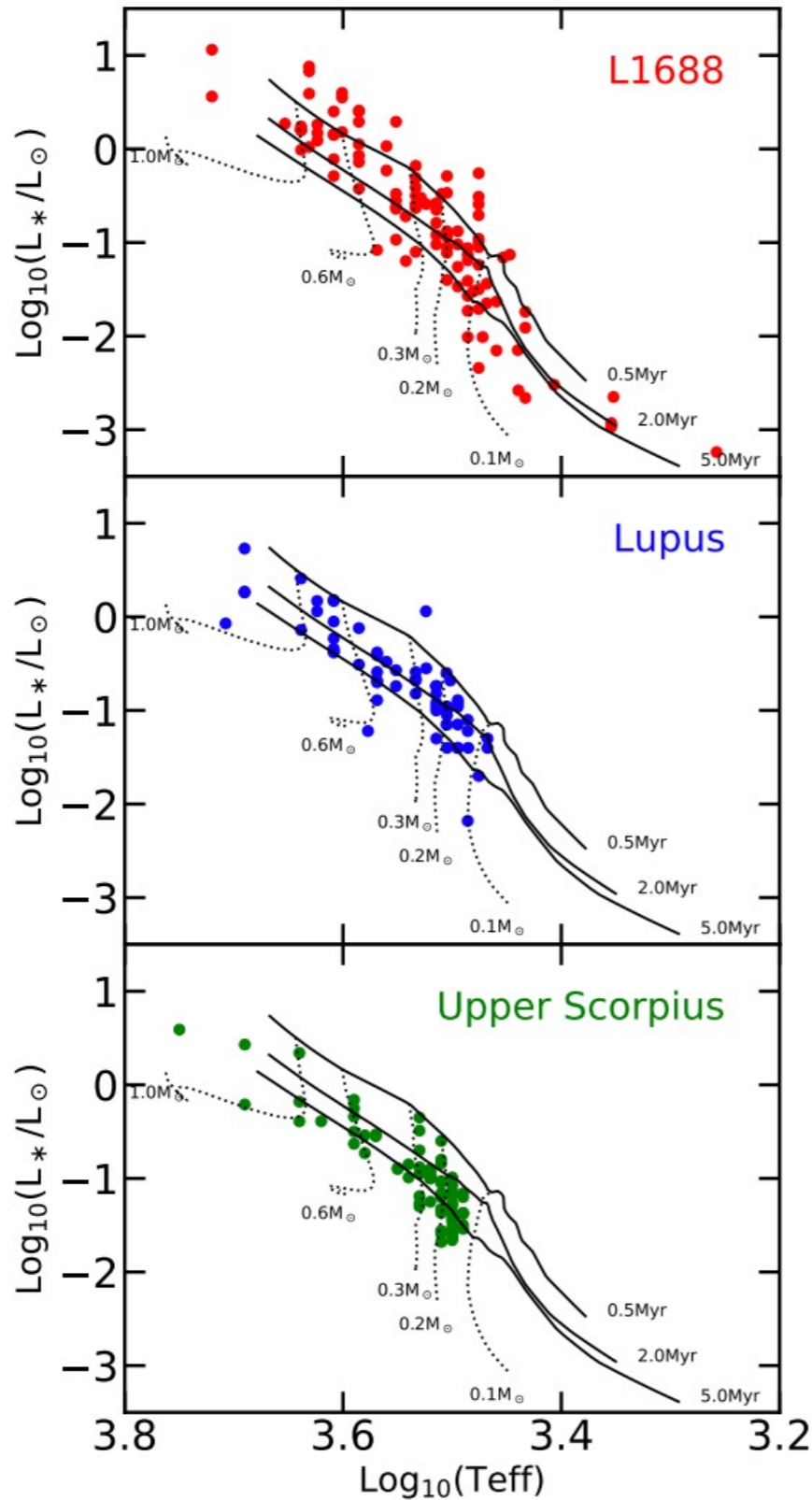


(Manara et al. 2013)

- Place star on HR-diagram using T_{eff} and L_{star} to read off masses and ages (hoping that the tracks are accurate...)
- T_{eff} from spectral typing
- L_{star} from magnitudes and extinction

Stellar parameters

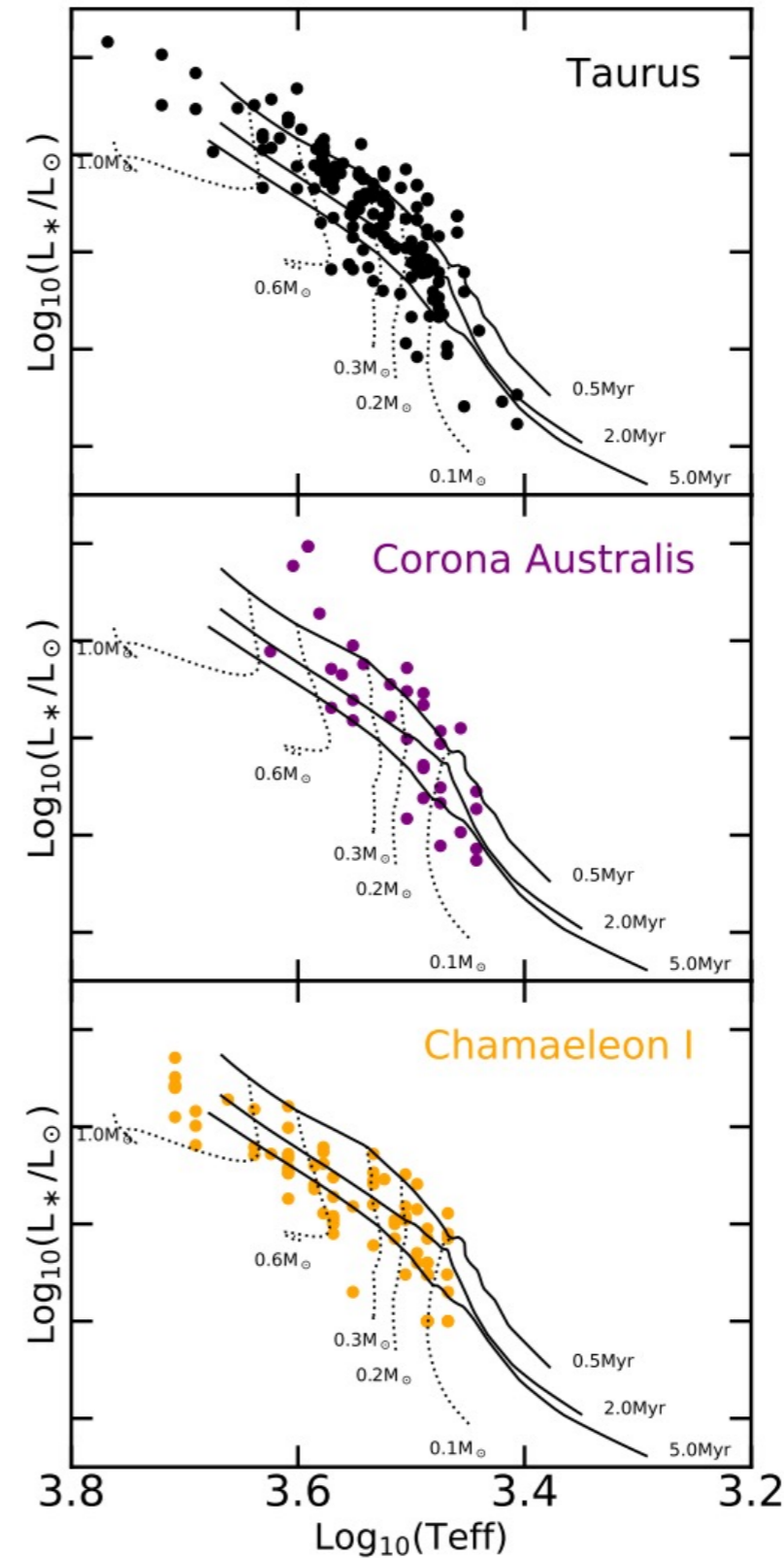
~1Myr



~2Myr

~5Myr

~0.9Myr

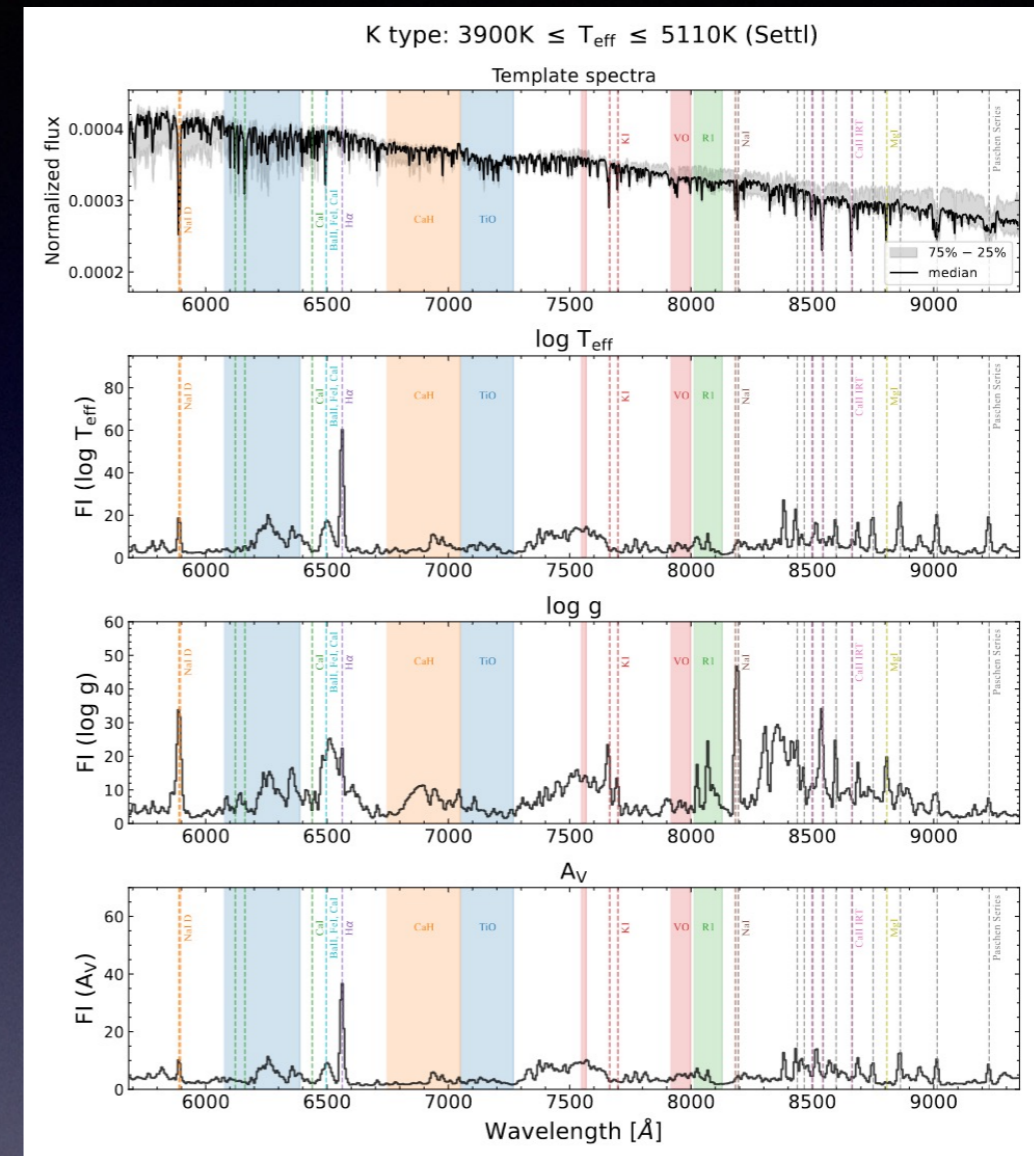
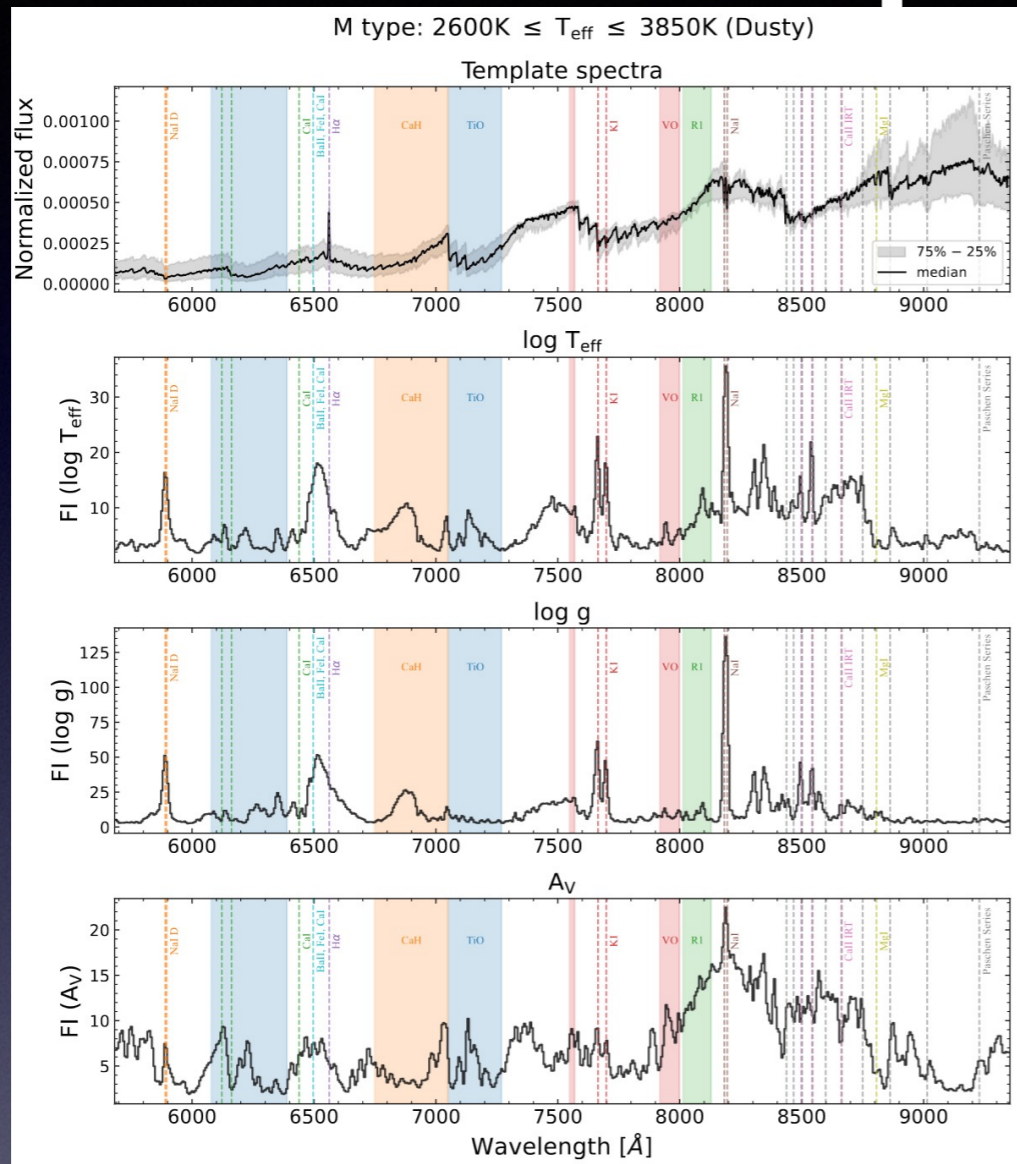


~0.6Myr

~3Myr

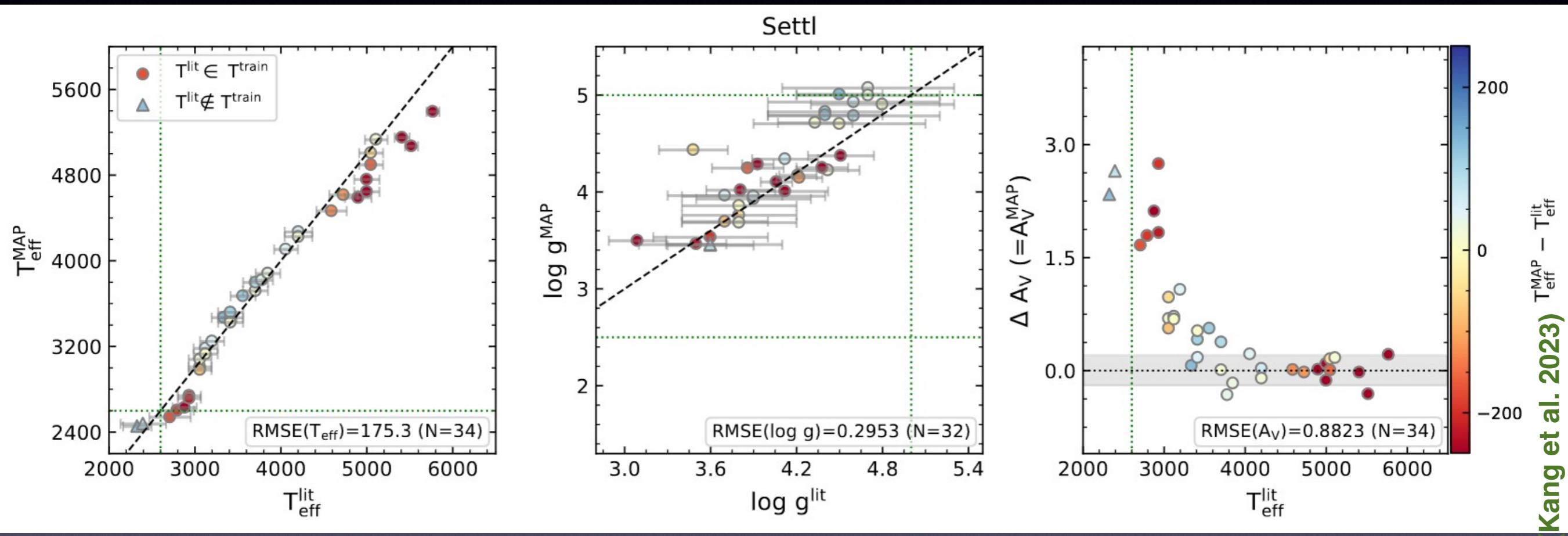
(Testi et al. 2022)

Stellar parameters



- Place star on HR-diagram using T_{eff} and L_{star} to read off masses and ages (hoping that the tracks are accurate...)
- T_{eff} from spectral typing – problems: S/N, extinction and veiling
- L_{star} from magnitudes and extinction – problems: extinction and excess/veiling/variability

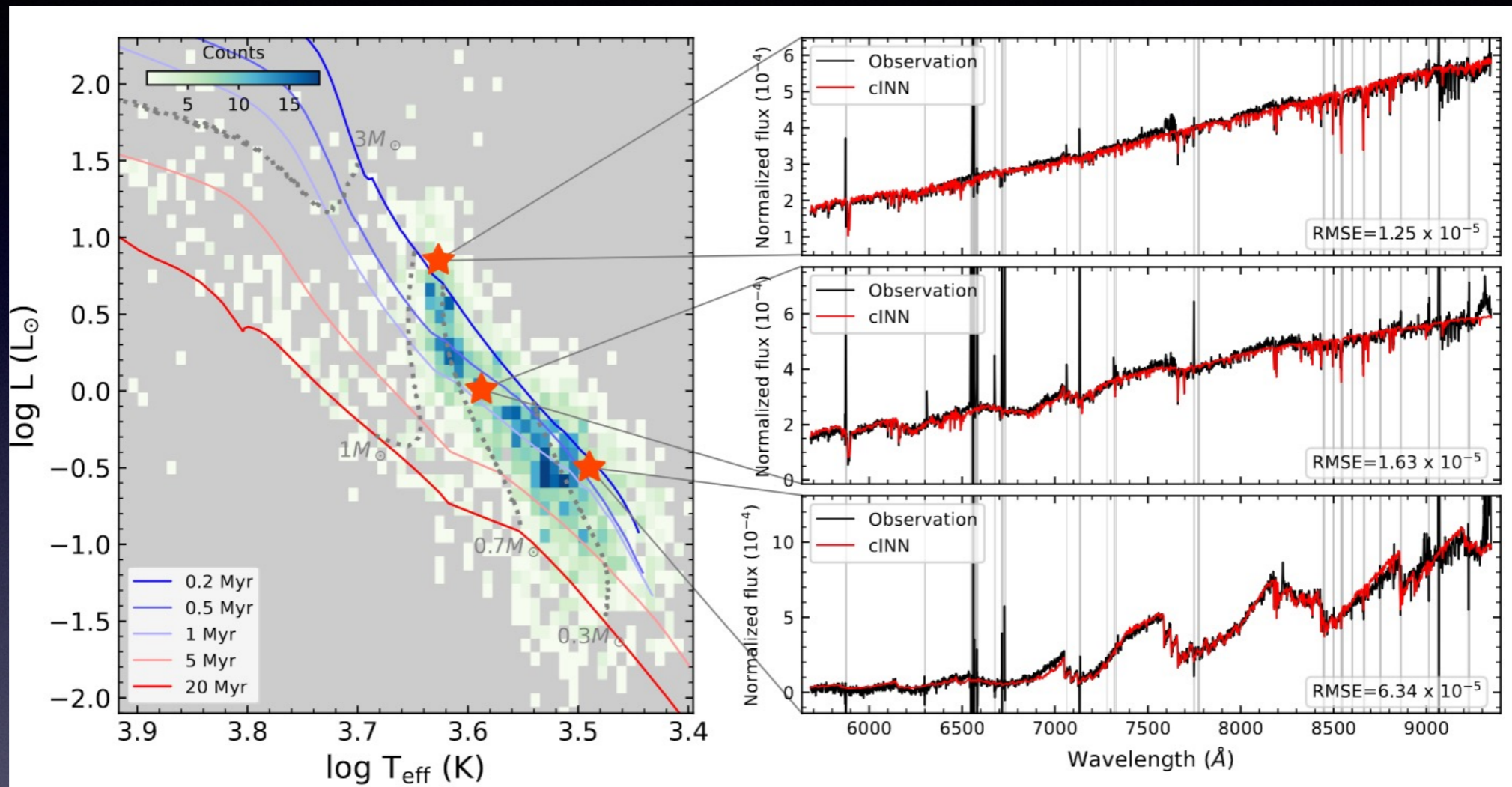
Stellar parameters



(Kang et al. 2023)

- Place star on HR-diagram using T_{eff} and L_{star} to read off masses and ages (hoping that the tracks are accurate...)
 - T_{eff} from spectral typing – problems: S/N, extinction and veiling
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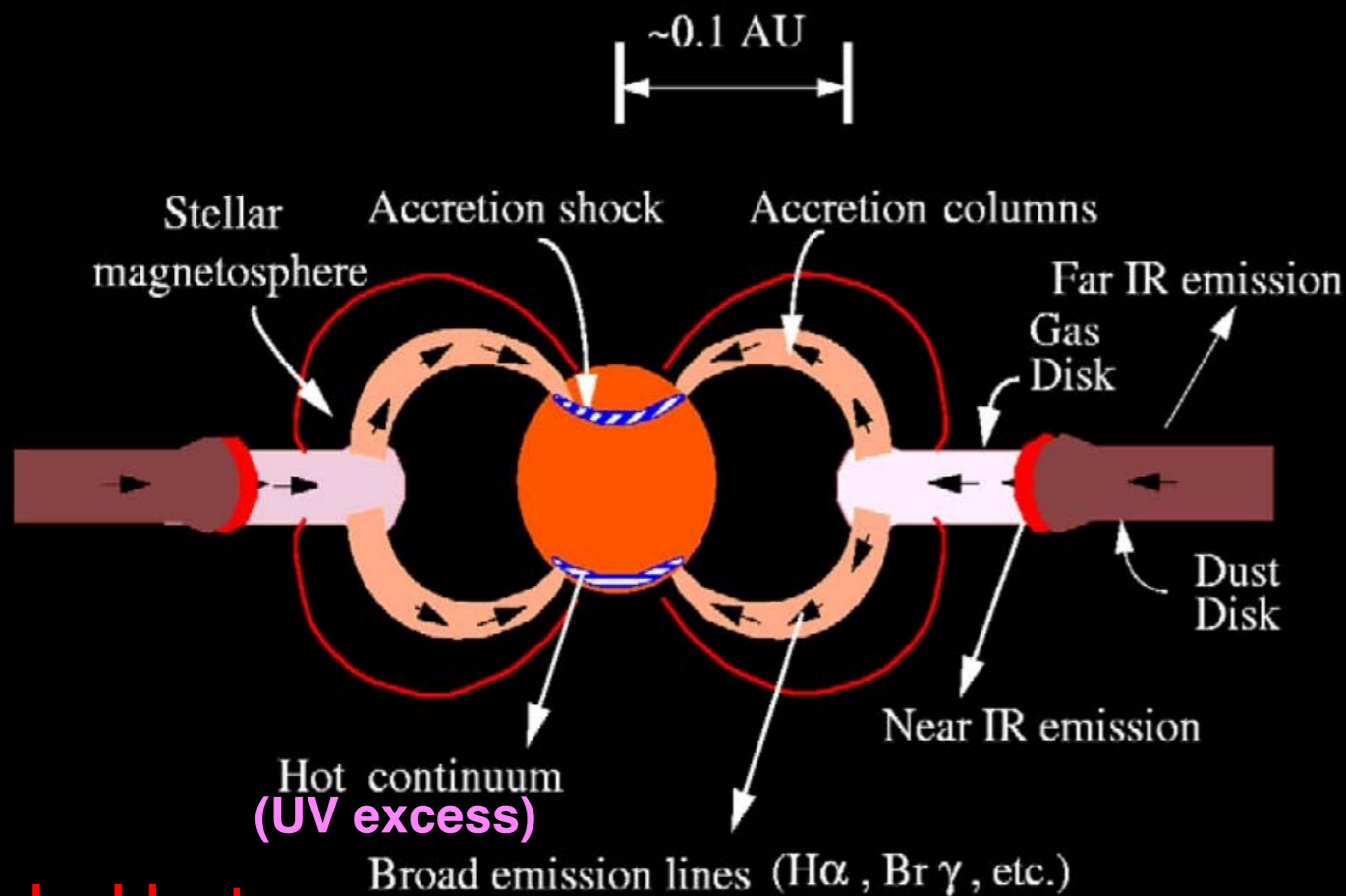
Stellar parameters



- Place star on HR-diagram using T_{eff} and L_{star} to read off masses and ages (hoping that the tracks are accurate...)
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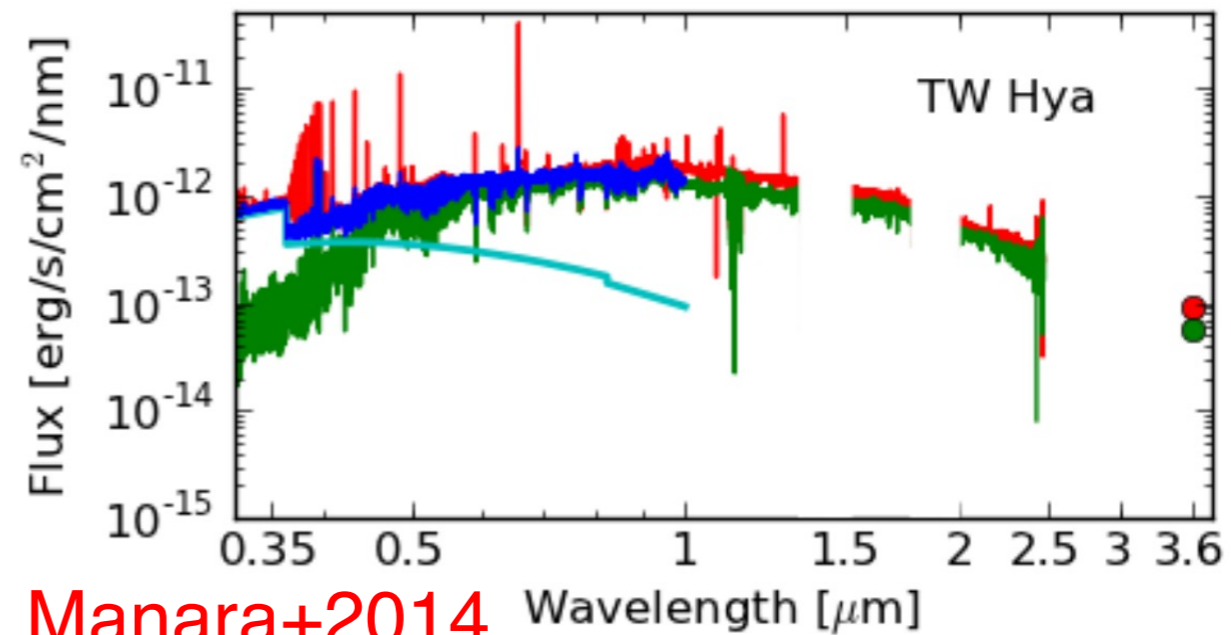
Accretion

T Tauri star - magnetospheric accretion

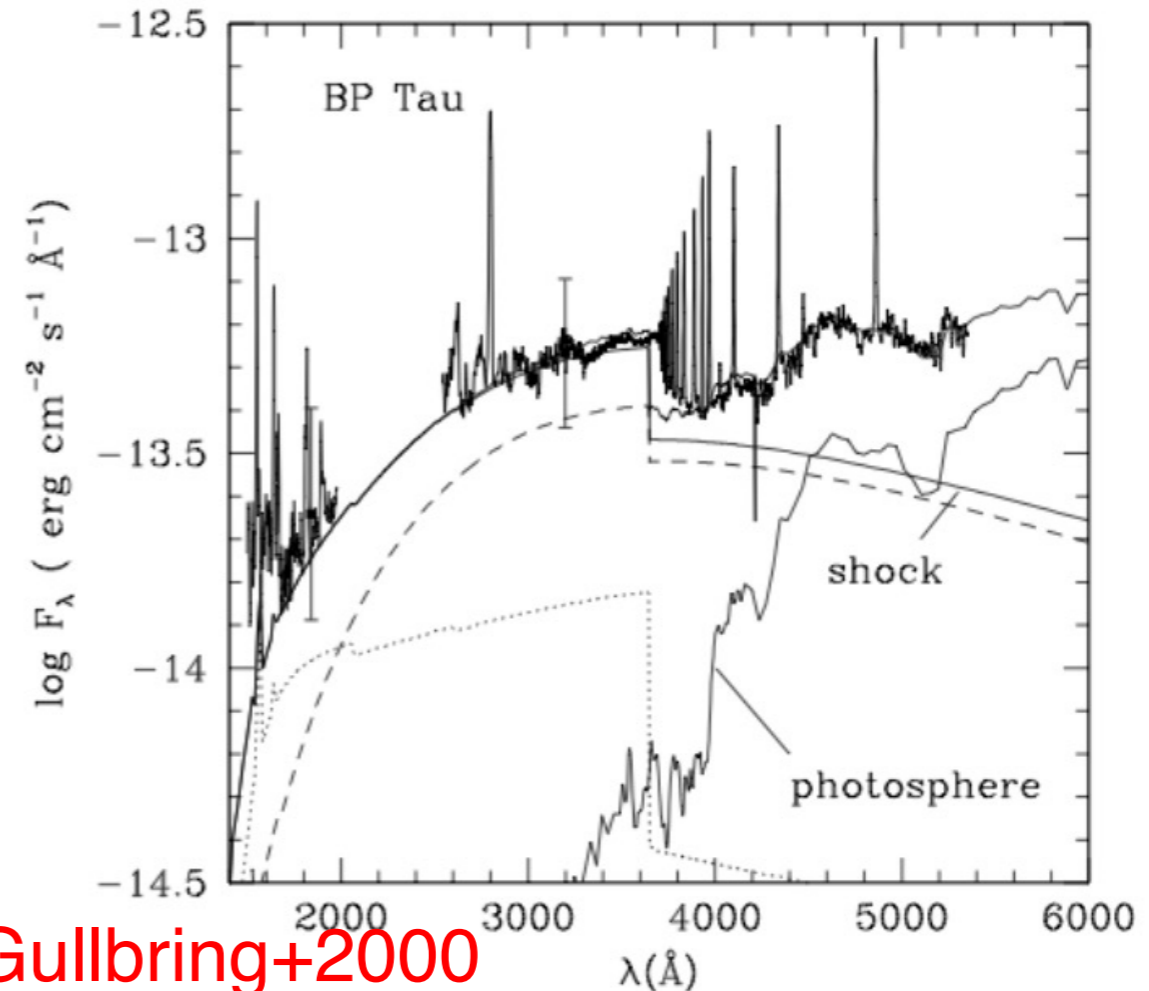


L. Hartmann

- Direct measurement of accretion: energy released in the collision
- Indirect measurement: emission lines from accretion columns



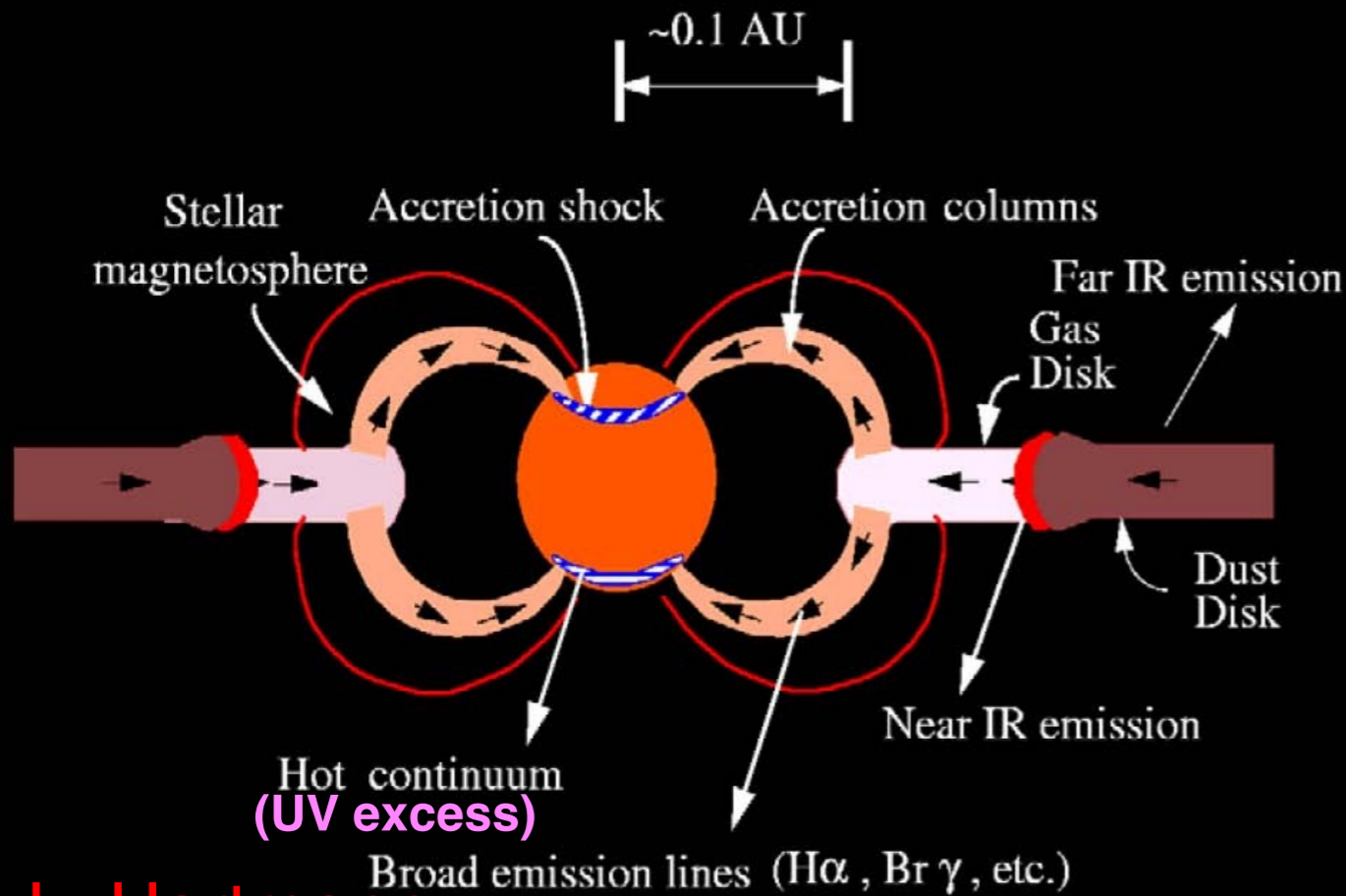
Manara+2014



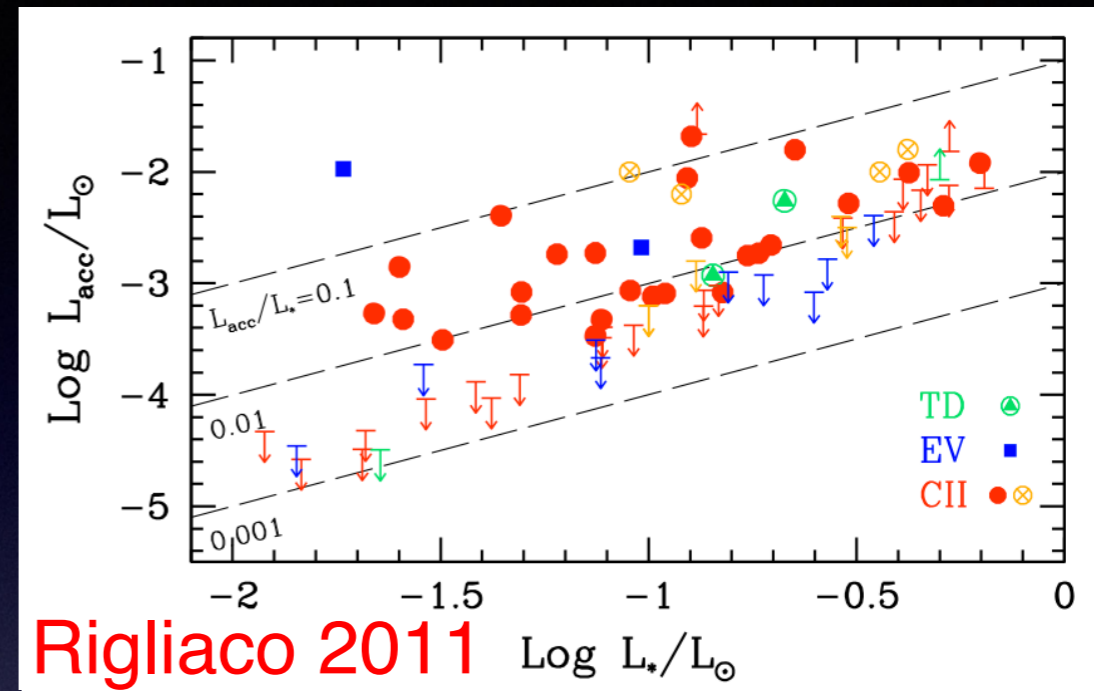
Gullbring+2000

Accretion

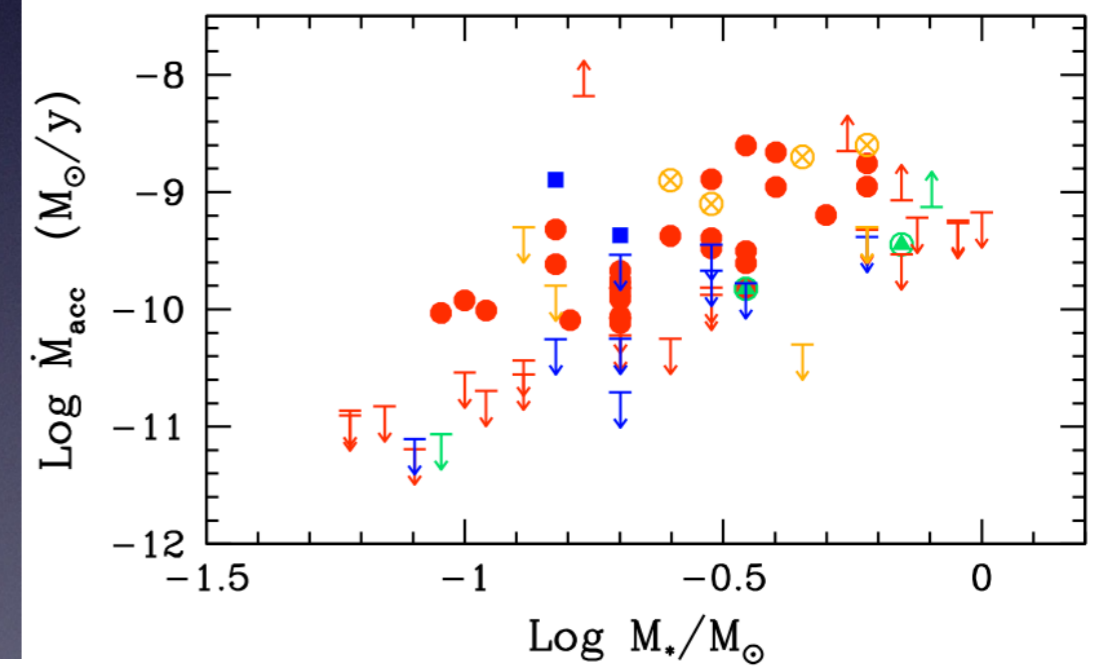
T Tauri star - magnetospheric accretion



L. Hartmann



Rigliaco 2011



Gullbring 1998

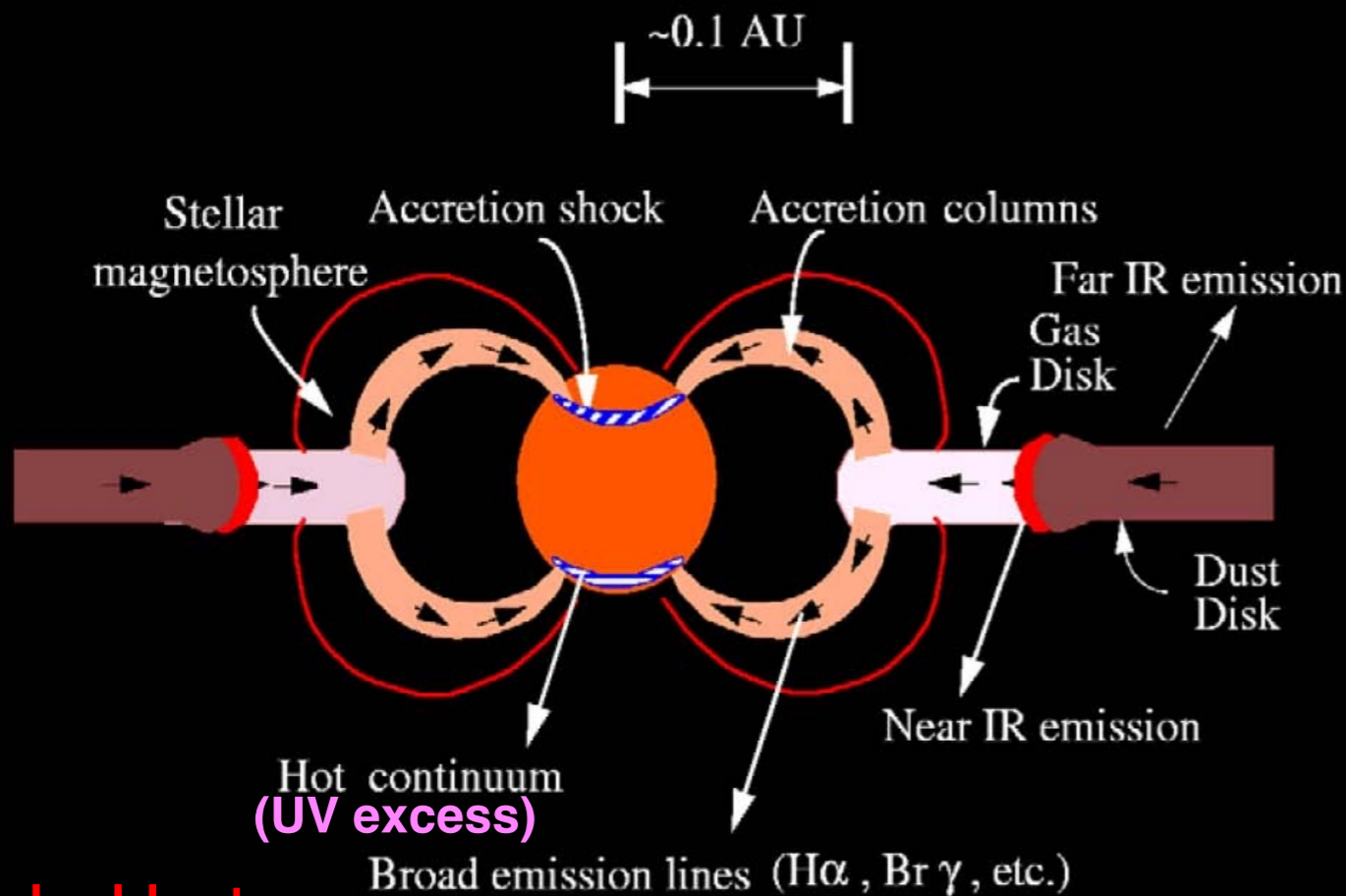
$$\dot{M}_{\text{acc}} = \left(1 - \frac{R_{\star}}{R_m}\right)^{-1} \frac{L_{\text{acc}} R_{\star}}{GM_{\star}} = \frac{L_{\text{acc}} R_{\star}}{0.8GM_{\star}}$$

$R_m \sim 5 R_{\text{star}}$

- L_{acc} measured directly from the UV excess luminosity (with a correction factor for FUV/EUV)

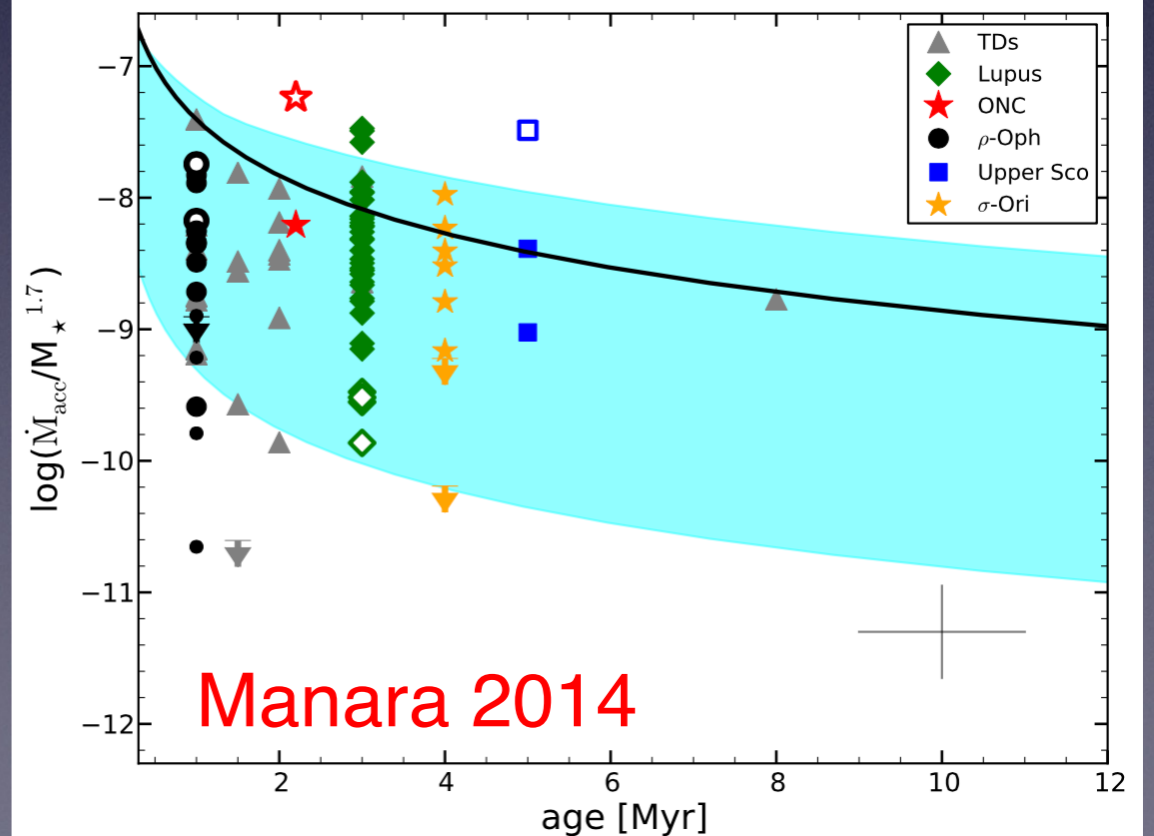
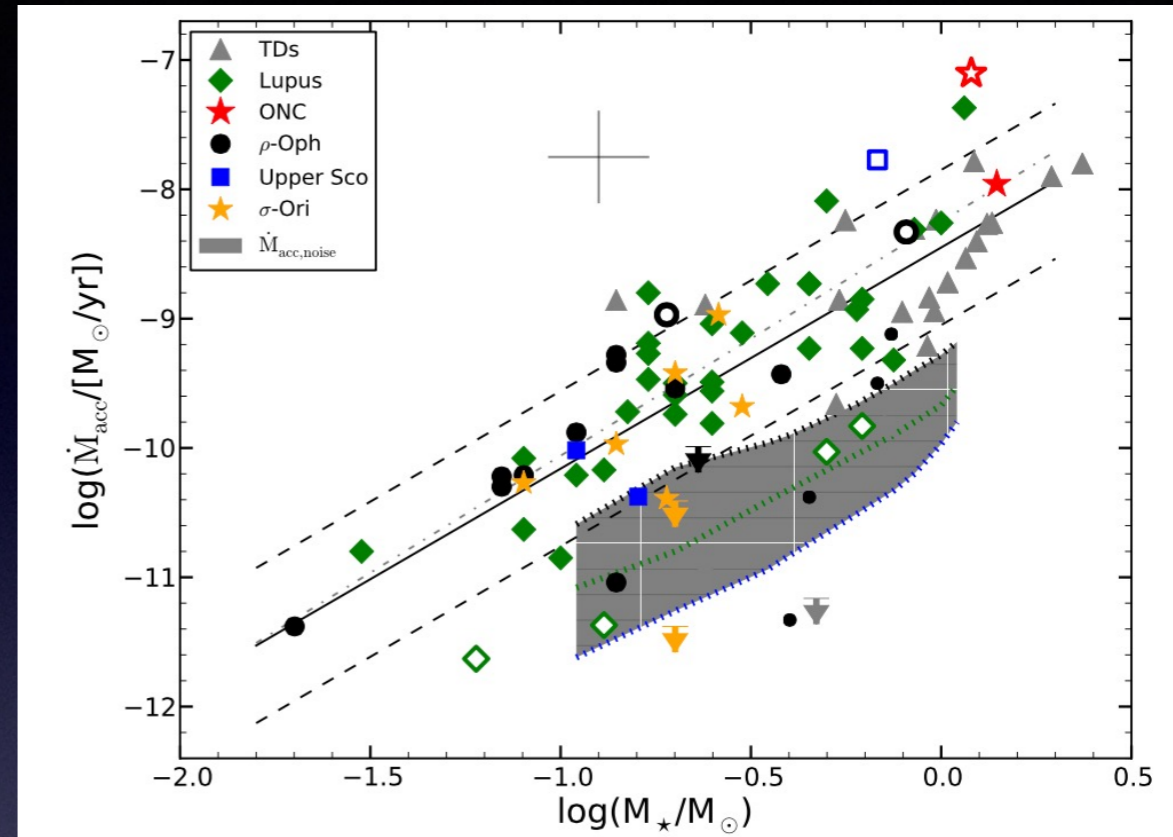
Accretion

T Tauri star - magnetospheric accretion



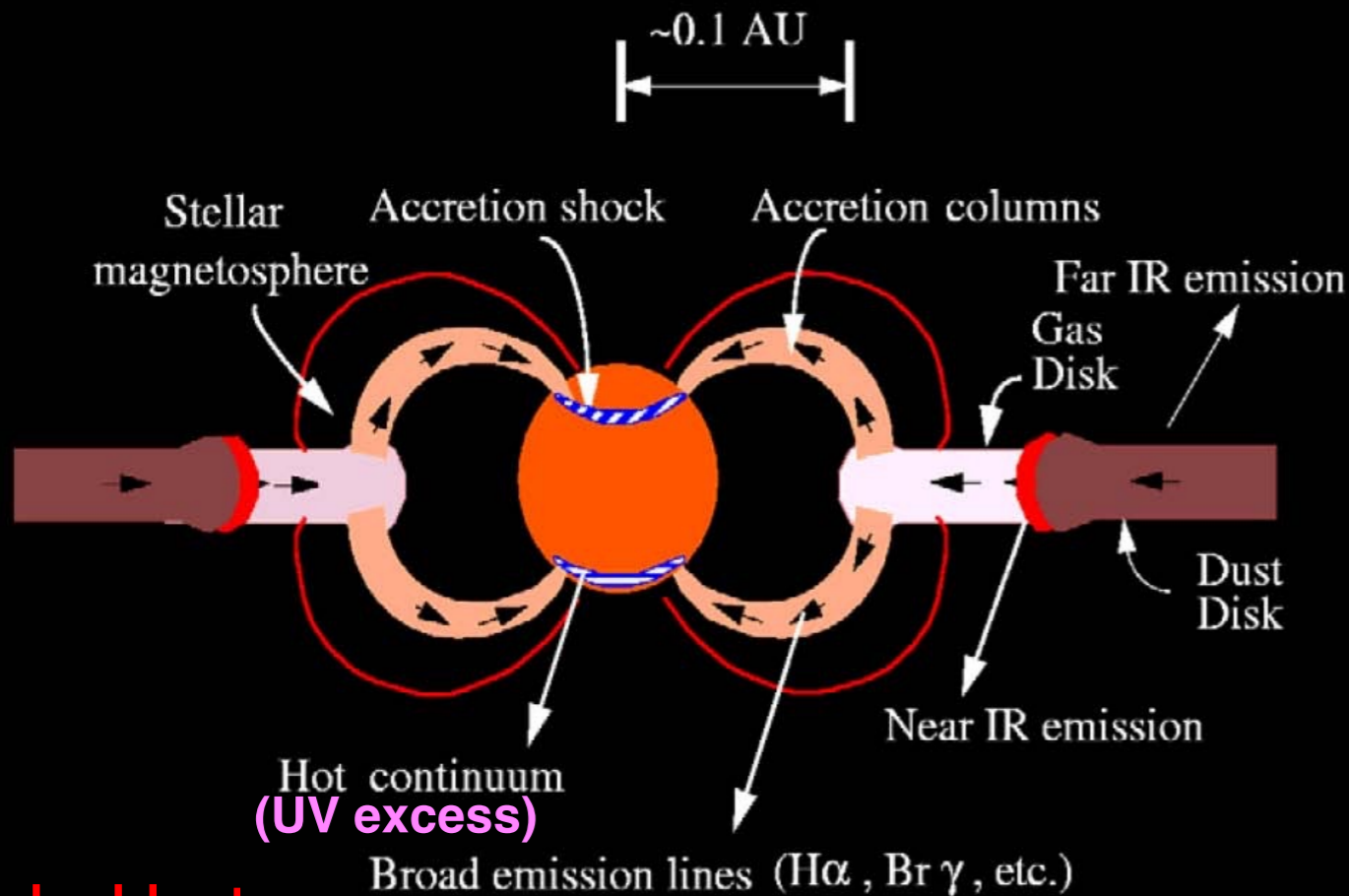
L. Hartmann

- Accretion rates fall “more or less” where predicted
- Evolution still hard to constrain (need better age/acc measurements)



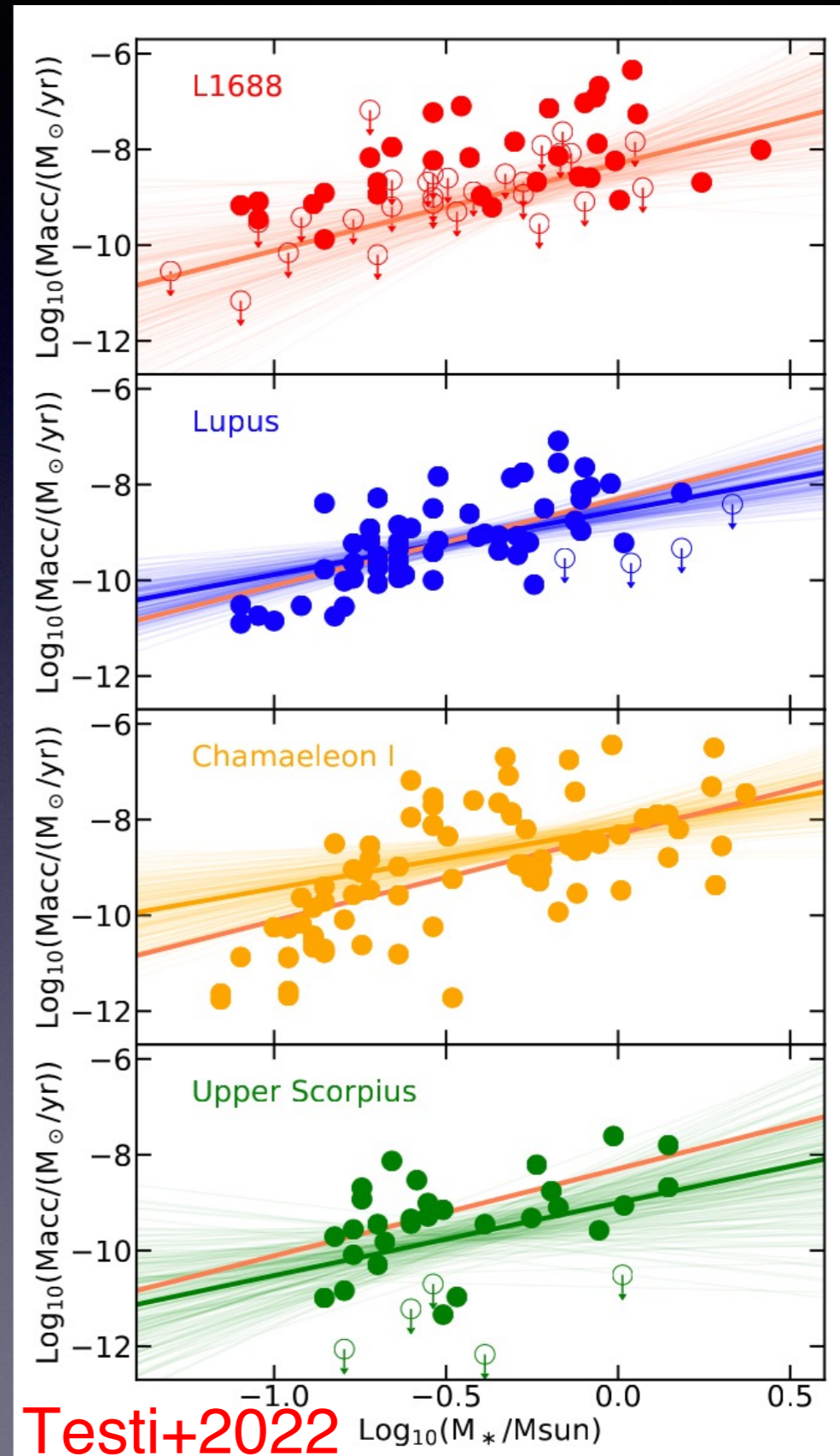
Accretion

T Tauri star - magnetospheric accretion



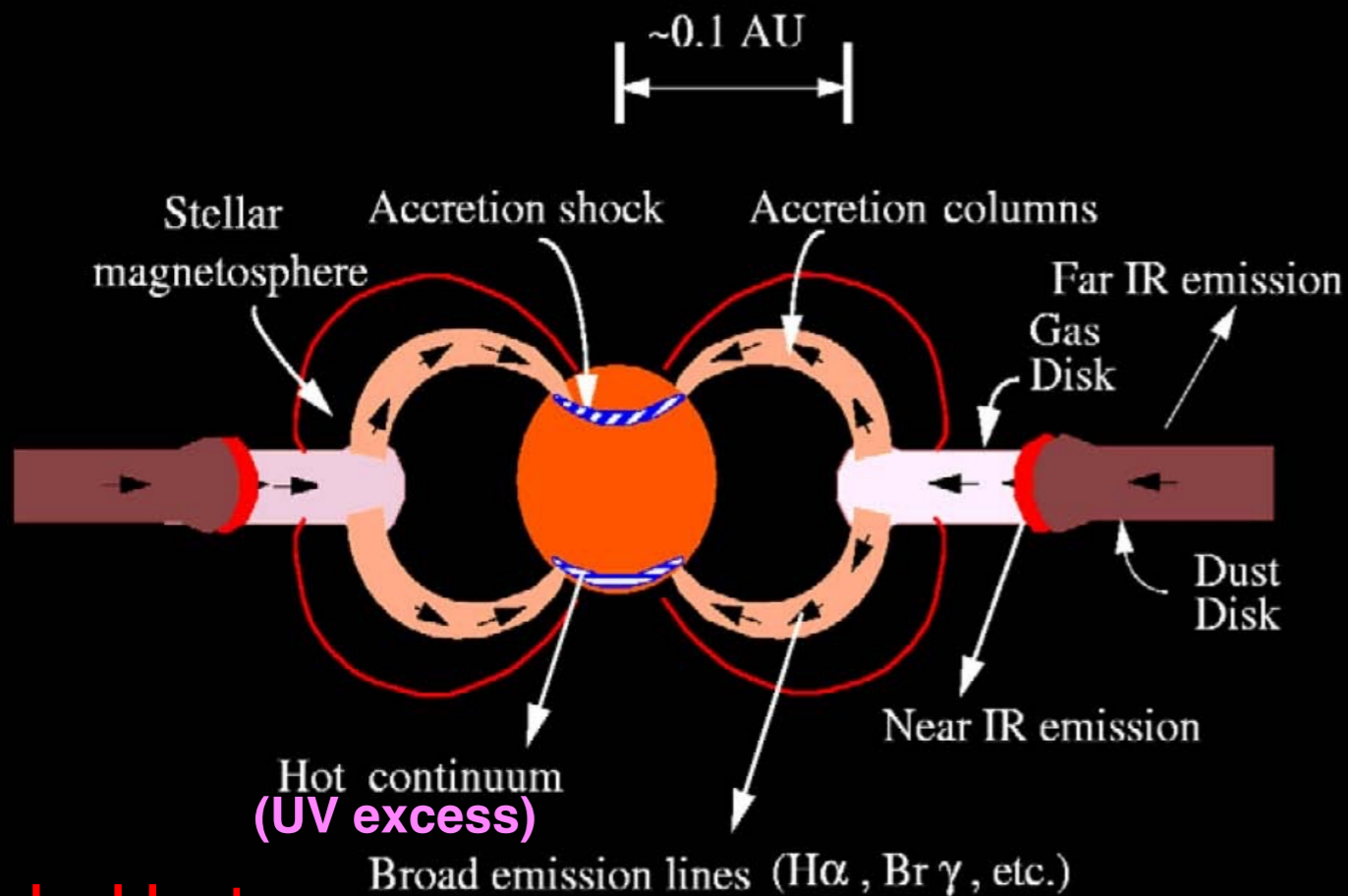
L. Hartmann

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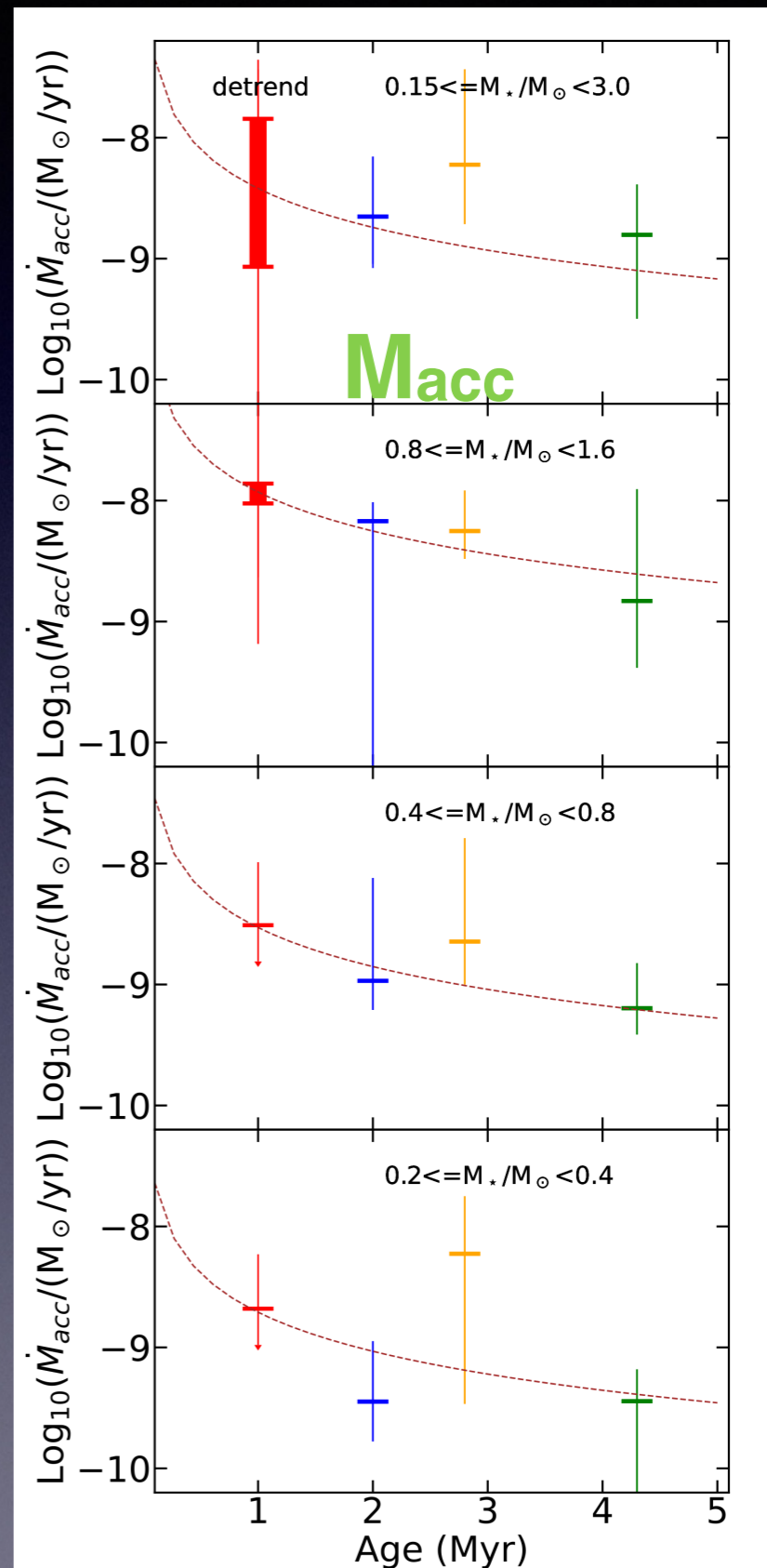
Accretion

T Tauri star - magnetospheric accretion



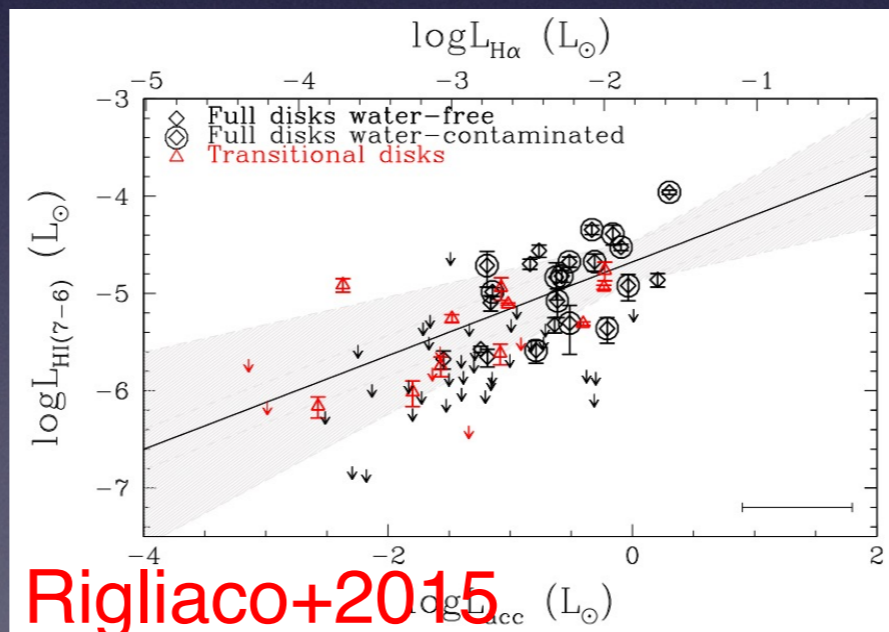
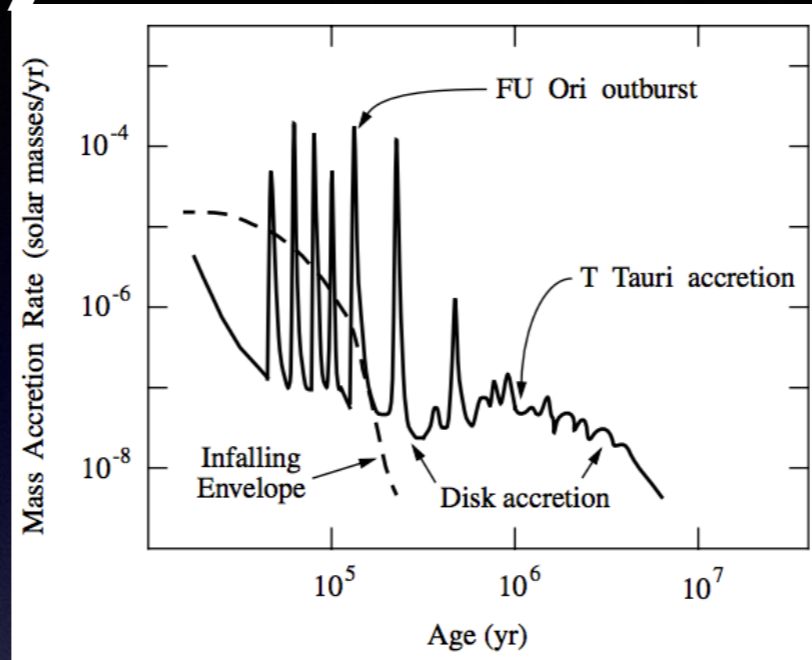
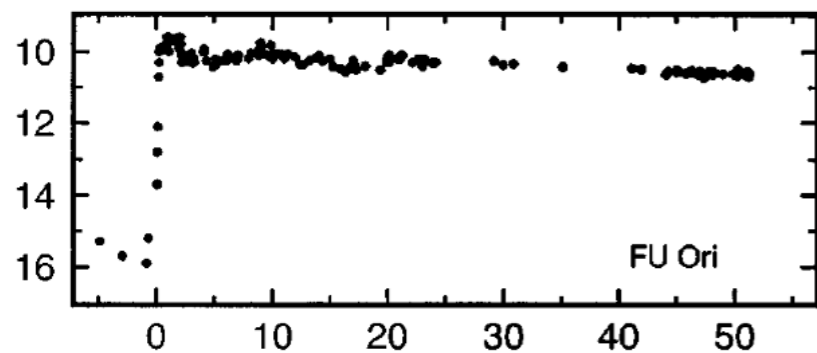
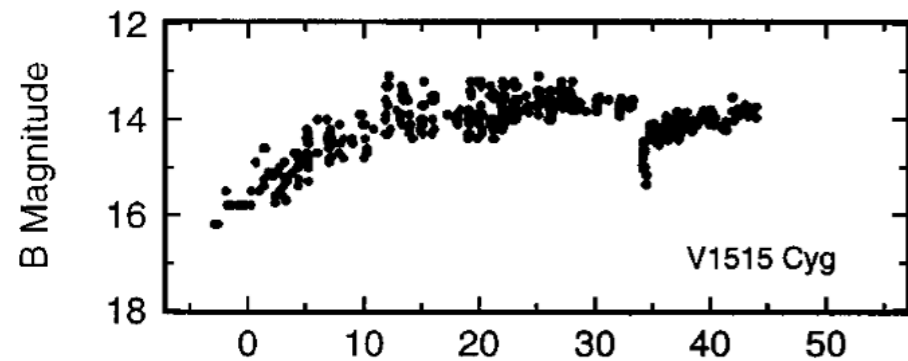
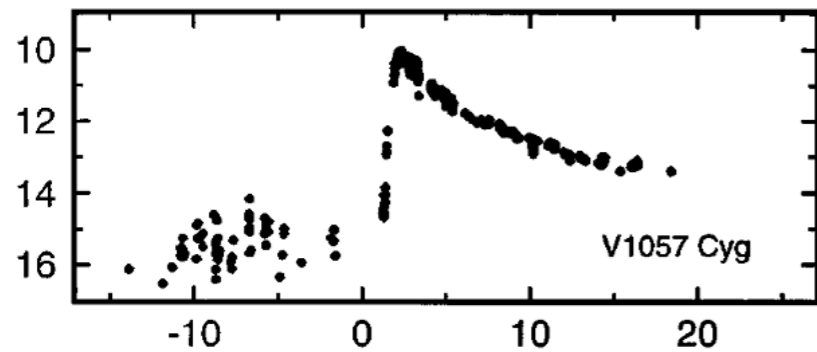
L. Hartmann

- Accretion rates fall “more or less” where predicted
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Testi+2022, see also Manara et al. 2023

Early accretion

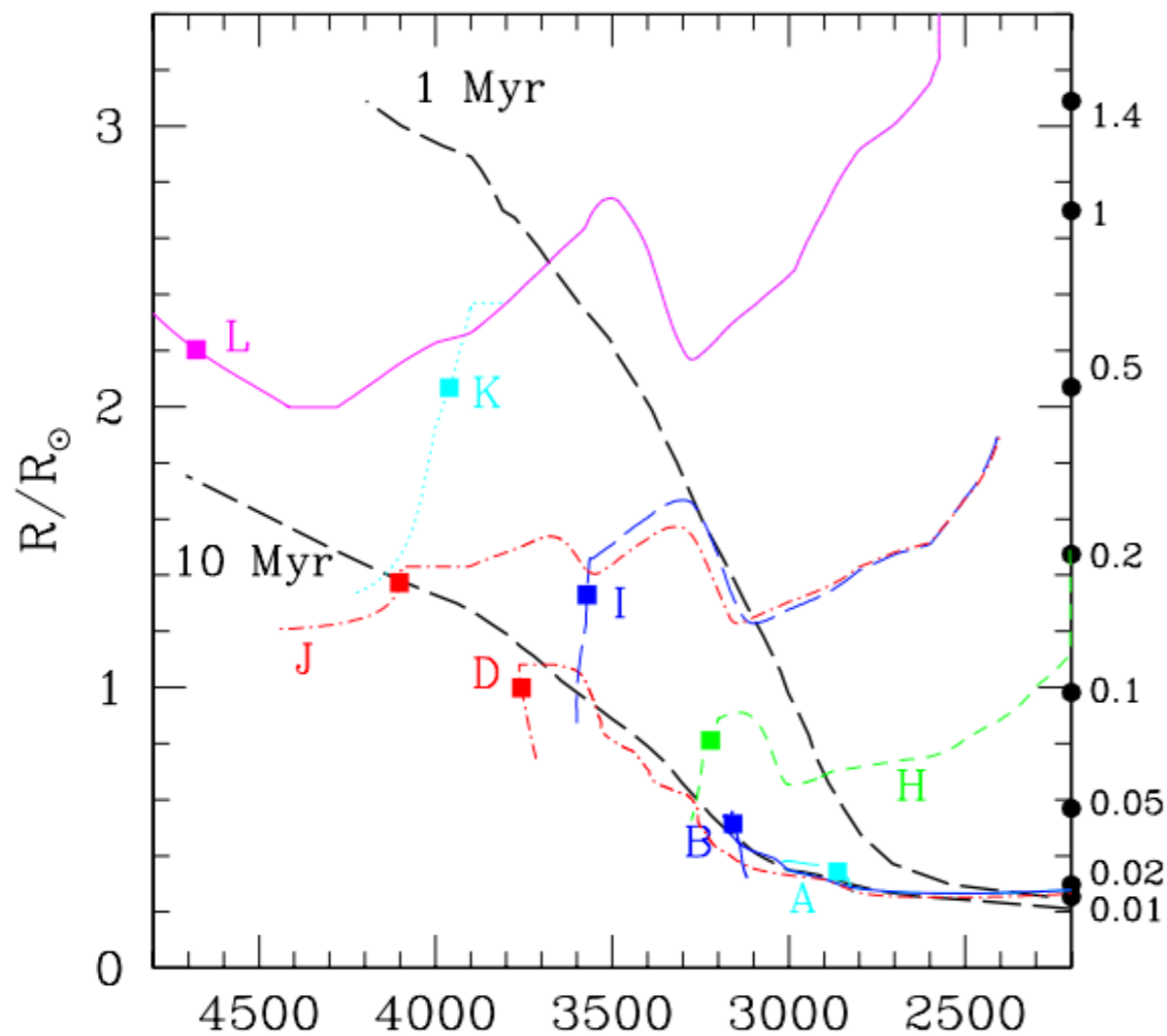


Hartmann & Kenyon 1996

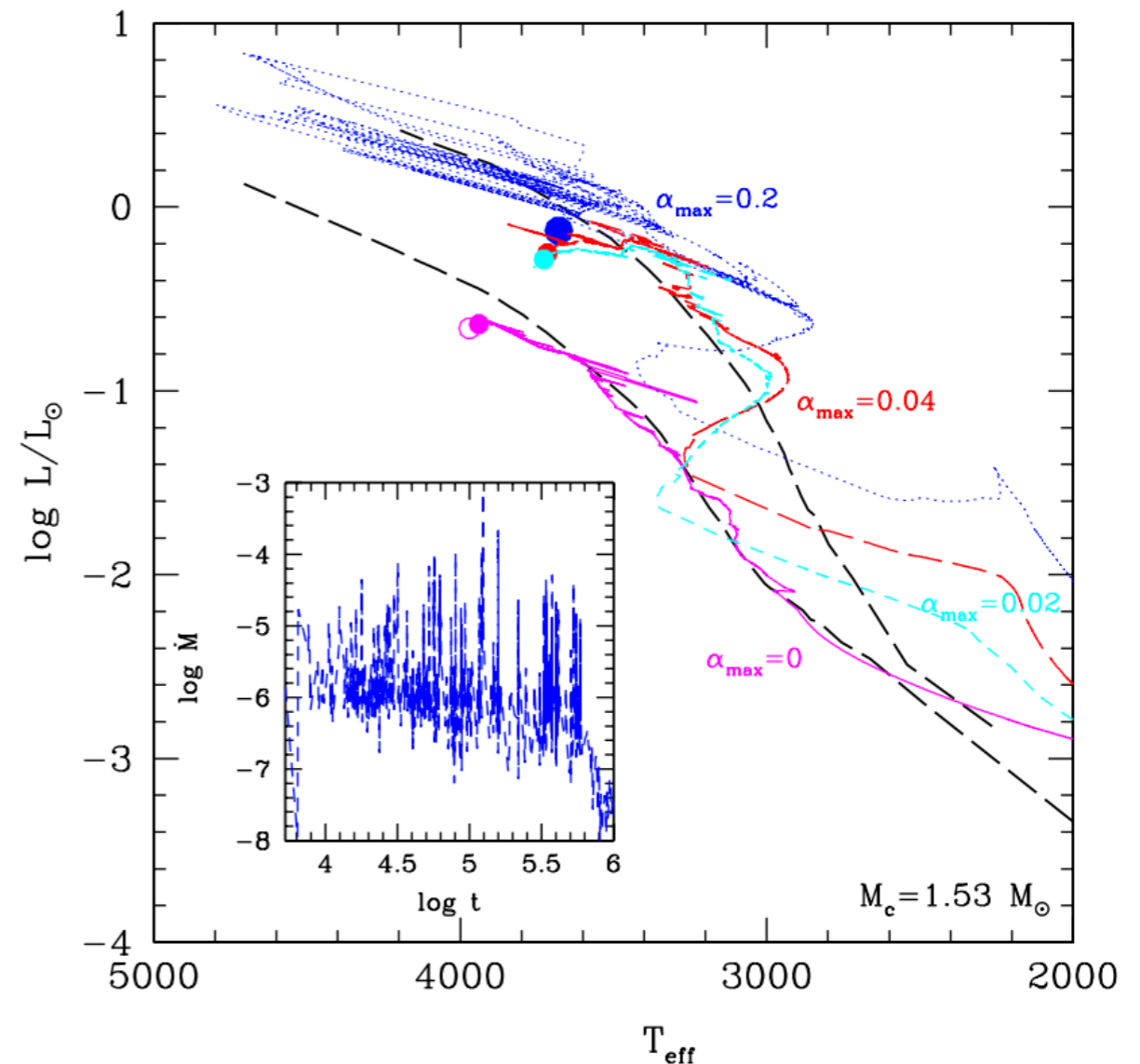
Rigliaco+2015

- Accretion highly variable in the early phases of disk evolution
- Hard to measure directly: hope from infrared lines

Young stars ages

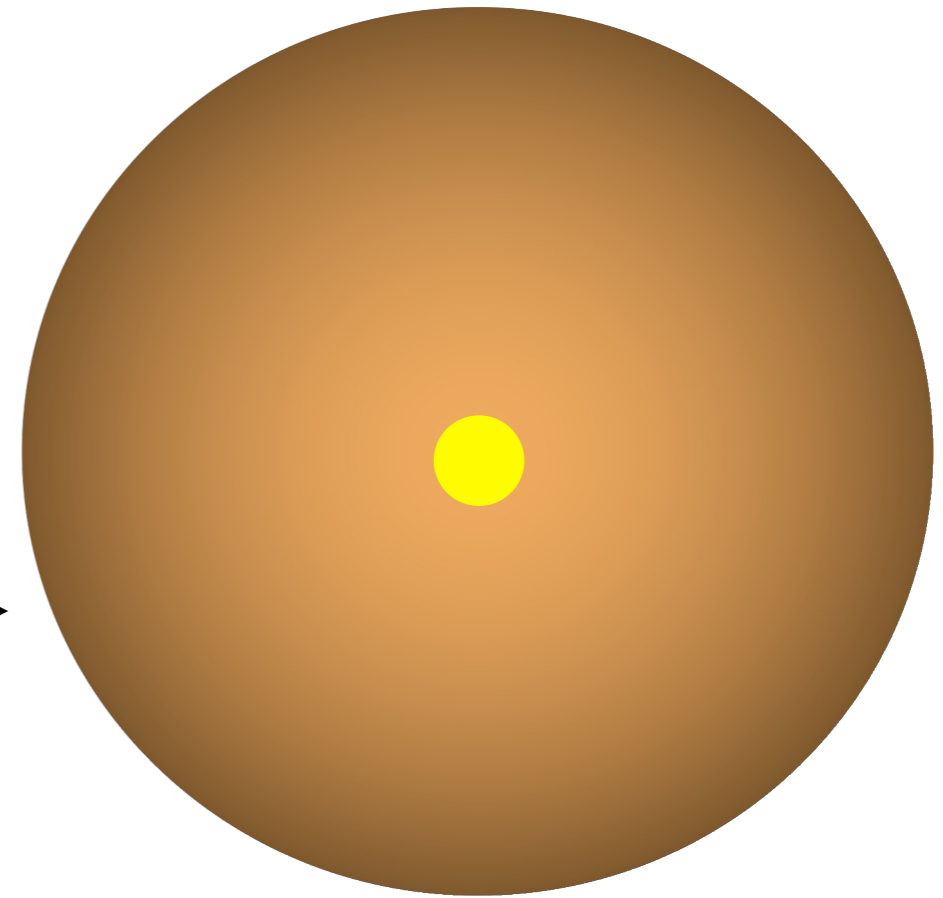
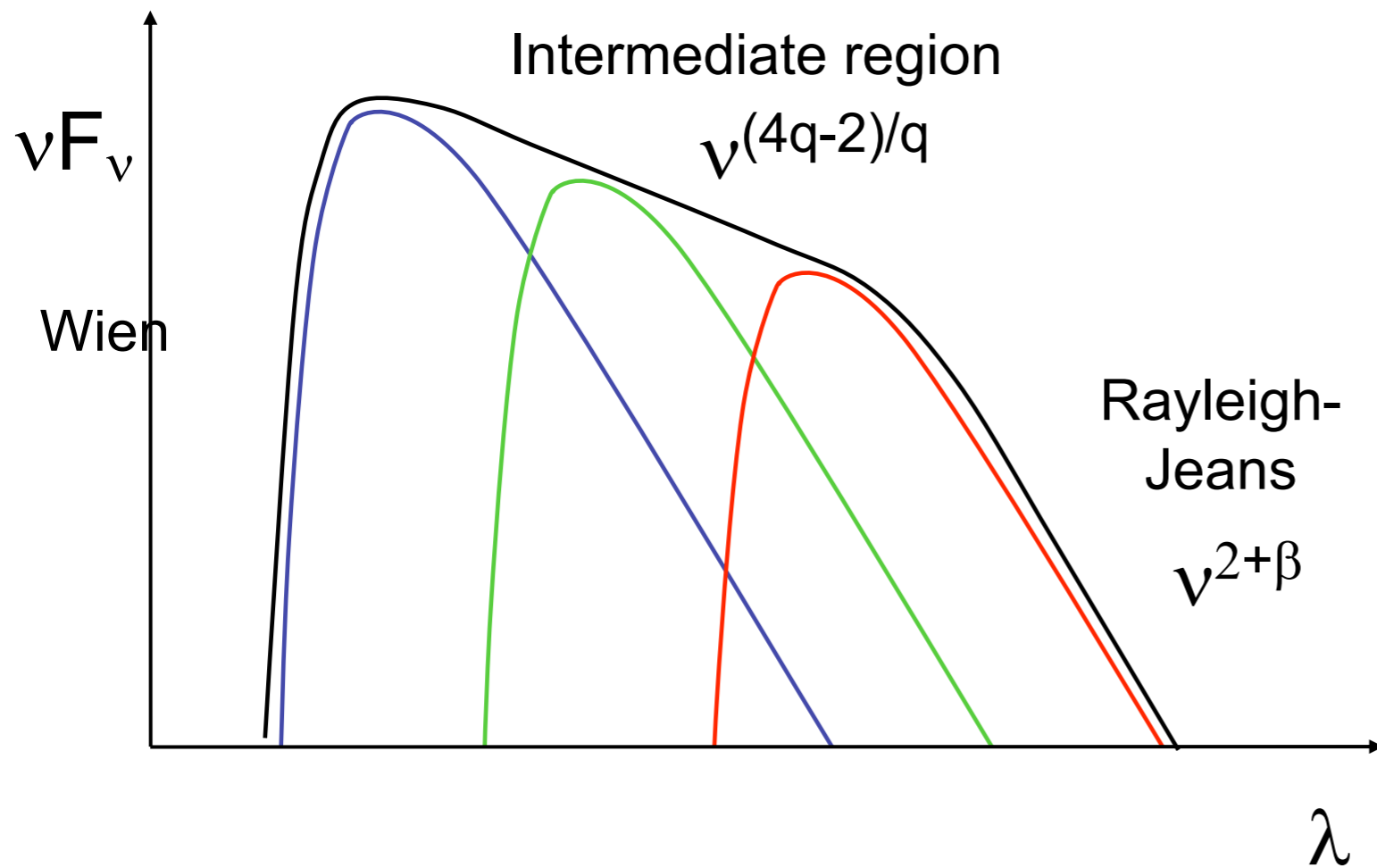


Baraffe+2010/2012



- Uncertainty from stellar accretion history
- Do we know “relative” ages?
- Early accretion history very uncertain, but potentially critical

SED for a locally isothermal disk



$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

$\tau_\nu \ll 1$

$$F_\nu \propto \Sigma(r) B_\nu(T_d(r)) \kappa_\nu$$

$T_d \sim \text{const.}$

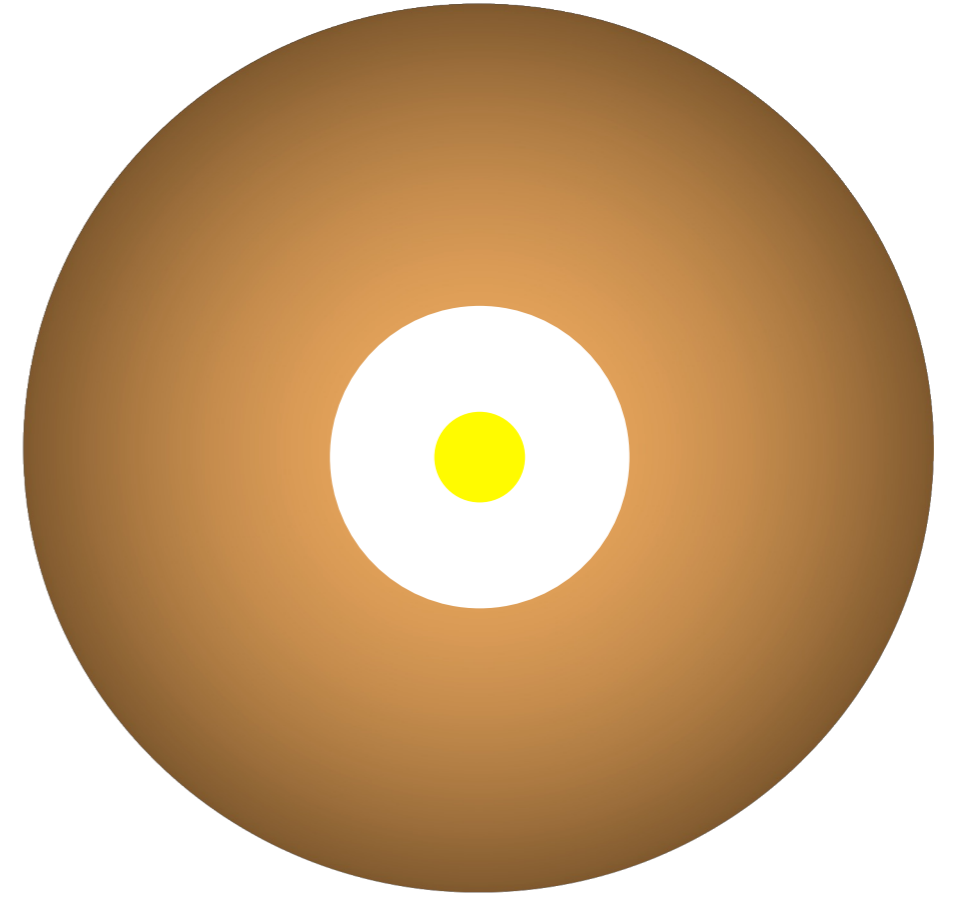
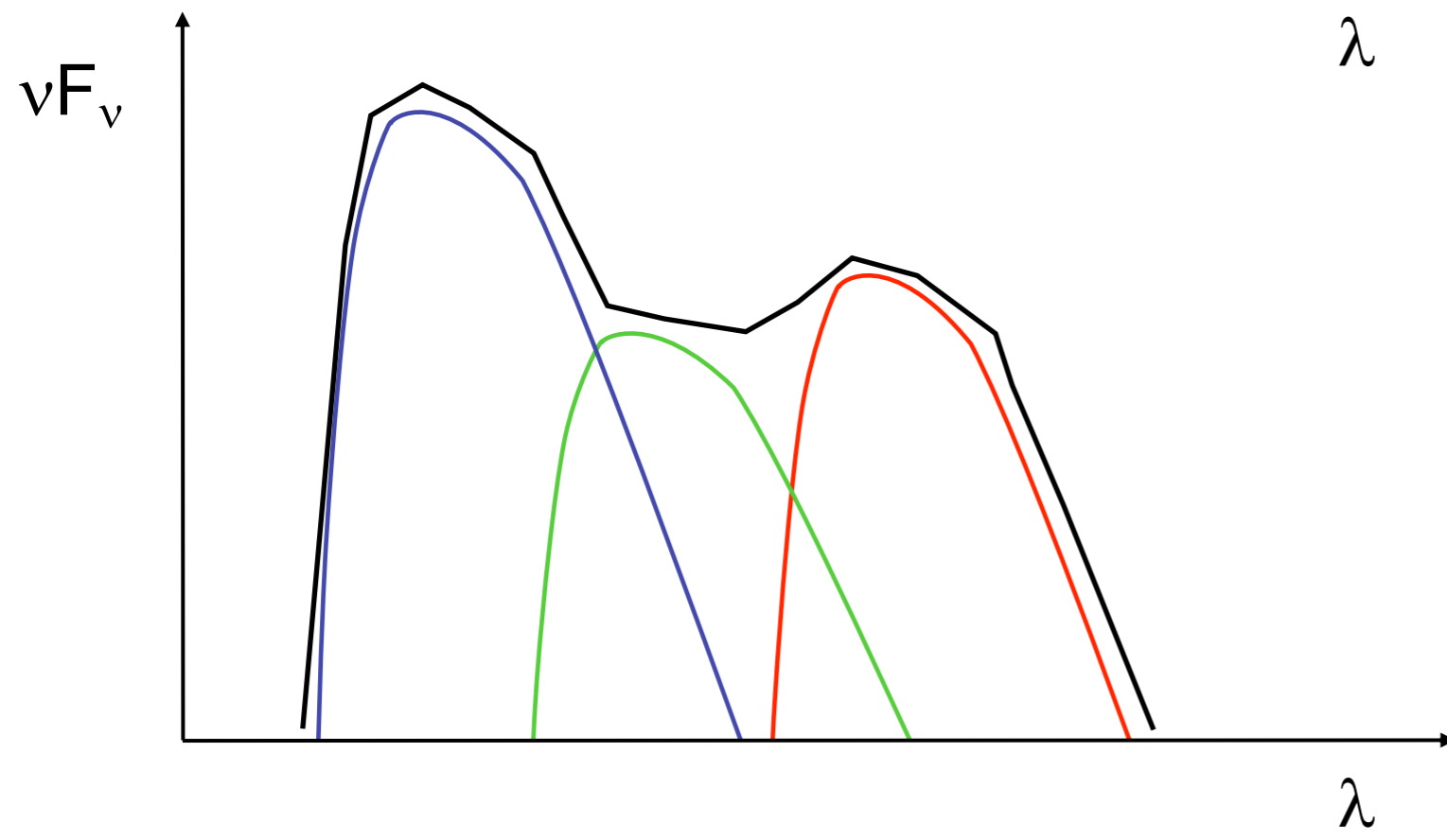
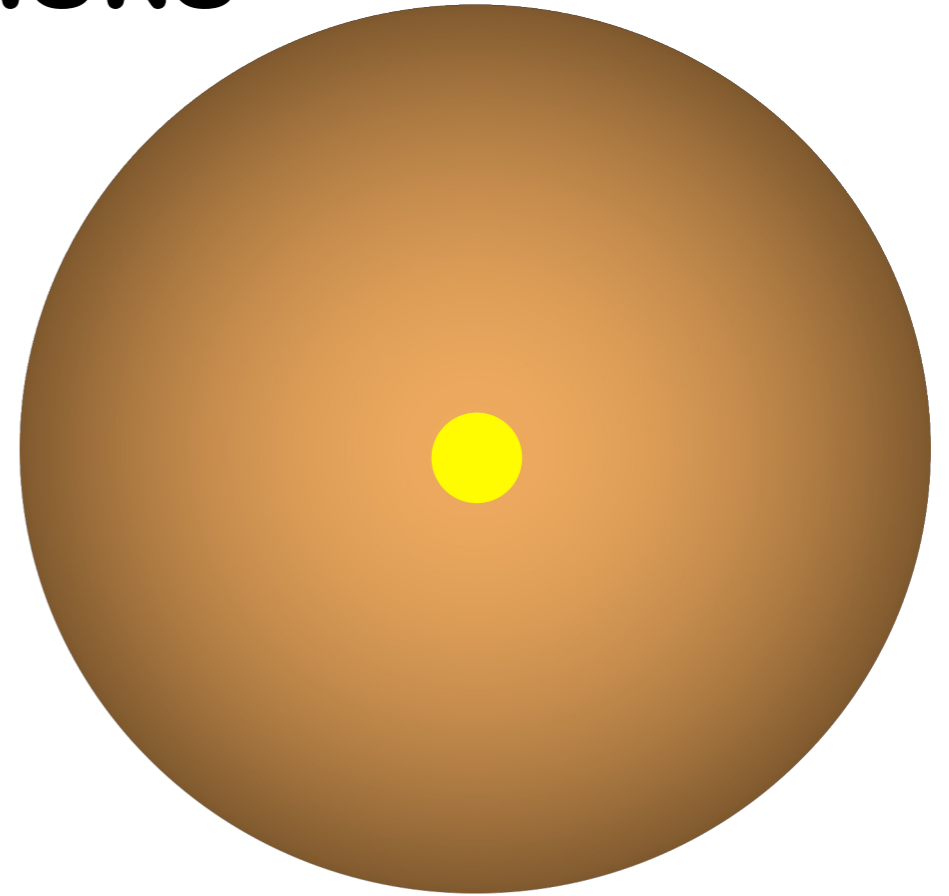
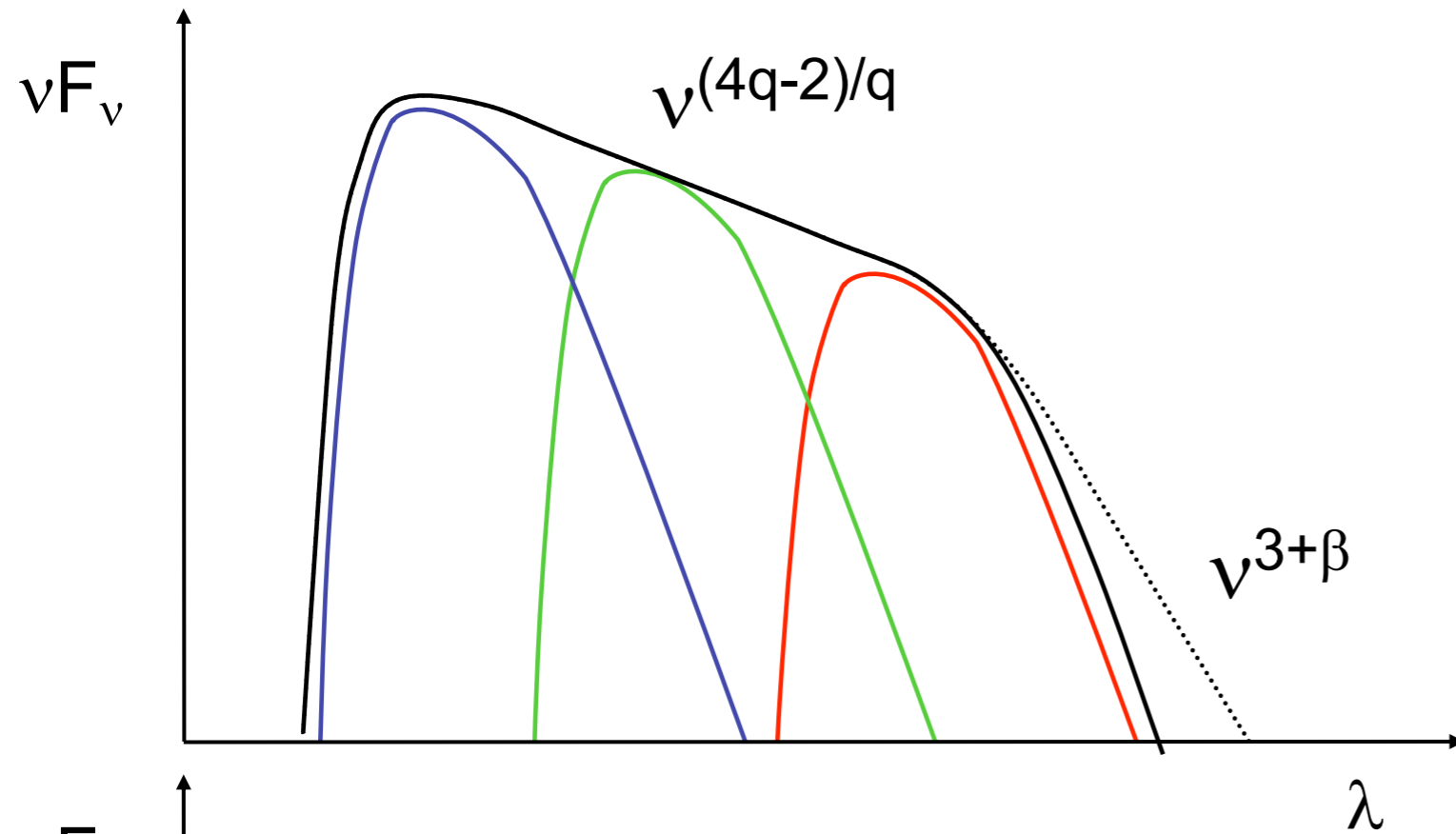
If $\tau_\nu \ll 1$:

$$F_\nu \propto \kappa_\nu \times B_\nu(T_d) \times M_d$$

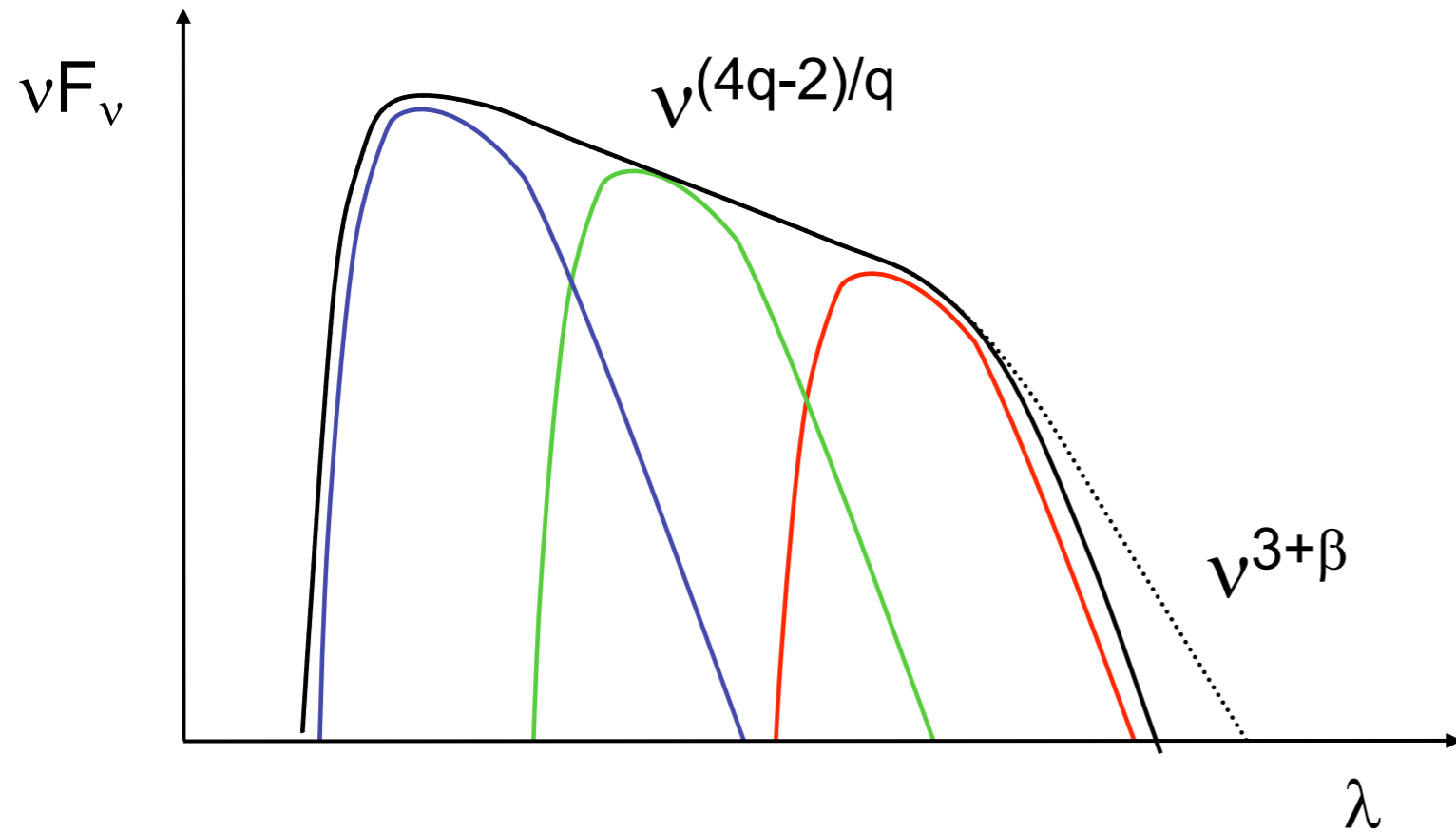
If $\tau_\nu \gg 1$:

$$F_\nu \propto B_\nu(T_d) \times \text{Area}$$

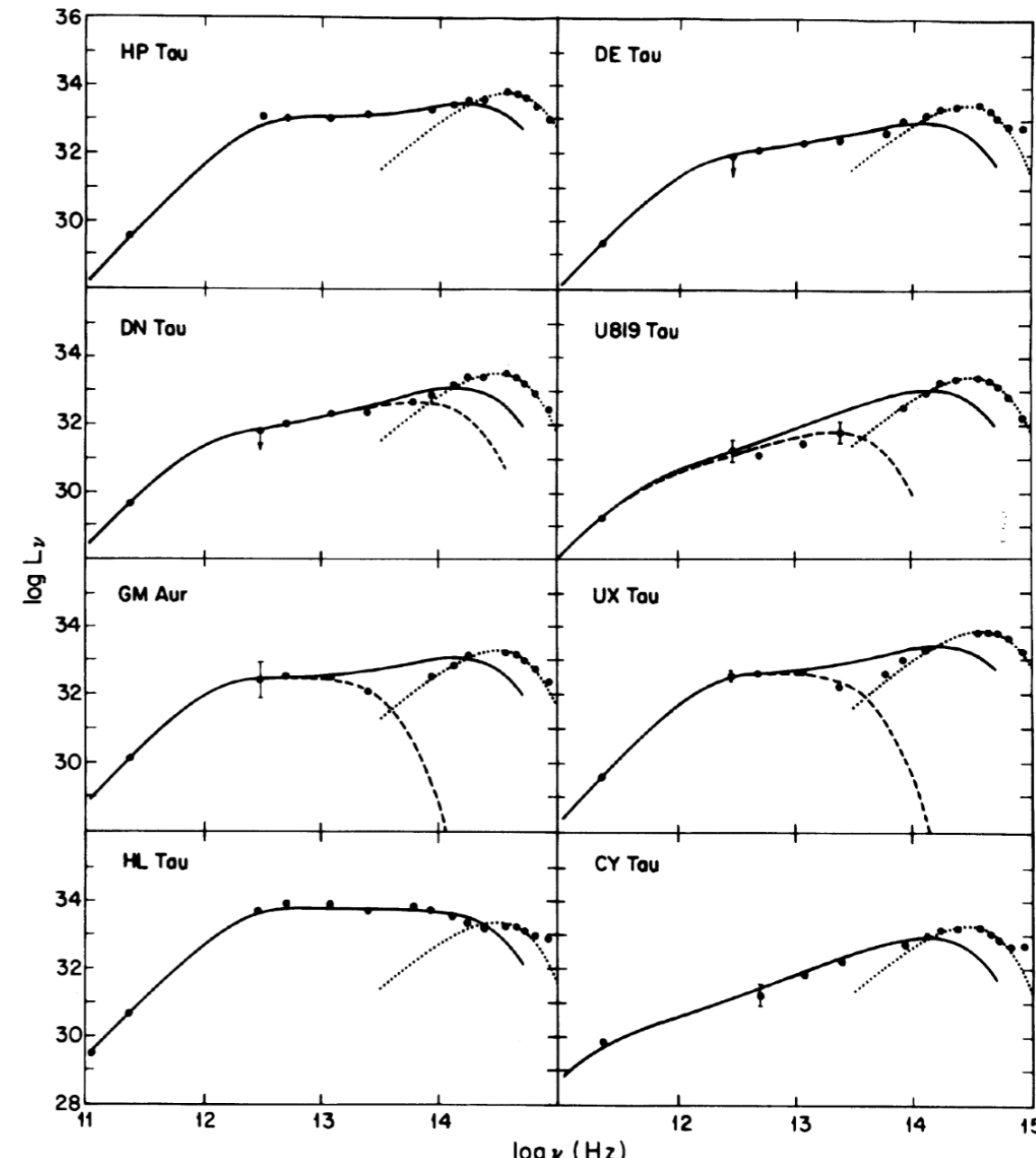
Consequence: SED signature for Transition Disks



SED of a locally isothermal disk



Beckwith+ 1991

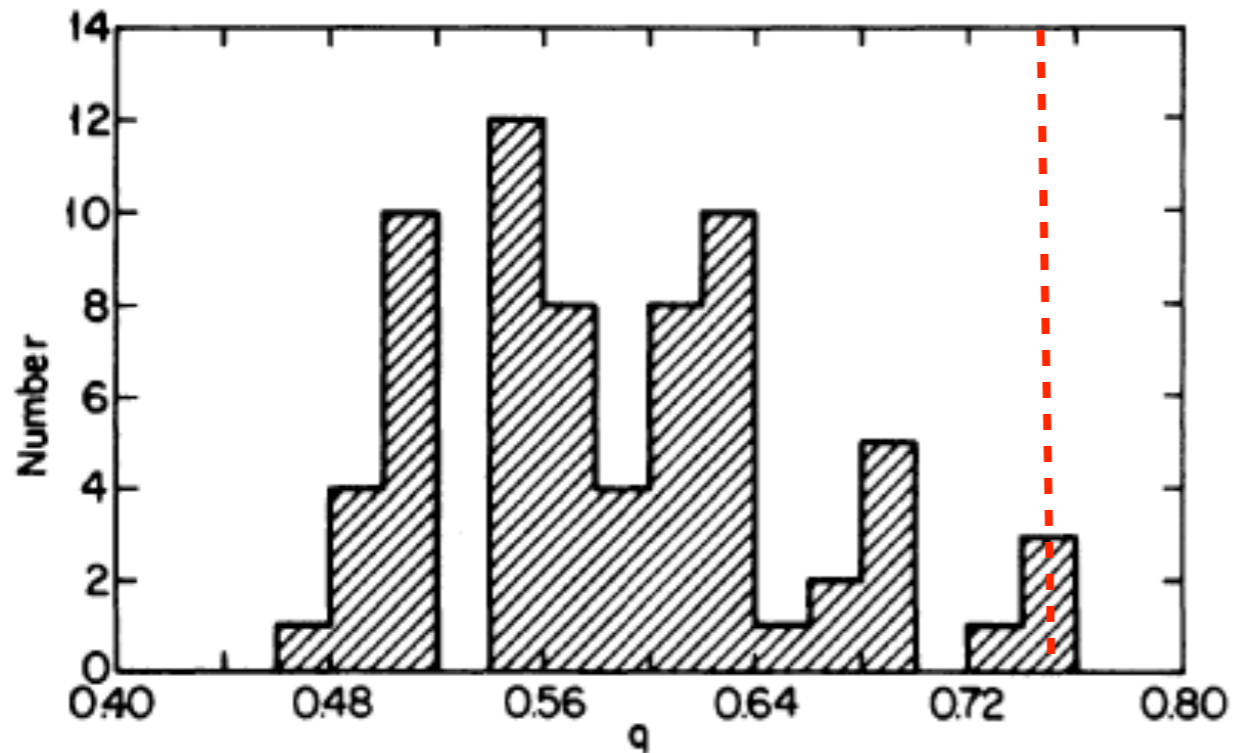


$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

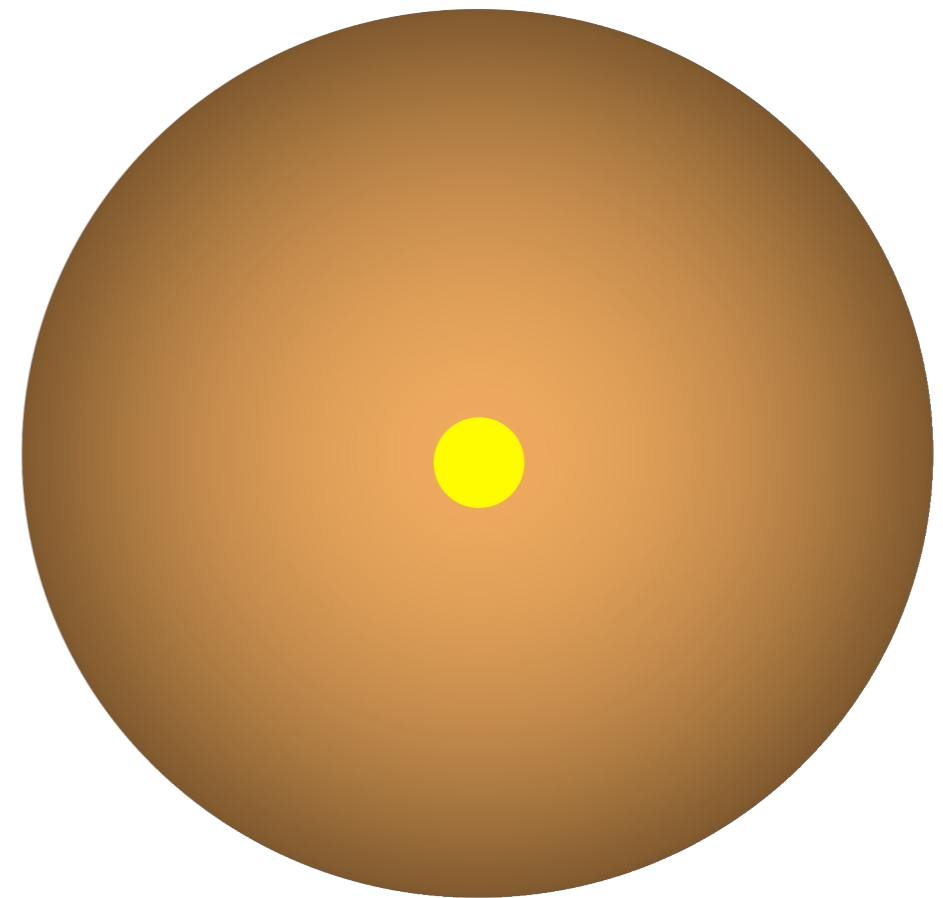
$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

SED for a locally isothermal disk



Beckwith et al. (1991)



$$F_{\nu} = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_{\nu}(T_d)(1 - e^{-\tau_{\nu}})2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_{\nu} \propto \Sigma(r) \kappa_{\nu} \quad \Sigma(r) \propto r^{-p} \quad \kappa_{\nu} \propto \kappa_0 v^{\beta}$$

Viscous heating provides a poor fit of protoplanetary disc temperature: real disks are warmer than expected in the outer regions!

“flat” passive disk

Irradiation flux:

$$F_{\text{irr}} = \alpha \frac{L_*}{4\pi r^2}$$

The flaring angle:

$$\alpha \cong \frac{0.4 r_*}{r}$$

$$T = \left(\frac{0.4 r_* L_*}{4\pi\sigma r^3} \right)^{1/4}$$

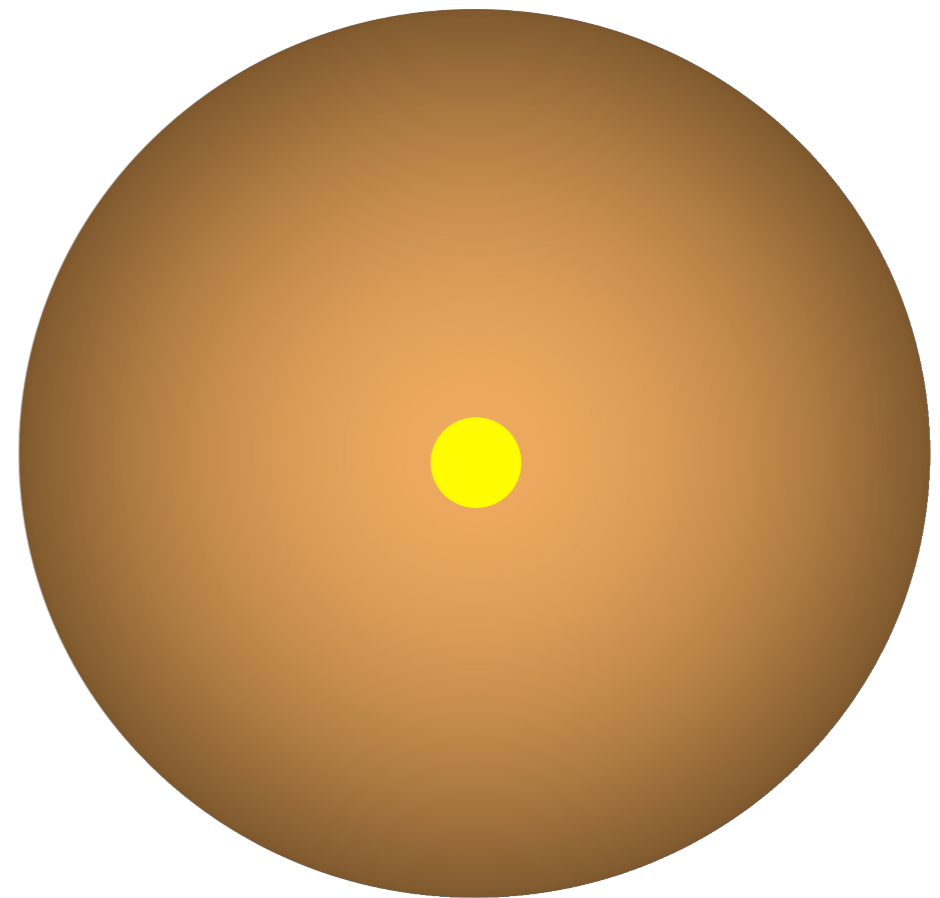
$$T \propto r^{-3/4}$$

Coincidentally, same profile as an
viscously heated disk : not good!

$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 v^\beta$$



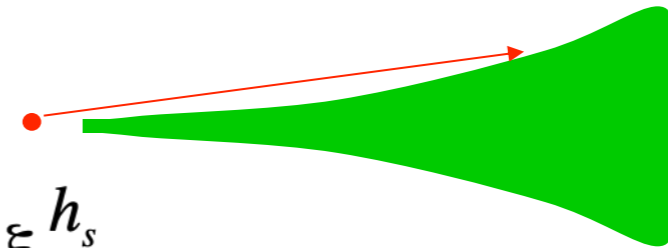
“flared” passive disk

Irradiation flux:

$$F_{\text{irr}} = \alpha \frac{L_*}{4\pi r^2}$$

The flaring angle:

$$\alpha = r \frac{\partial}{\partial r} \left(\frac{h_s}{r} \right) \rightarrow \xi \frac{h_s}{r}$$

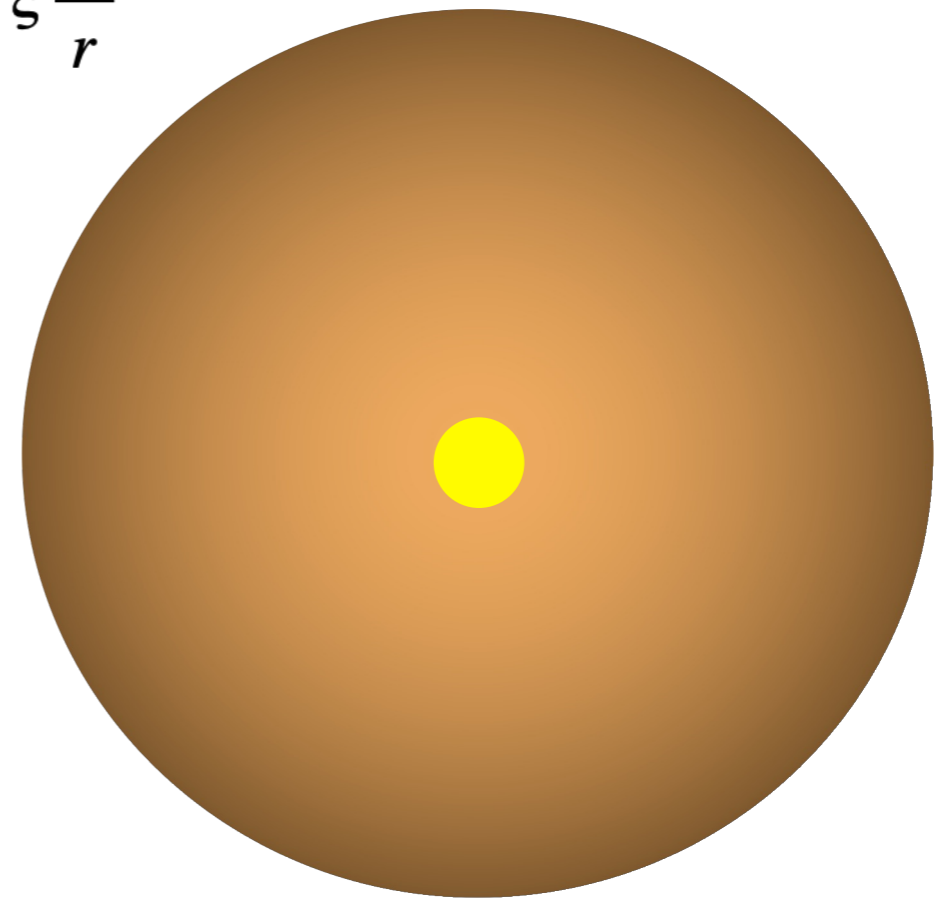


$$T^4 = \frac{\xi}{\sigma} \frac{h_s L_*}{4\pi r^3}$$

$$h_s = \chi h$$

Can work...

...depending on $h_s(r)$

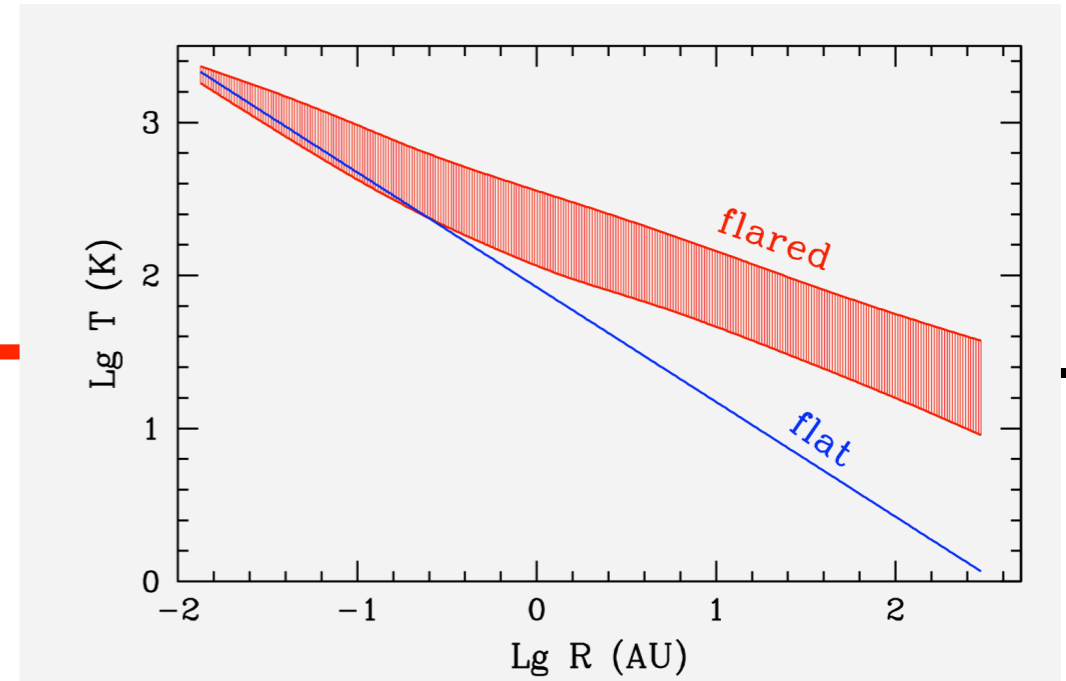
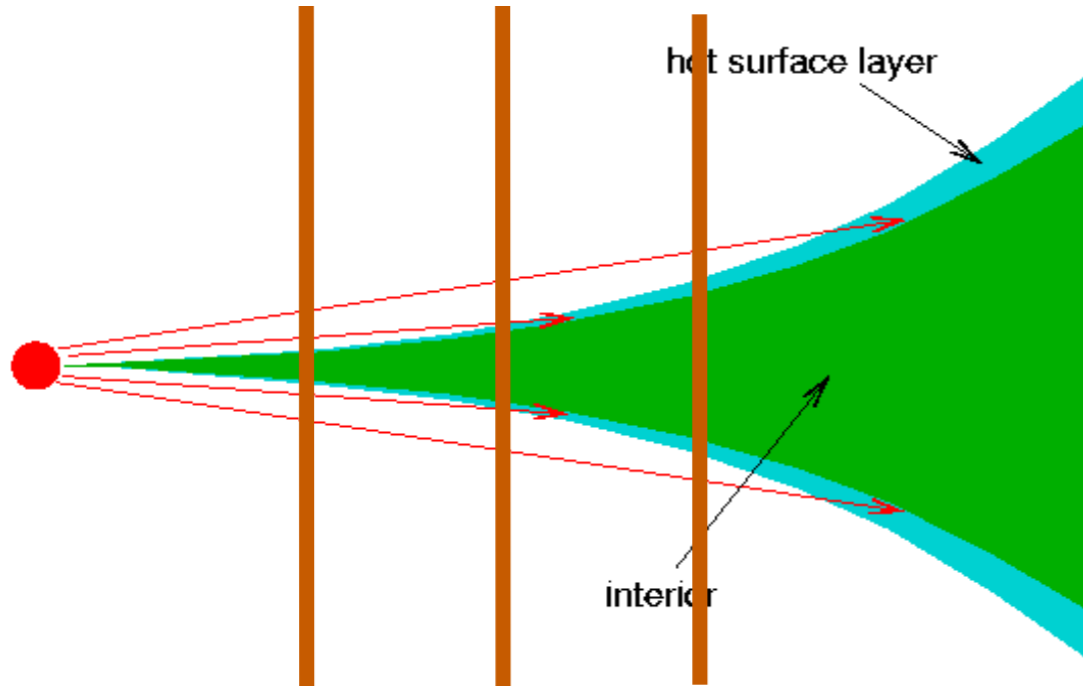


$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d) (1 - e^{-\tau_\nu}) 2\pi r dr$$

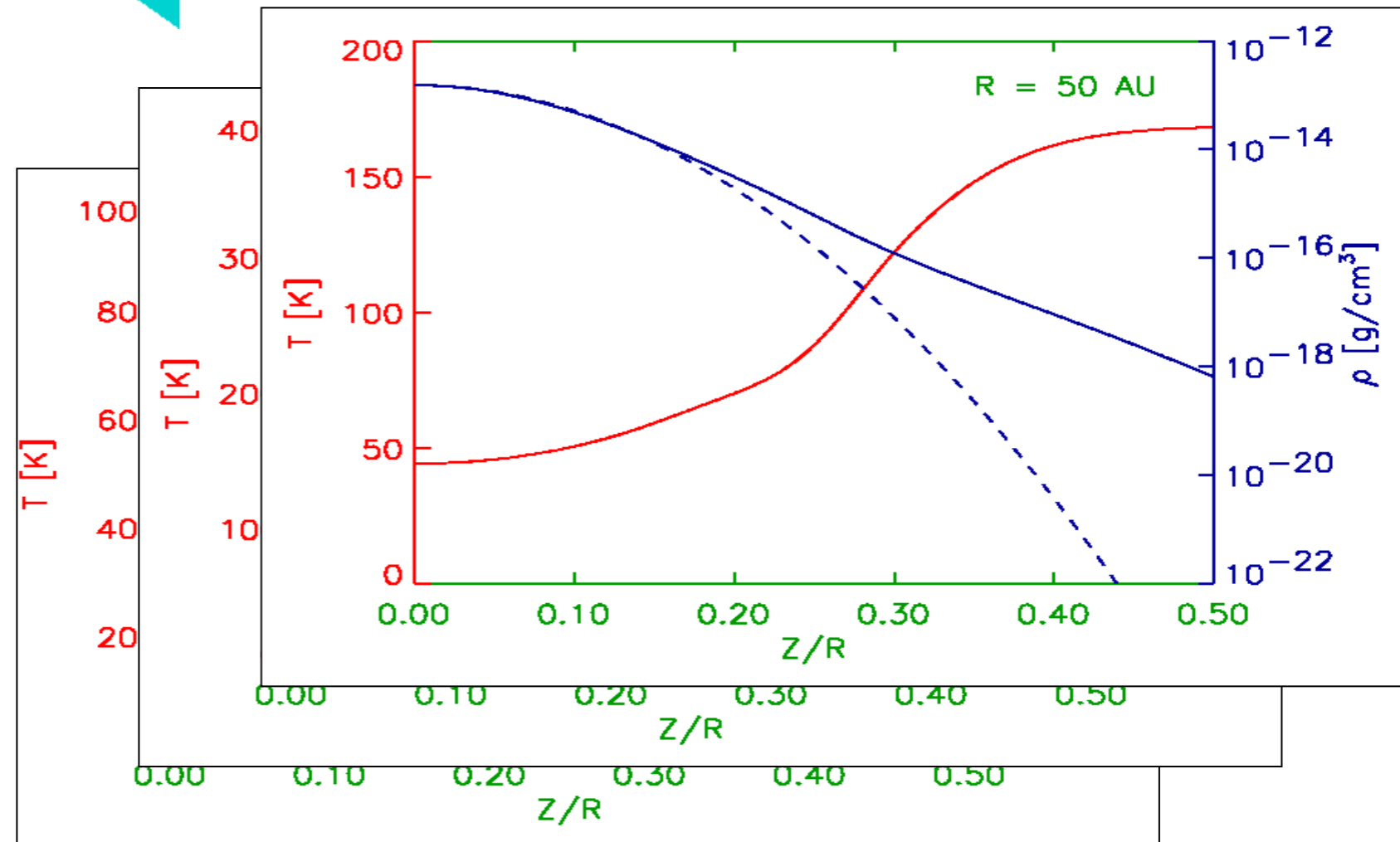
$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

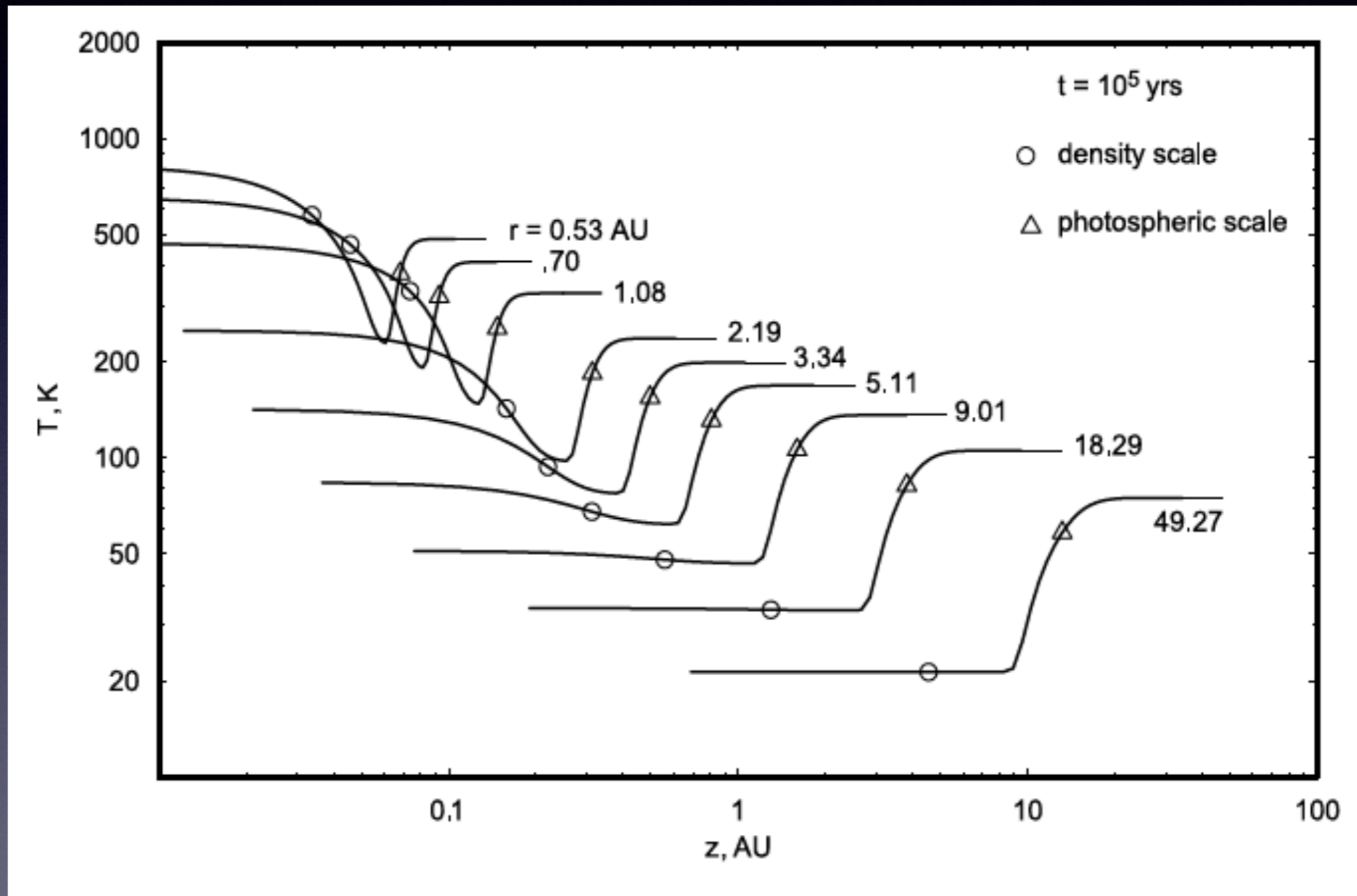
Flared disks: detailed models



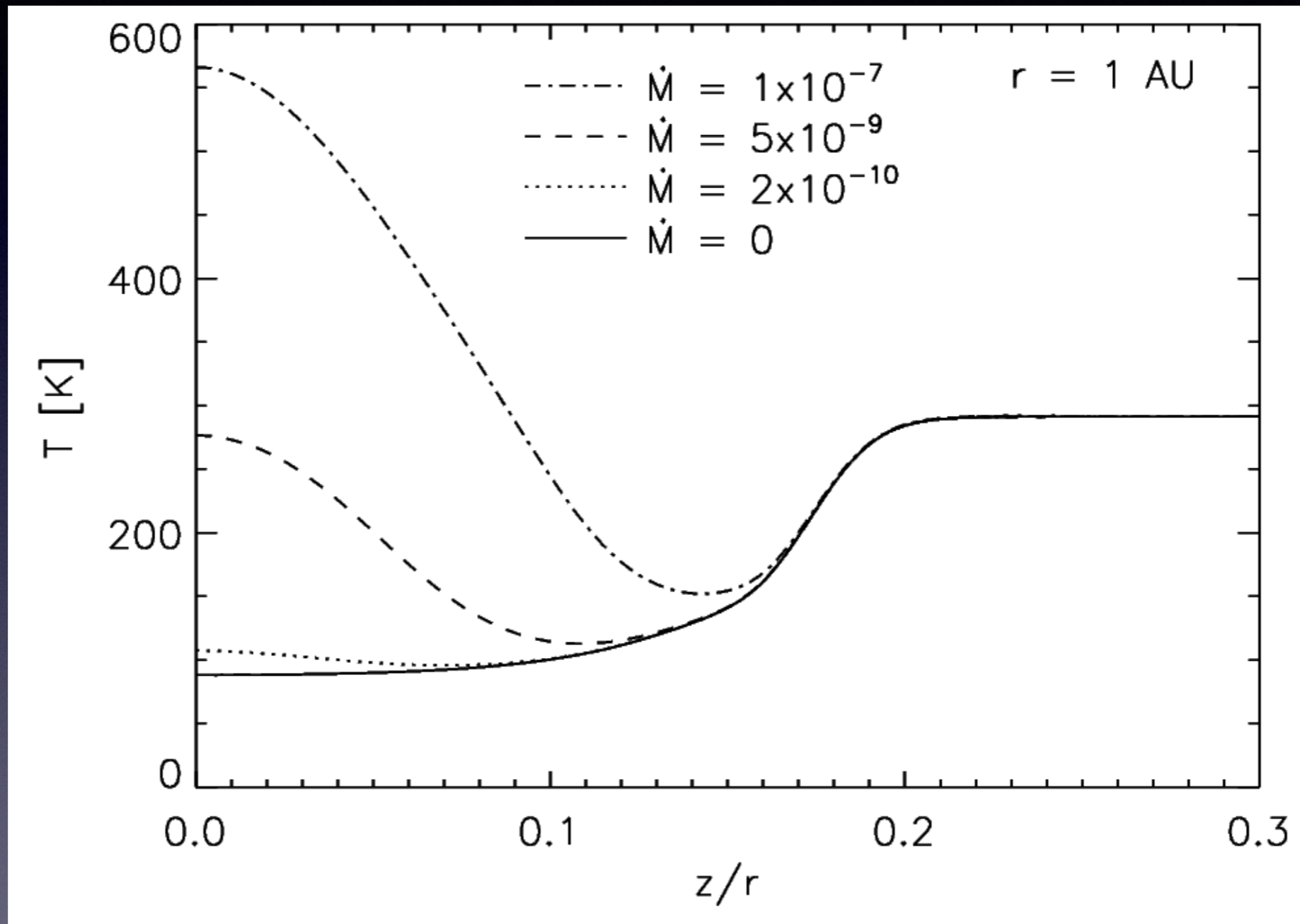
... consists of vertical slices, each forming a 1D problem. All slices are independent from each other.



Including viscous heating



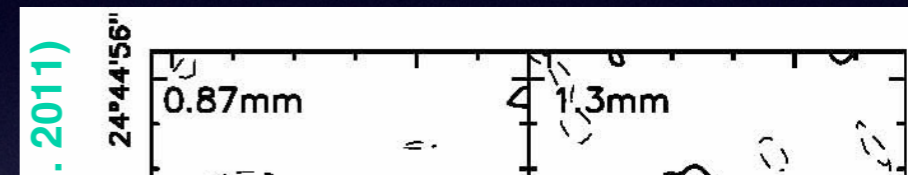
Including viscous heating



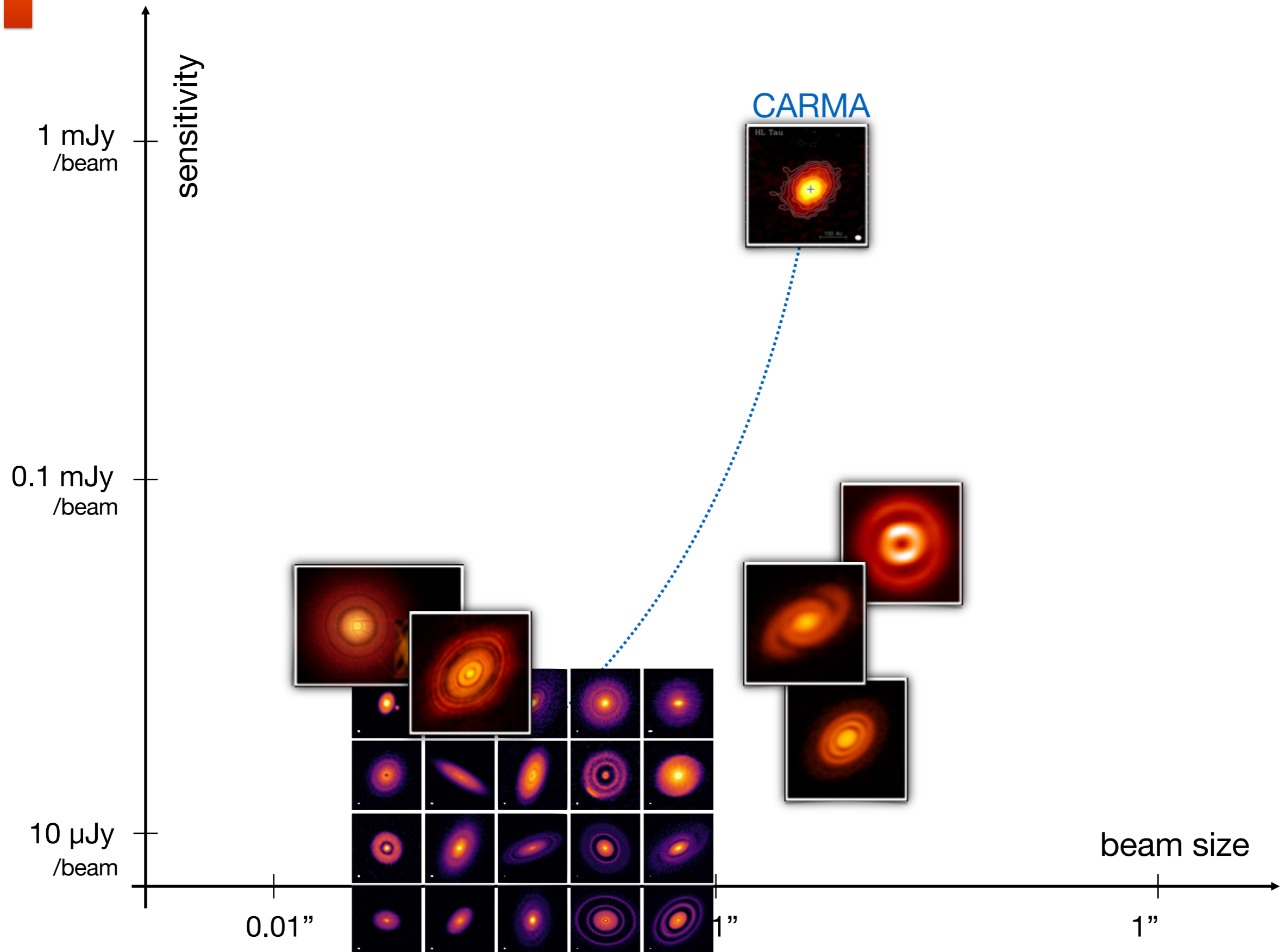
($M_{\text{acc}} \sim 10^{-8} M_{\text{sun}}/\text{yr}$ @ 1 Myr)

Resolving disk structure

- $10\text{AU}@140\text{pc}=0.14\text{ arcsec}$
- Diffraction: $0.14\text{arcsec}@1\text{mm} \Rightarrow 1.5\text{km}$
- Need to use interferometry

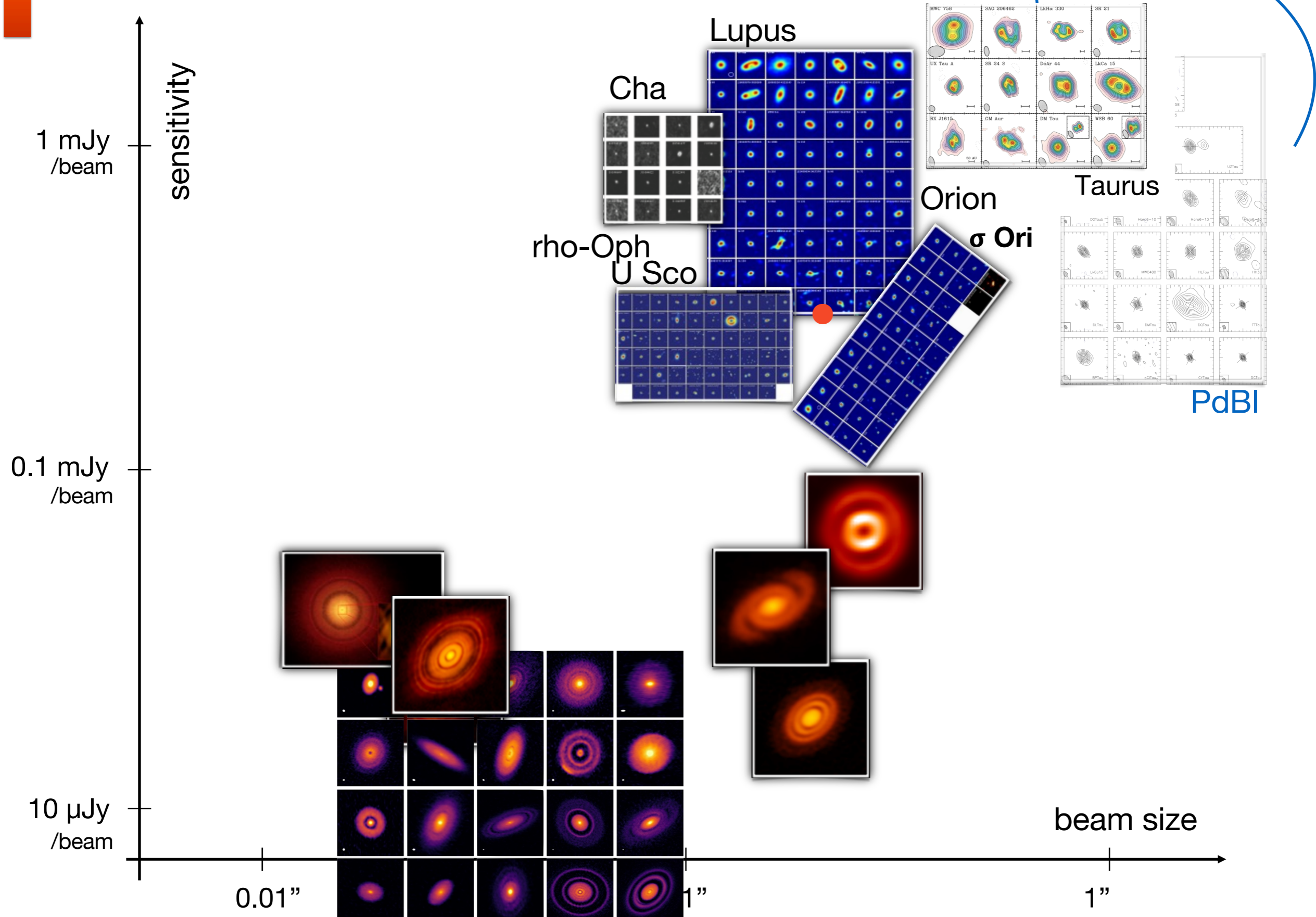


The ALMA Revolutions



(slide thanks to M. Tazzari)

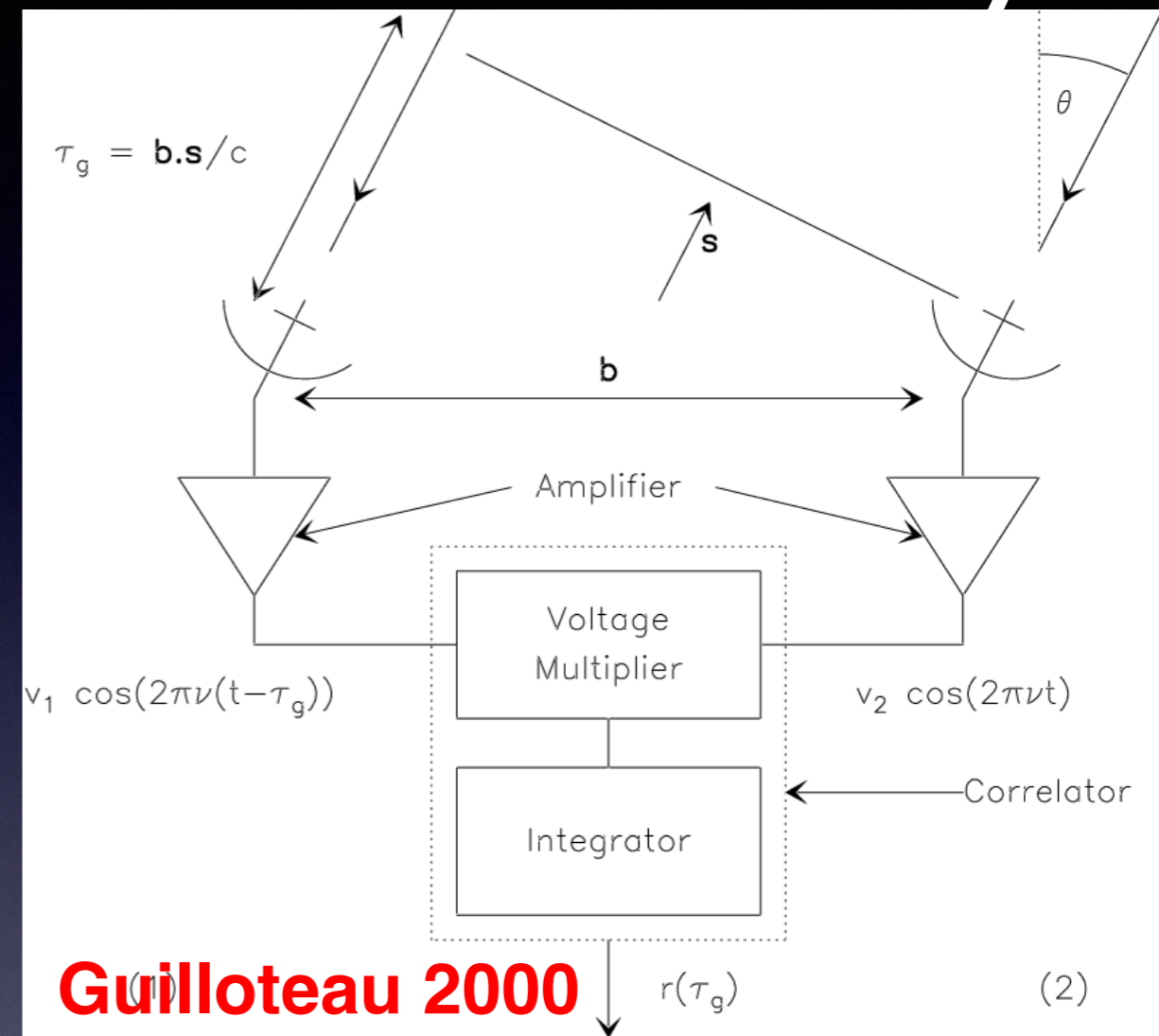
The ALMA Revolutions



(slide thanks to M. Tazzari)

Small digression on interferometry

- Interference pattern of the signal from two antennas separated by a baseline b
- After correction for the optical path delay each pair of antennas measure the fringe visibility corresponding to the baseline b (as seen from the source)



$$V(u, v) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} P(x, y) I(x, y) \exp(-2i\pi (ux + vy)) dx dy$$

(x, y) = Sky (u, v) = baselines plane

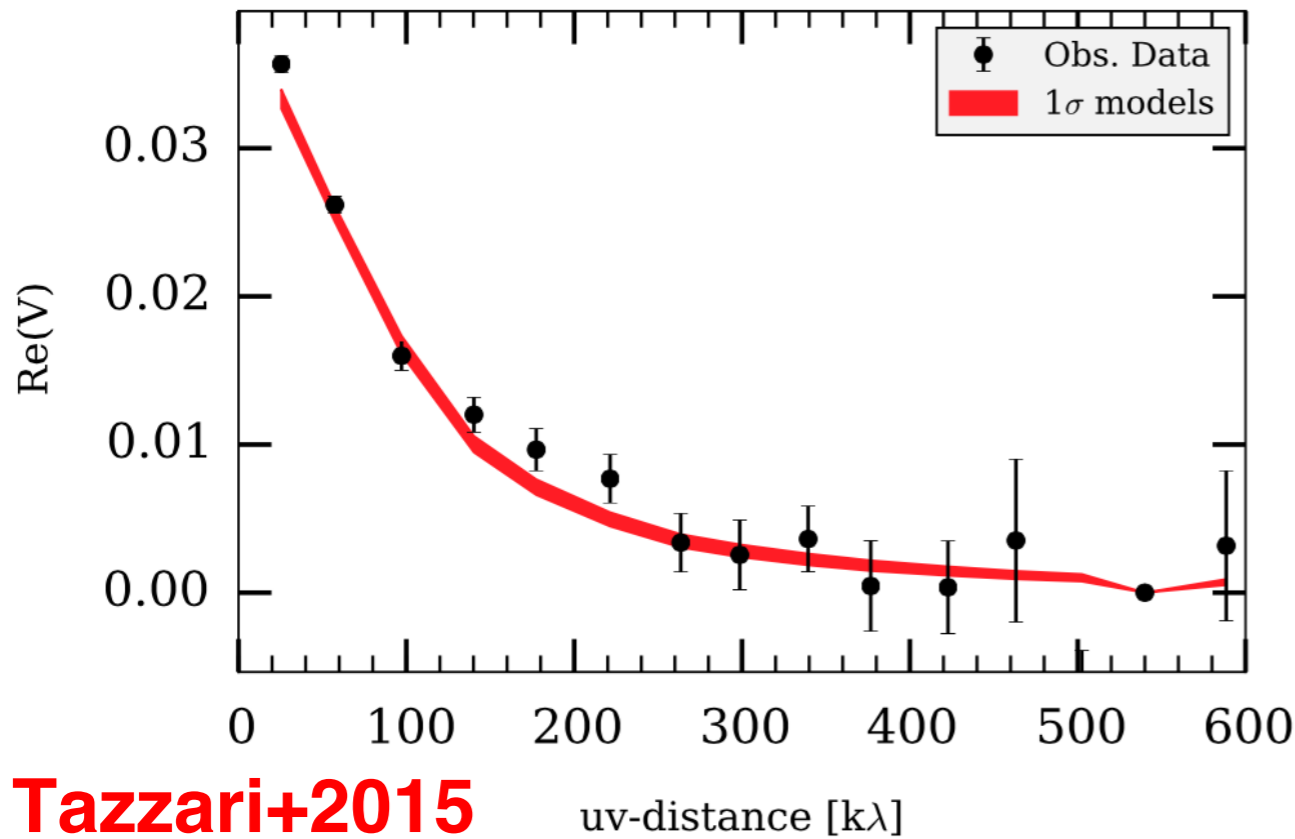
$P(x, y)$ = Antenna power pattern

$V(u, v)$ = Measured visibility

$I(x, y)$ = Brightness distribution on Sky

Analysis of interferometric data

2.8mm CARMA



$$\Sigma(R, t) = \Sigma_t \left(\frac{R_t}{R} \right)^\gamma \times \exp \left\{ -\frac{1}{2(2-\gamma)} \left[\left(\frac{R}{R_t} \right)^{(2-\gamma)} - 1 \right] \right\}$$

Bayesian Fitting Tool

Disk model

computes disk emission at different wavelengths

Fourier Transform

Synthetic visibilities

in the (u,v) plane sampled at the P.A.

Interferometric data

Visibilities in the (u,v) plane

posterior $\propto \exp(-\chi^2/2)$

- Models solve for the self consistent structure, given Sigma (and star)
- See also Isella+2007;2009

galario: a Gpu Accelerated Library for Analysing Radio Interferometry Observations

Marco Tazzari¹★, Frederik Beaujean² and Leonardo Testi^{2,3}

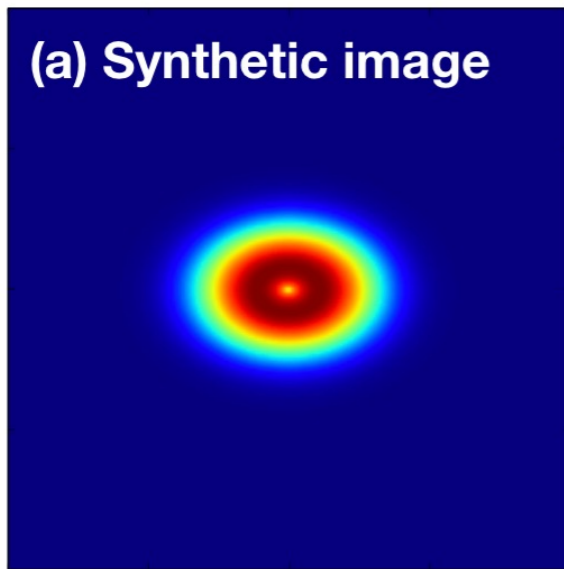
¹Institute of Astronomy, University of Cambridge, Madingley Road, CB3 0HA, Cambridge, UK

²Excellence Cluster Universe, Boltzmannstr. 2, D-85748 Garching, Germany

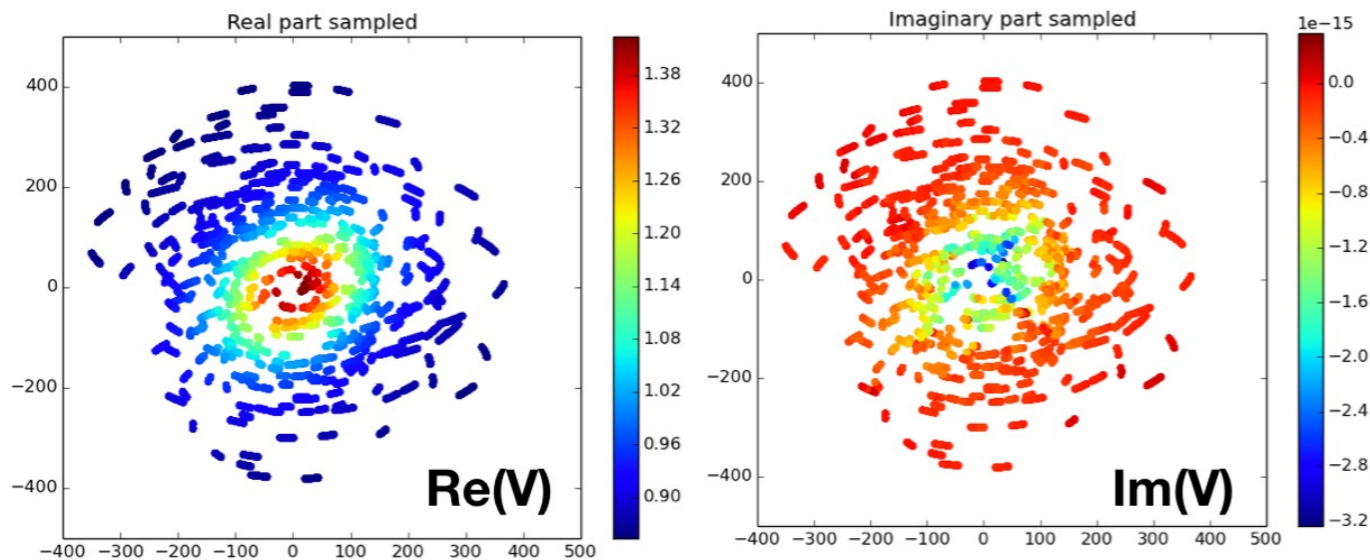
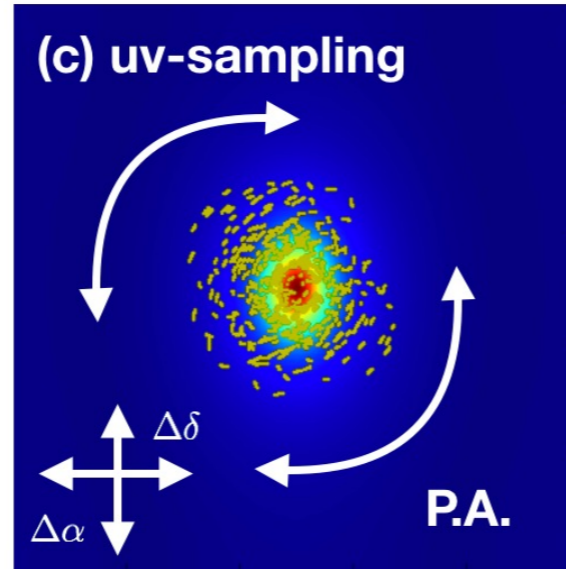
³European Southern Observatory, Karl Schwarzschild Str. 2, D-85748 Garching, Germany



(a) Synthetic image



(c) uv-sampling



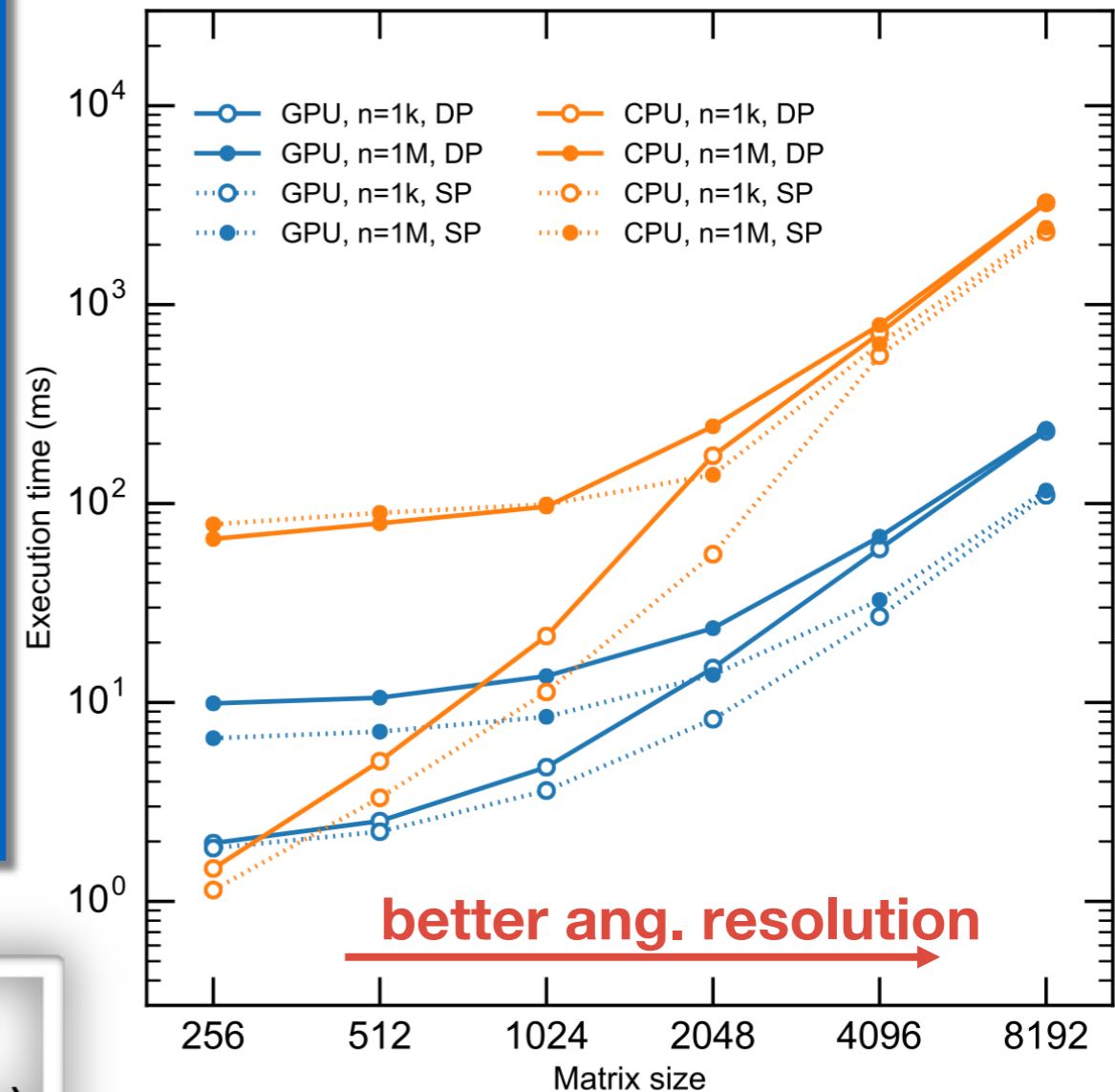
• example:

```
from galario import double_cuda, single_cuda
double_cuda.chi2(image, d_alpha, d_delta, uv, obs_vis)
```

visibility sampling)

is tools

<https://github.com/mtazzari/galario>



GALARIO: a GPU Accelerated Library for Analysing Radio Interferometry Observations



Marco Tazzari^{1*}, Frederik Beaujean² and Leonardo Testi^{2,3}

<https://github.com/mtazzari/galario>

► Easy to use:

- compute **visibilities** from 2D image:
- compute χ^2 from 2D image:
- compute χ^2 from 1D profile:

```
V_mod = sampleImage(image, dxy, u, v)
```

```
chi2 = chi2Image(image, dxy, u, v, ReV, ImV, w)
```

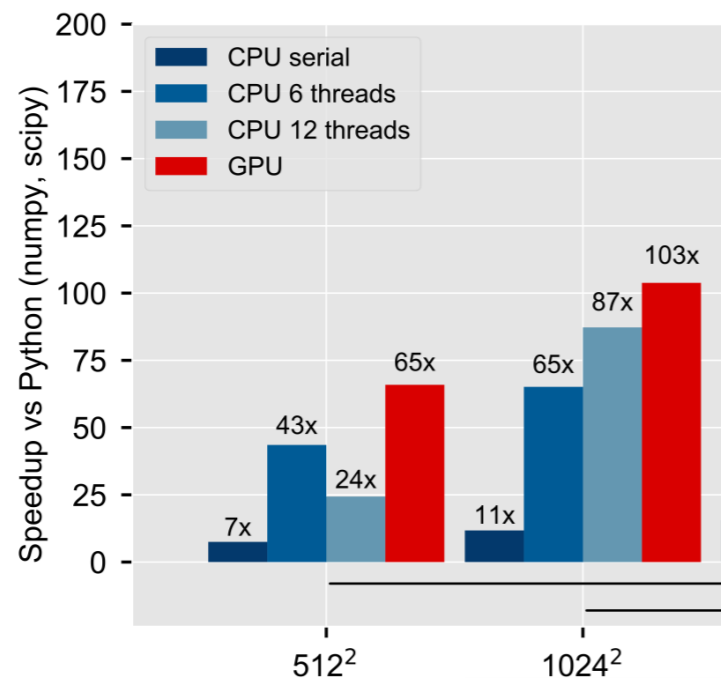
```
chi2 = chi2Profile(l, Rmin, dR, nxy, dxy, u, v, ReV, ImV, w)
```

► Easy to install:

```
conda install -c conda_forge galario
```

► *Fouriously* fast:

up to 150x faster than



► many applications:

- **protoplanetary** disks
- **debris** disks
- **high redshift** galaxies
- **massive** stars cores

► ready to exploit the ALMA wavelength coverage:

- **single**-wavelength continuum
- **multi**-wavelength continuum
- gas emission **spectral cubes**

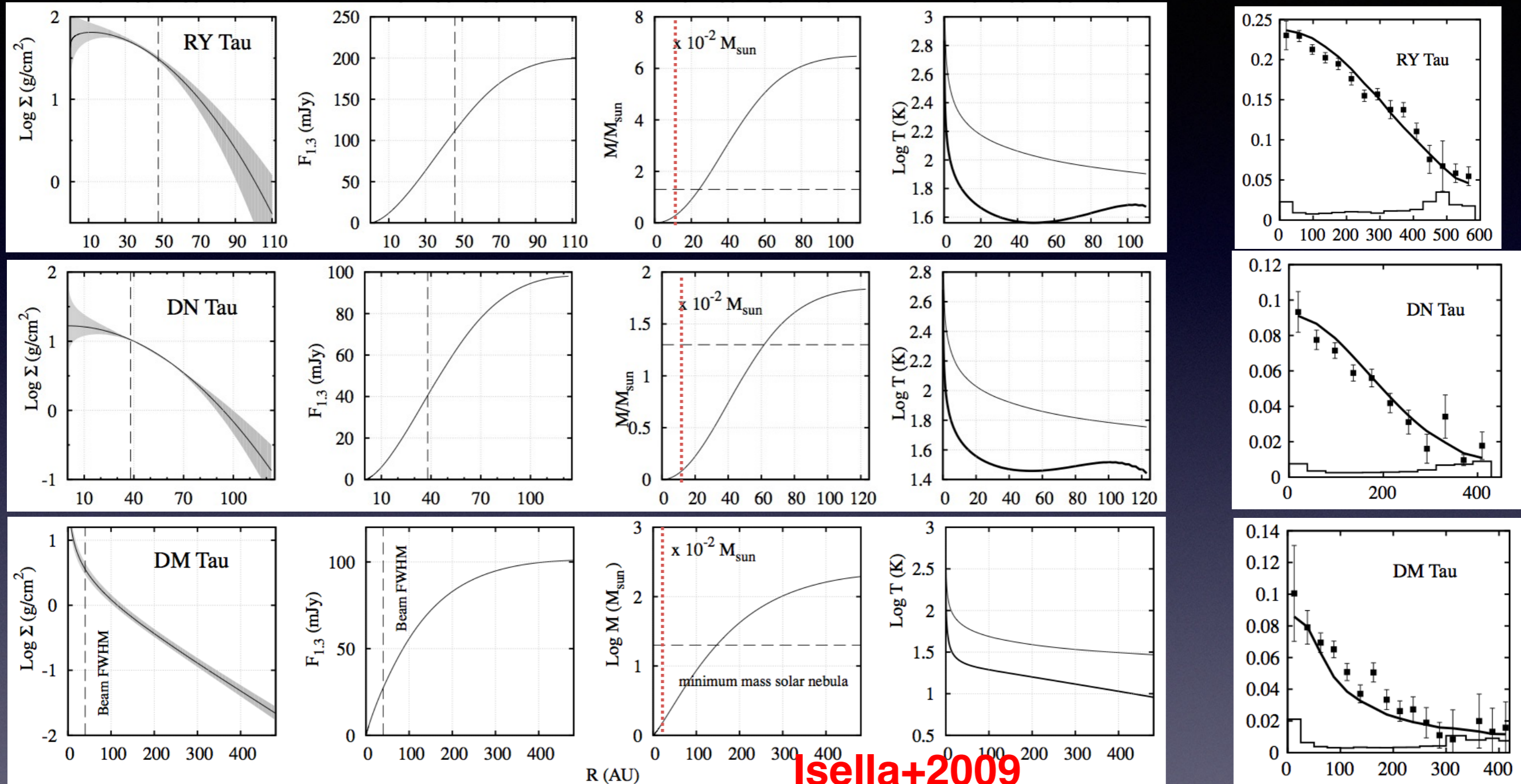
► single or multiple sources in the FOV

► fast enough for survey analysis

► Simple switch to GPU:

```
import galar
```

Examples of pre-ALMA results

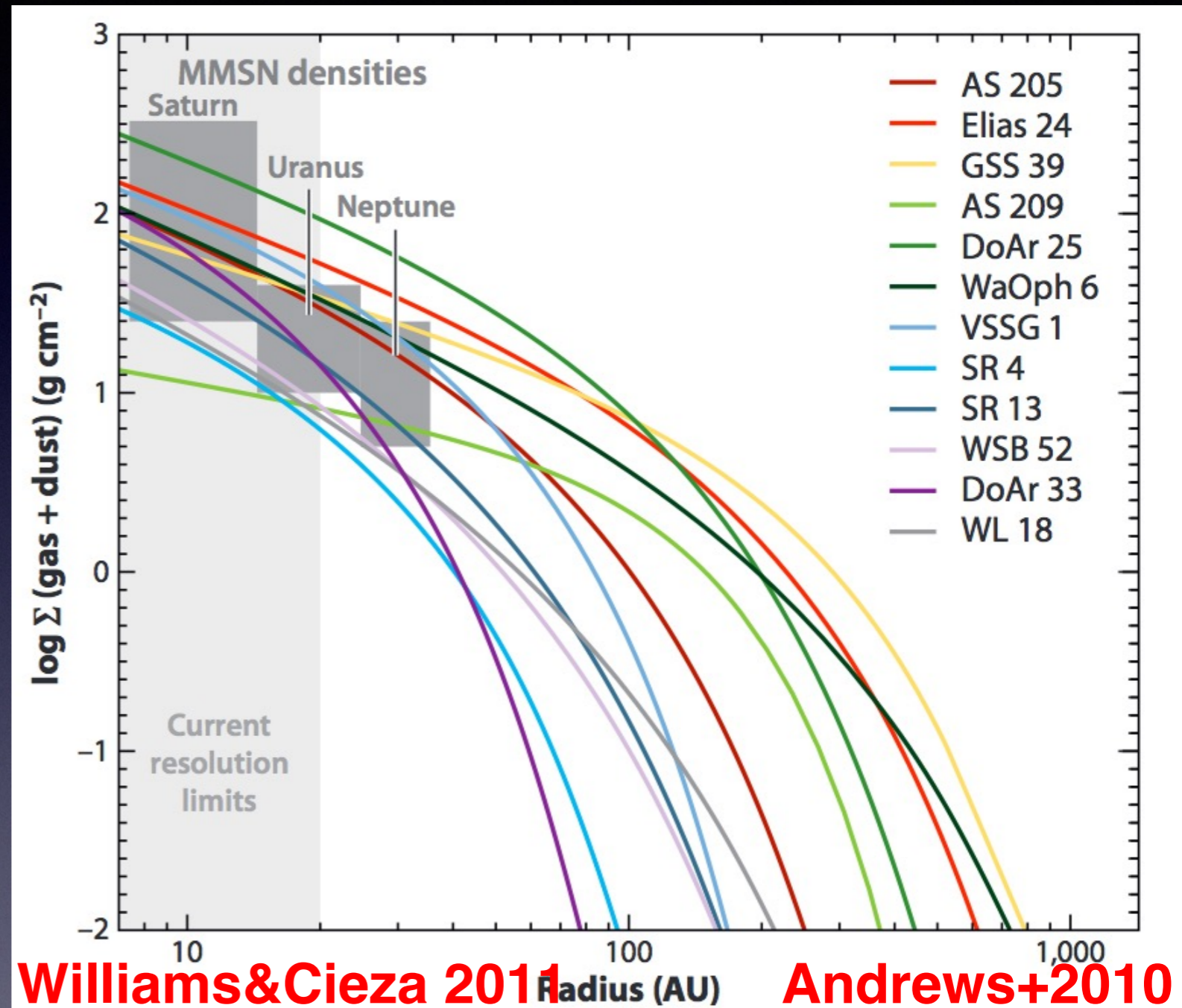
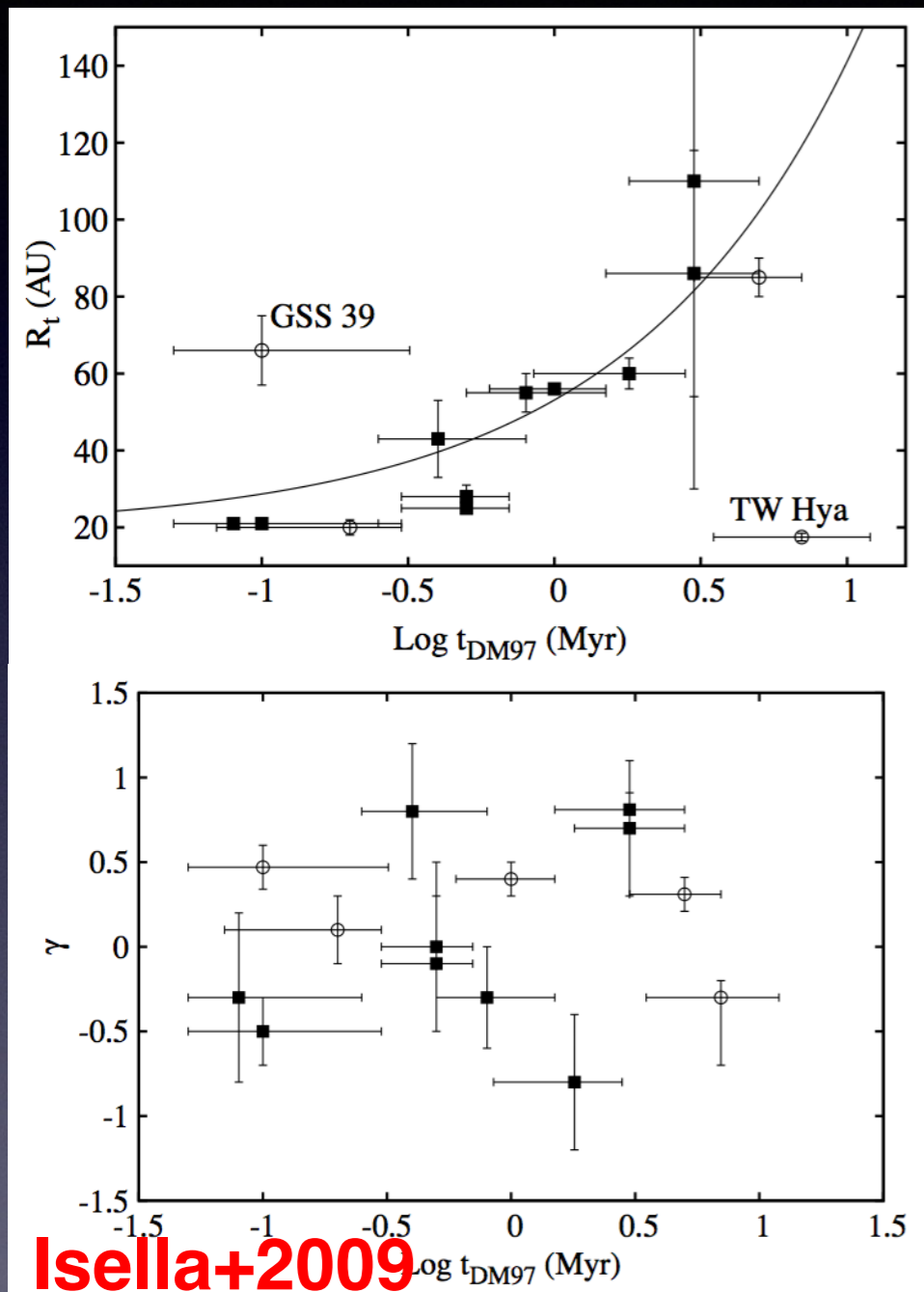


Isella+2009

$$\Sigma(R, t) = \Sigma_t \left(\frac{R_t}{R} \right)^\gamma \times \exp \left\{ -\frac{1}{2(2-\gamma)} \left[\left(\frac{R}{R_t} \right)^{(2-\gamma)} - 1 \right] \right\}$$

- Data generally well described, note limited angular resolution

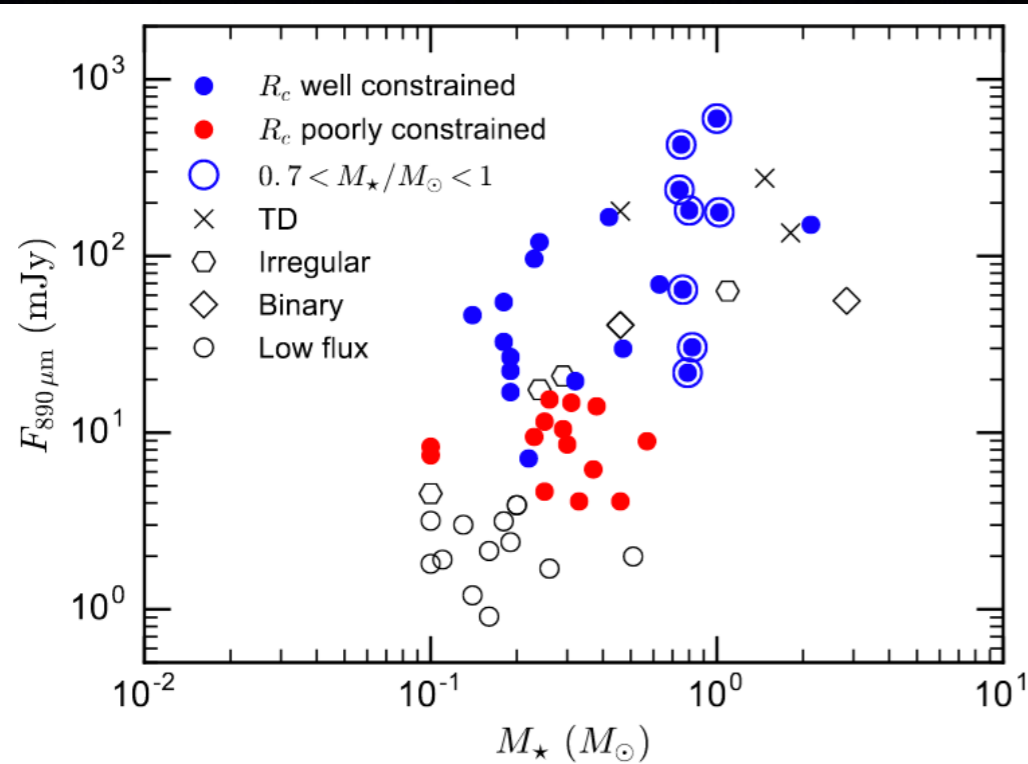
Examples of pre-ALMA results



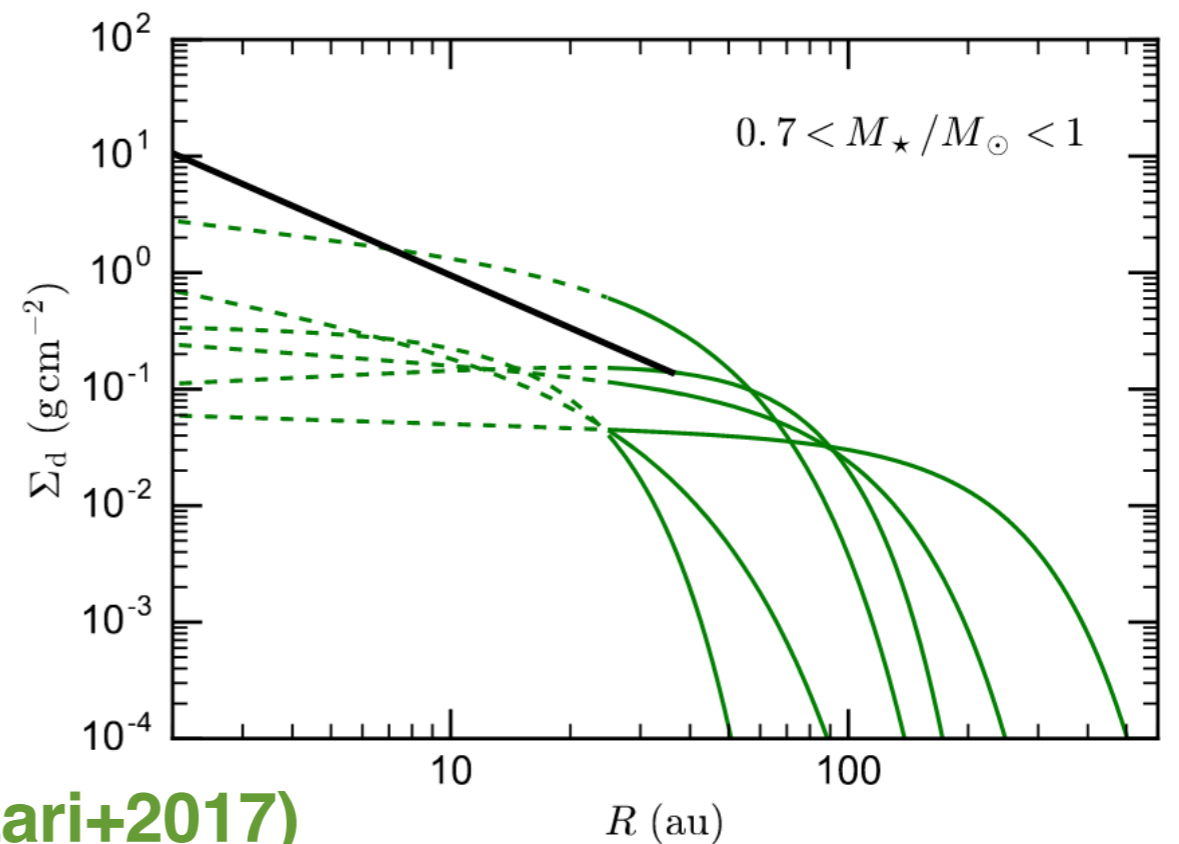
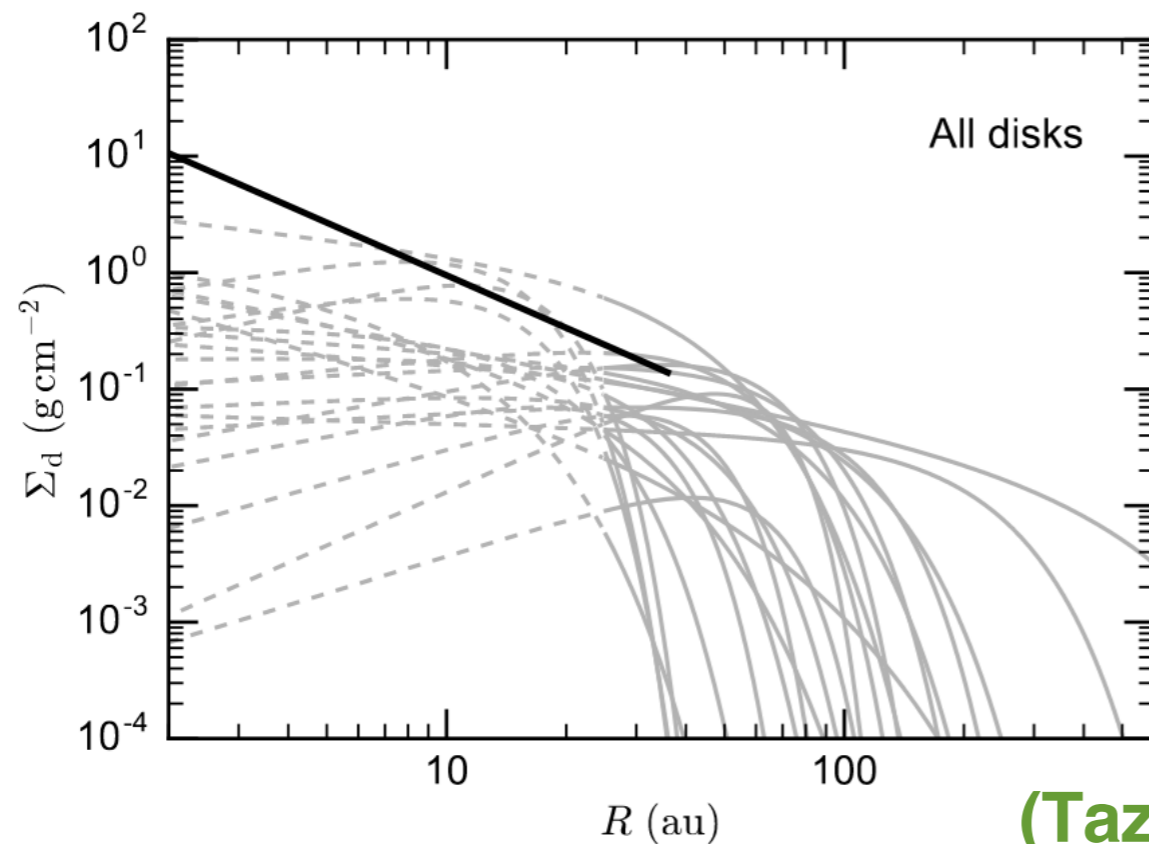
- Extract N random samples from “Taurus” applying the same selection biases as expected in the other region. Method first applied by Andrews+2013

Surface density distribution

Powered by
Galaro
(Tazzari+2018)



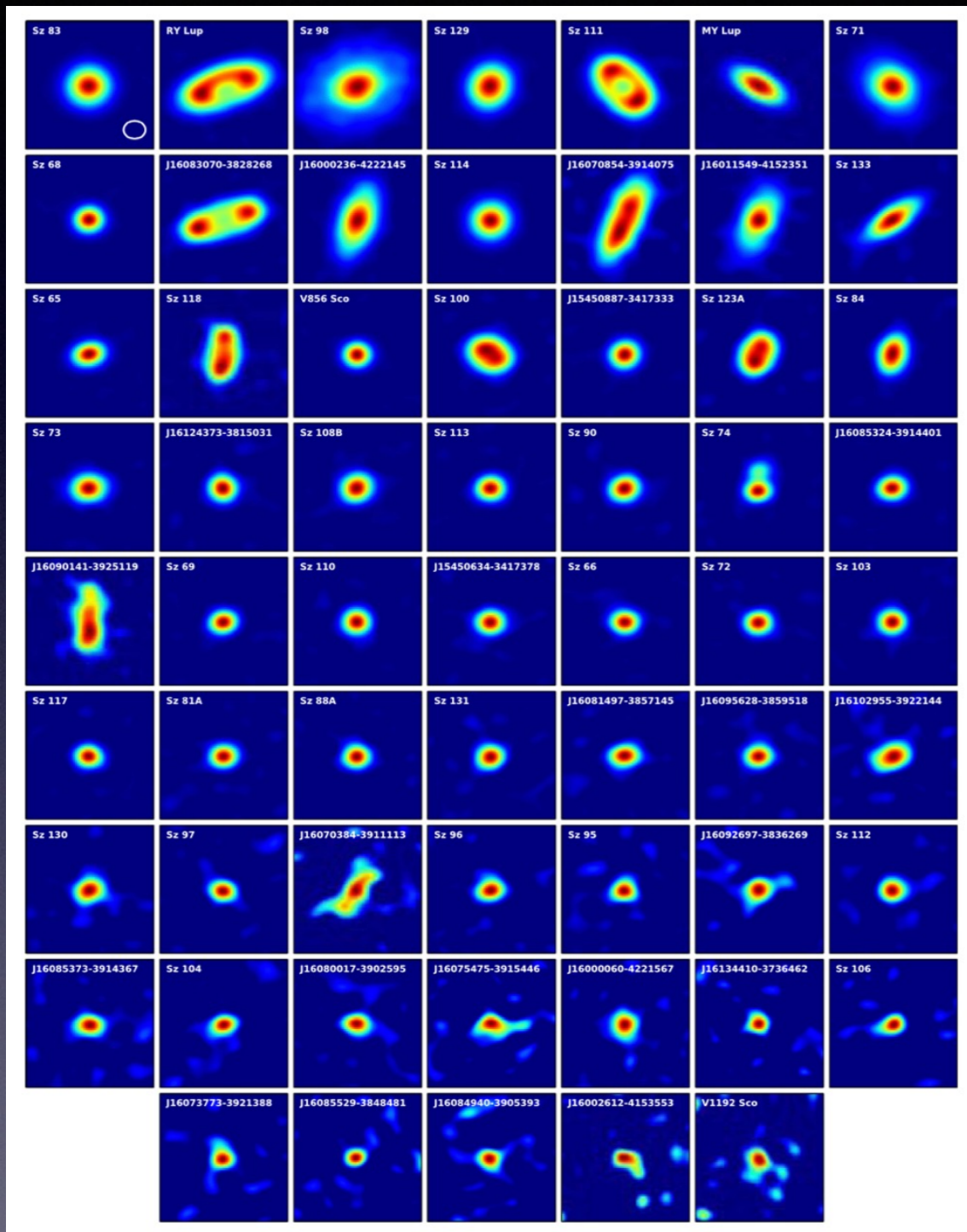
- First systematic/complete analysis of surface density distribution of solids in disks
- Compact disks ($R < 50 \text{ AU}$) are up to $\sim 30\text{-}40\%$ of the population



(Tazzari+2017)

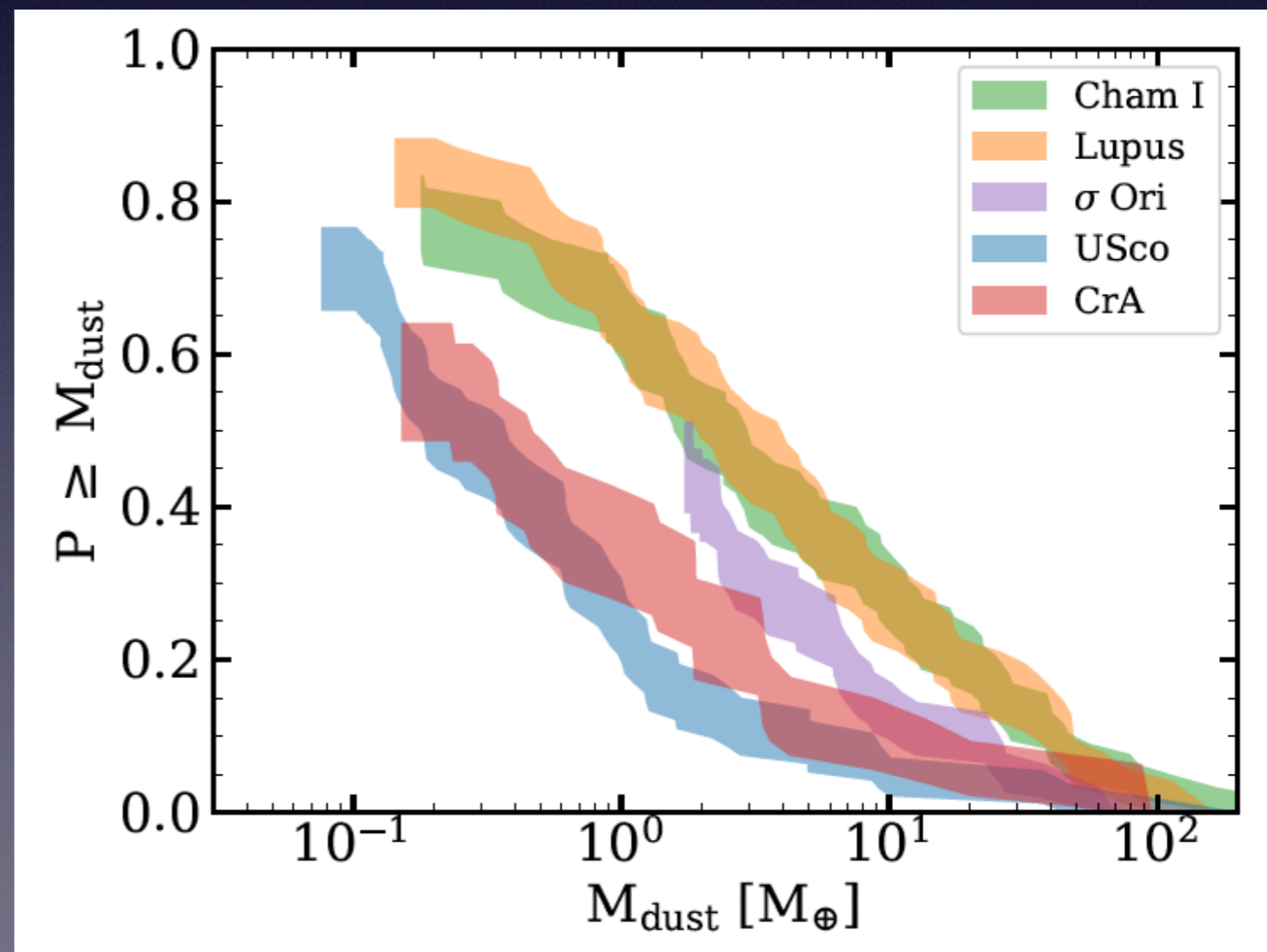
Full fit not always possible: order of magnitude estimates technique

- Initial surveys revealed a gradual decay (factor ~ 4 in ~ 5 Myr)
- Dust content is relatively low
- Estimates rely on simple assumption on temperature structure and dust opacity

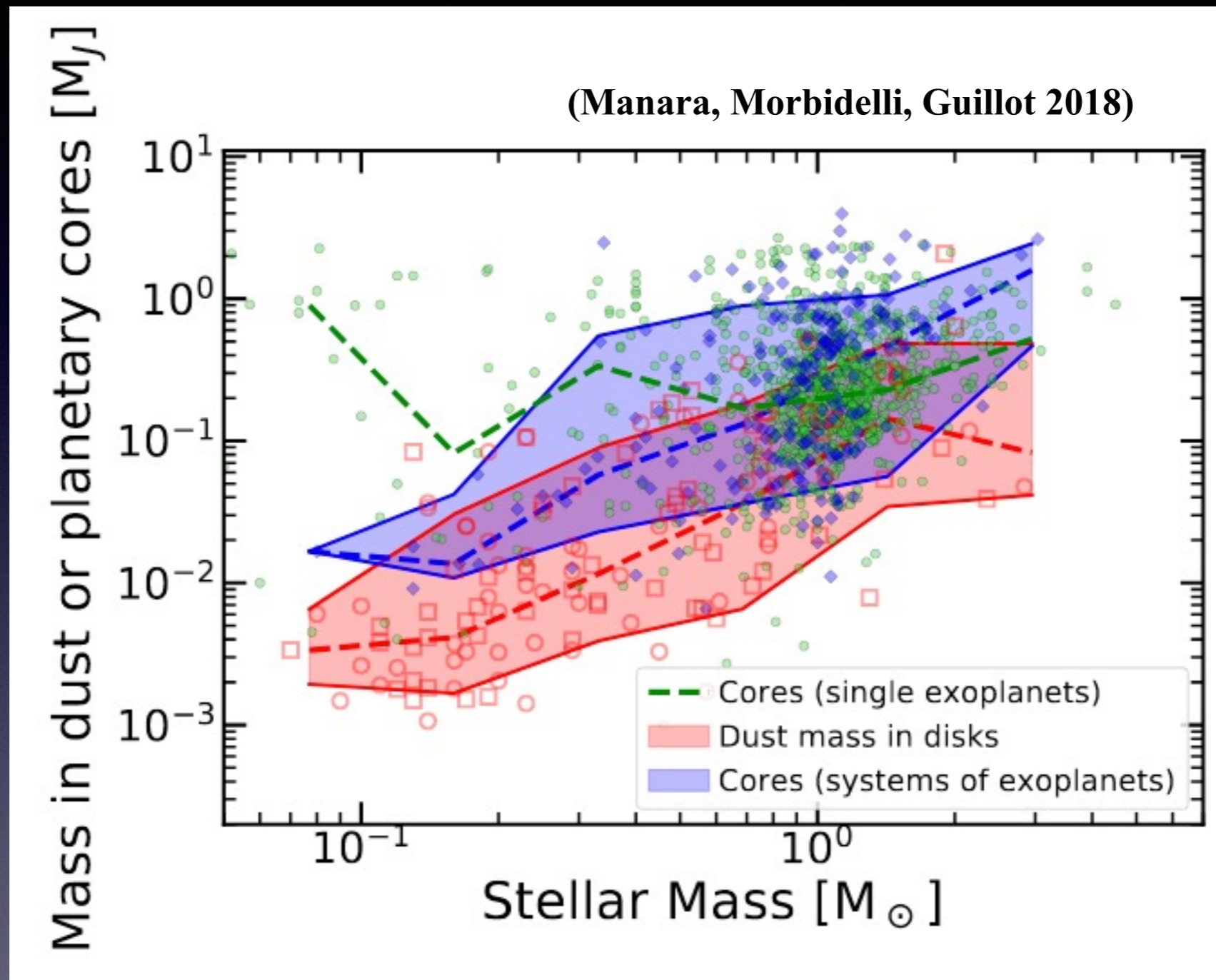


Andsell+2016

(see also Pascucci+2016, Andsell+2017, Barenfeld+2016, Cazzoletti+2019, Williams+2019, Testi+2022)

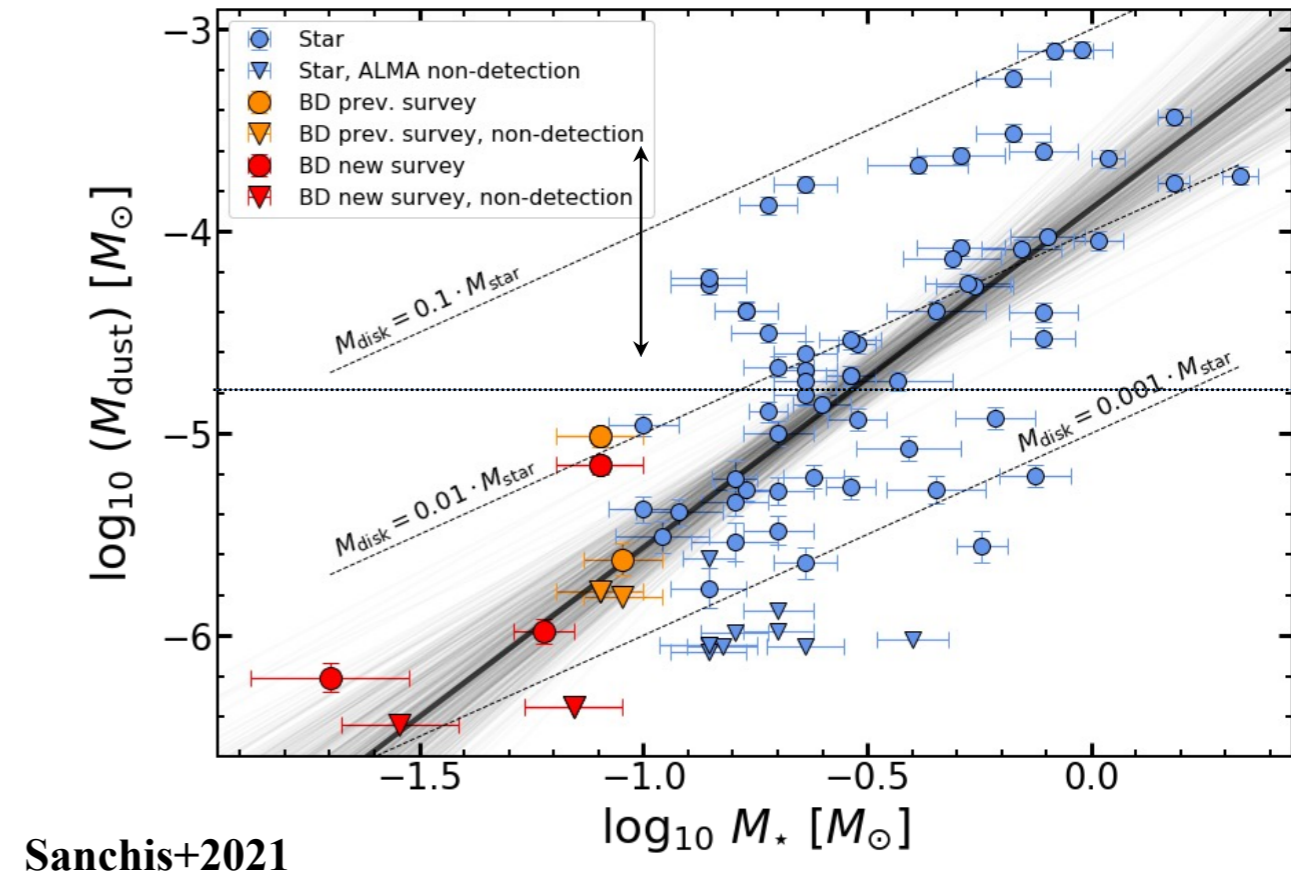
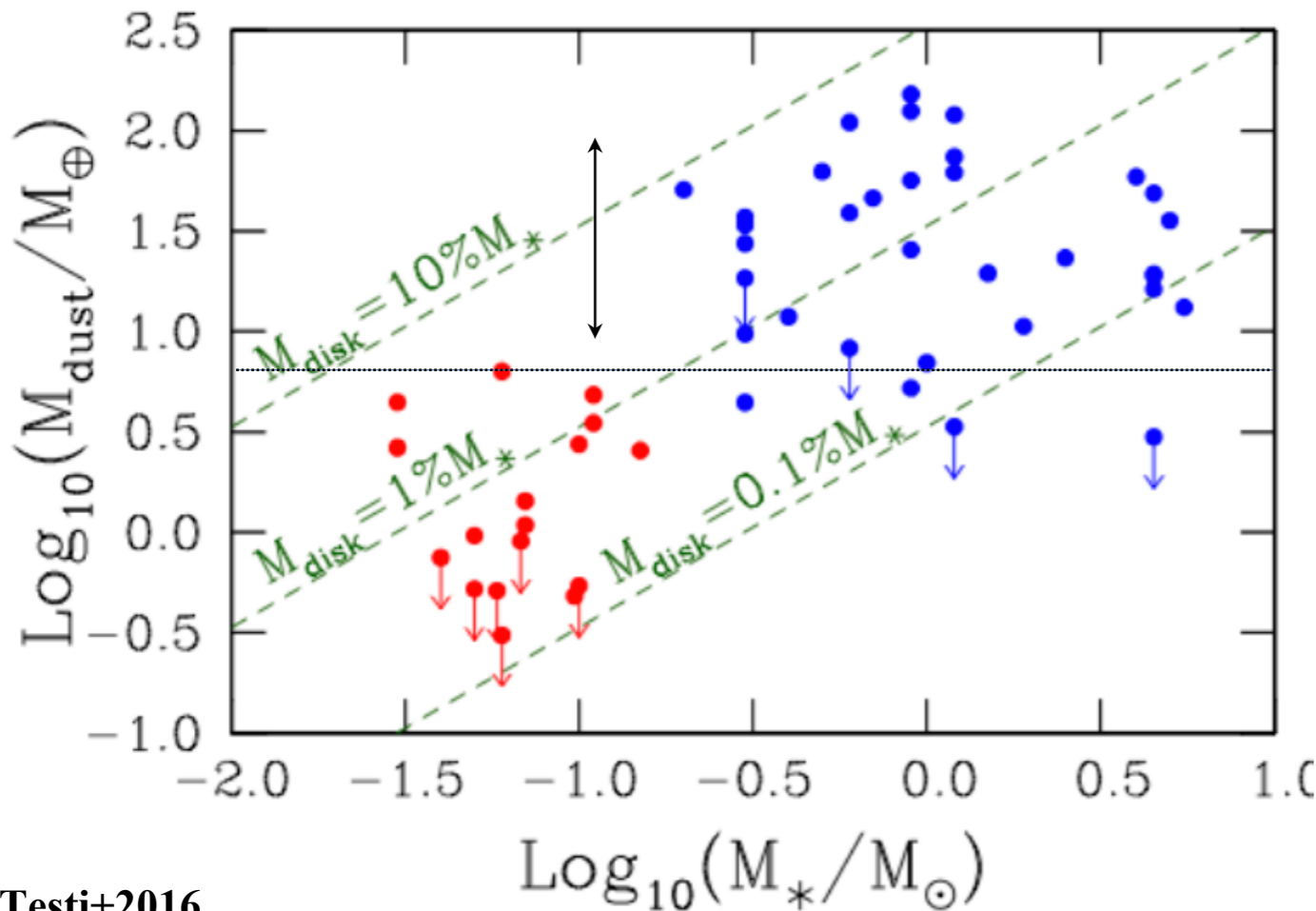


Solids in planets and disks



- 1-2Myr old disks do not contain enough solids
 - Consistent with the latest suggestions of Jupiter core growth (Kruijer+2017)

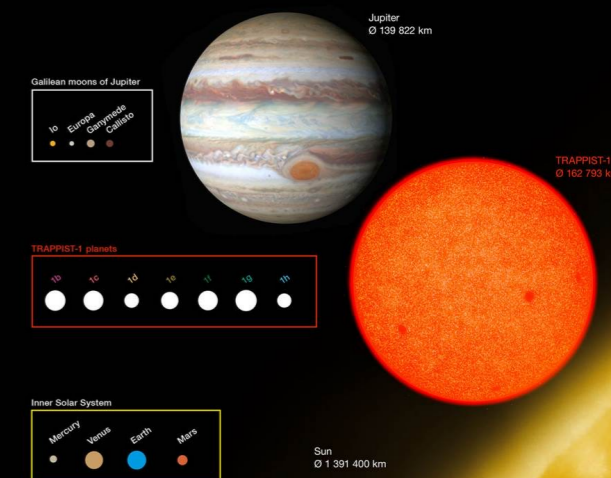
Deficit of solids in BD disks



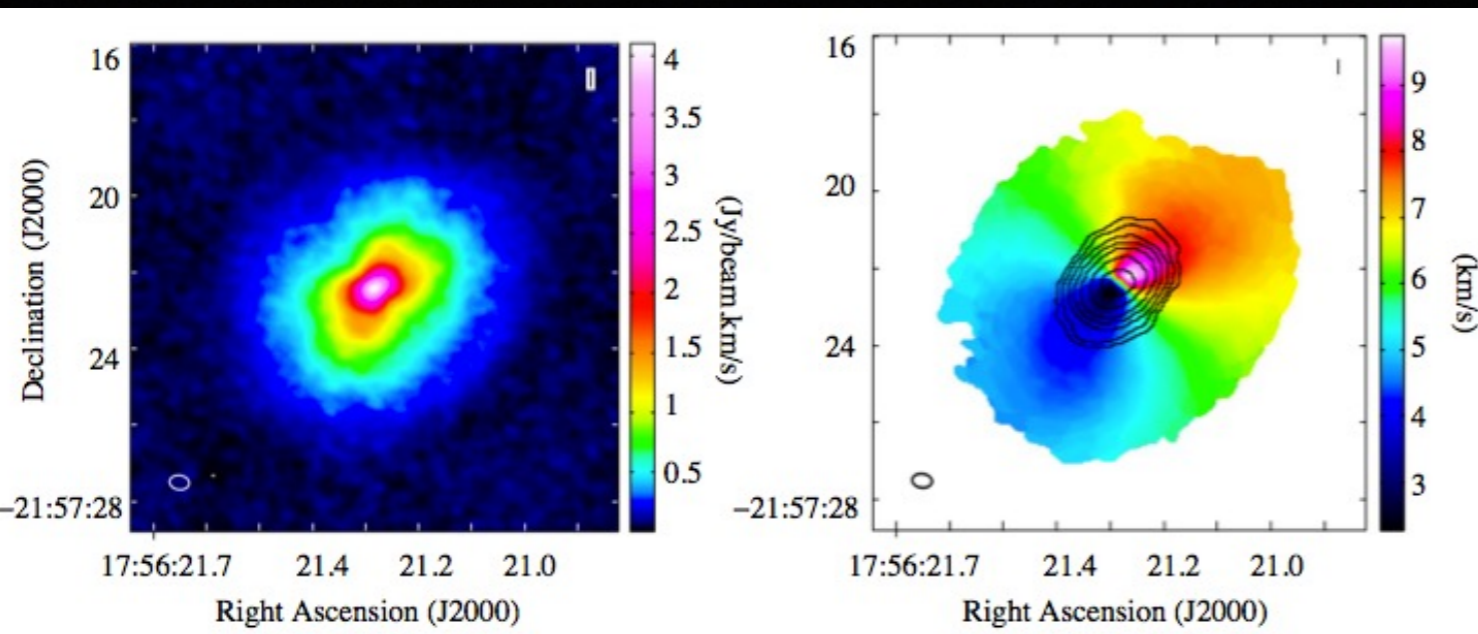
- Estimated solids mass in BD disks is too low to form the known exoplanets around BDs

Size Comparison

between TRAPPIST-1 system, Galilean moons of Jupiter and the inner Solar System

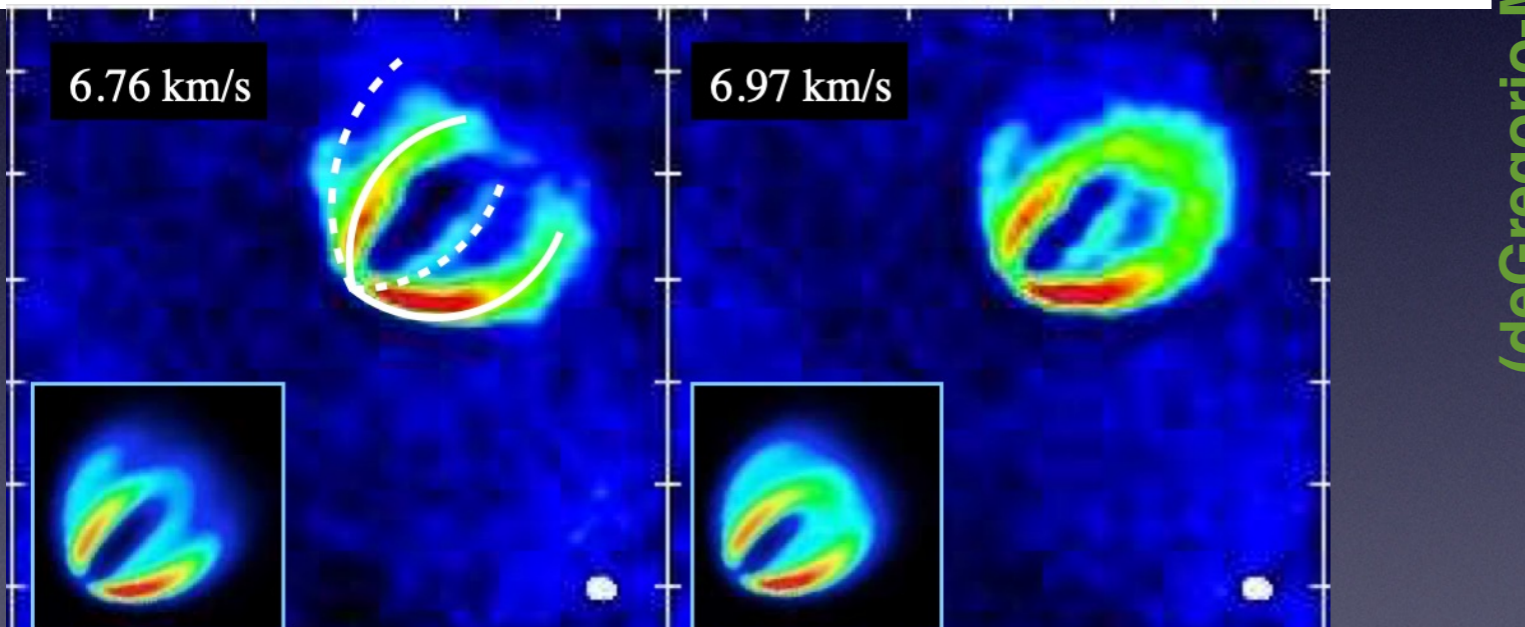


HD 163296 as seen by ALMA

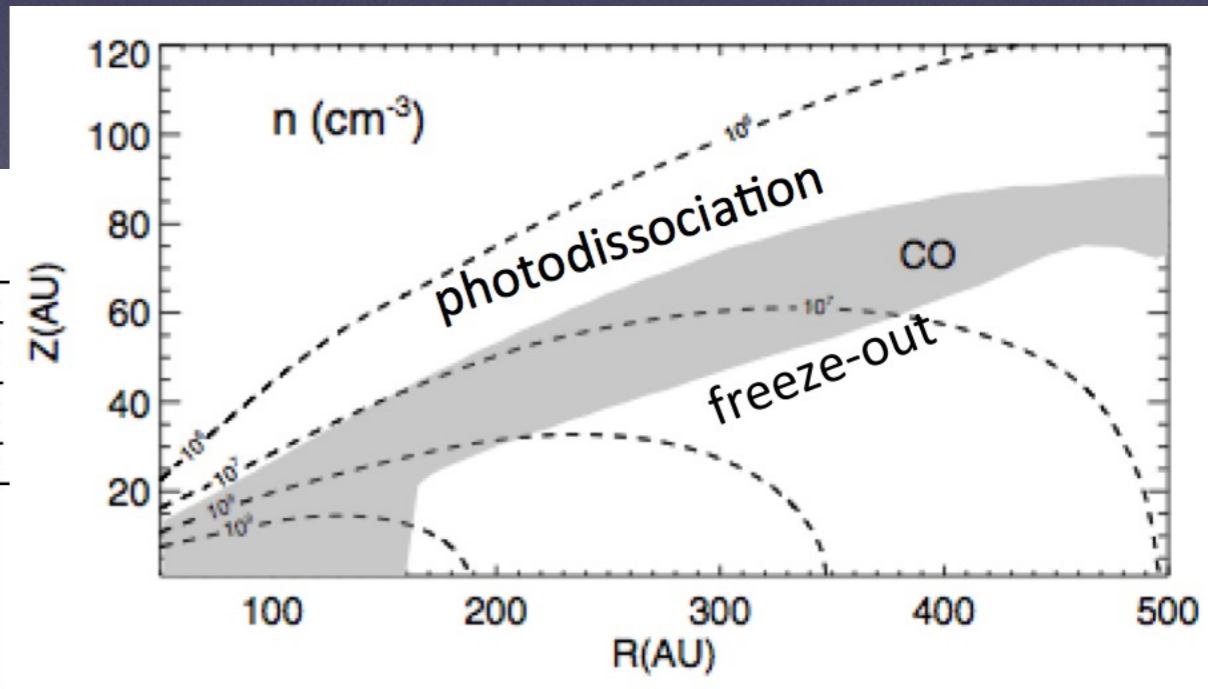
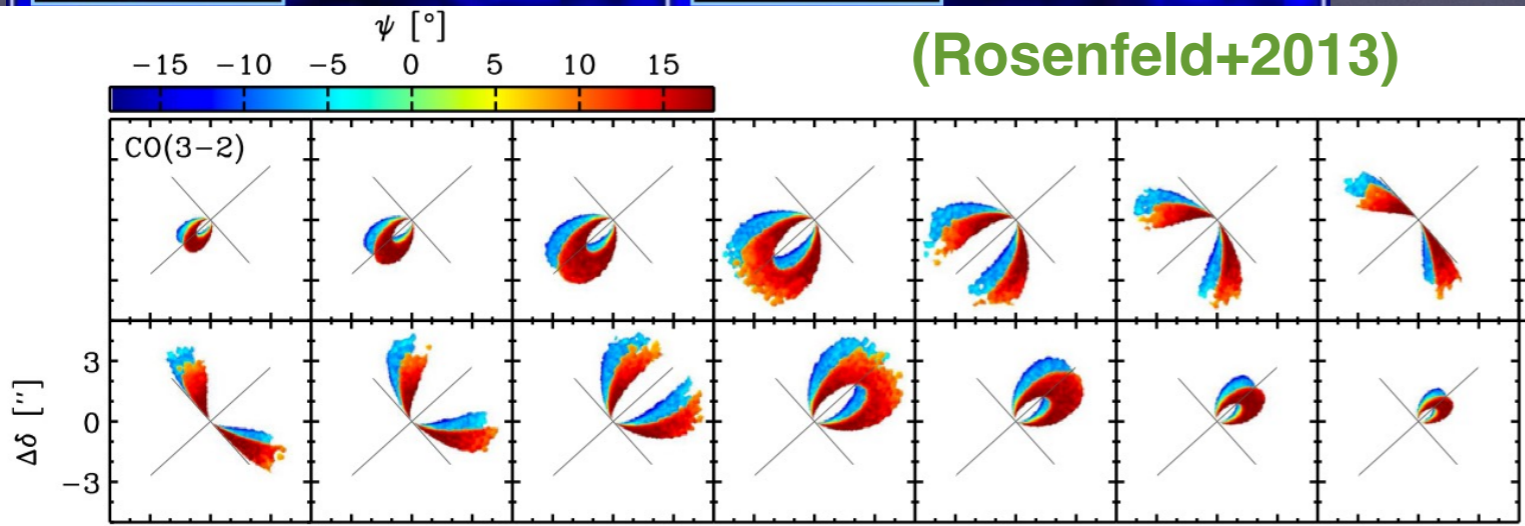


(deGregorio-Monsalvo+2013)

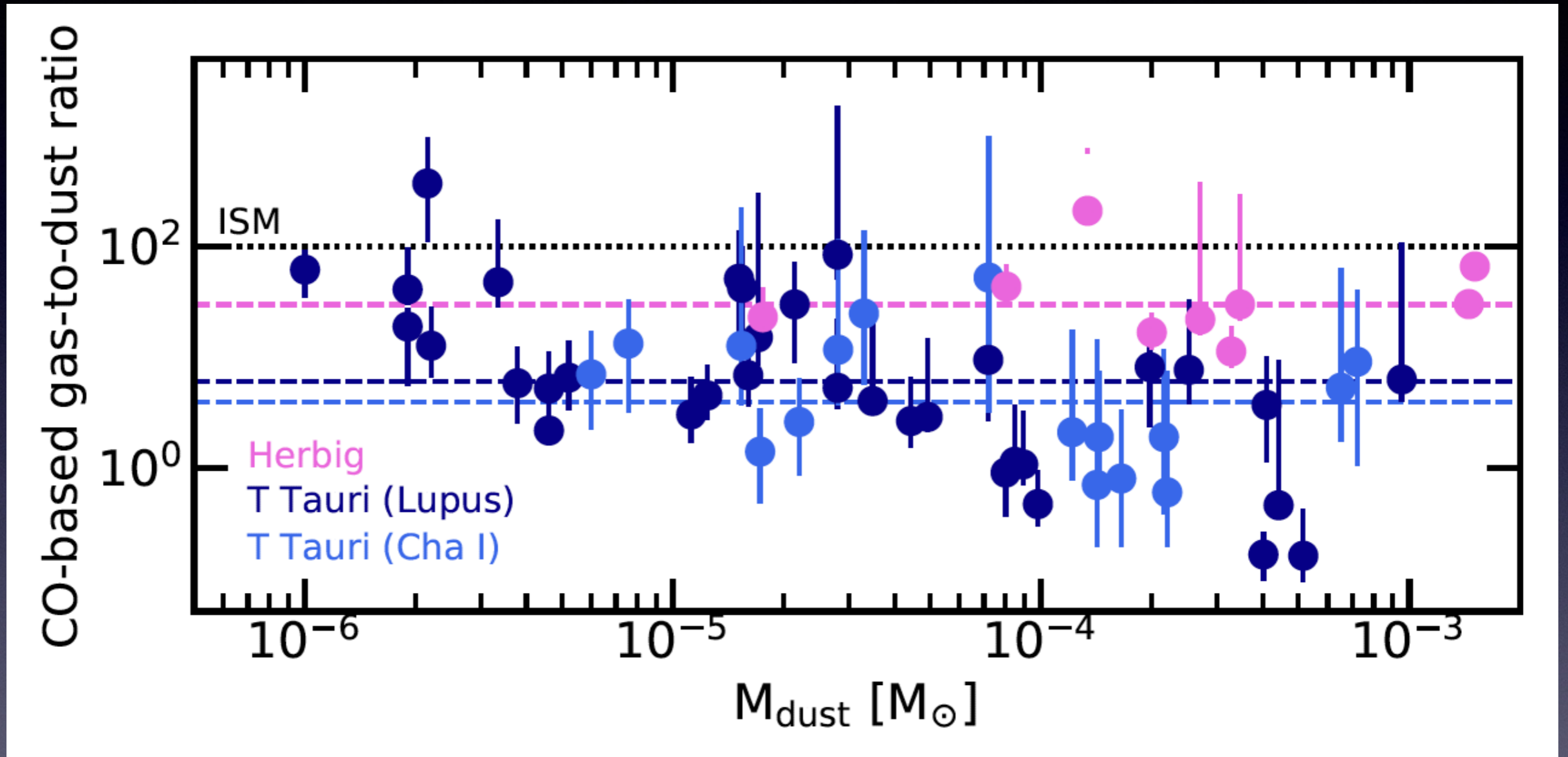
- Direct measurement of disk flaring and CO depletion on the mid plane



(Rosenfeld+2013)



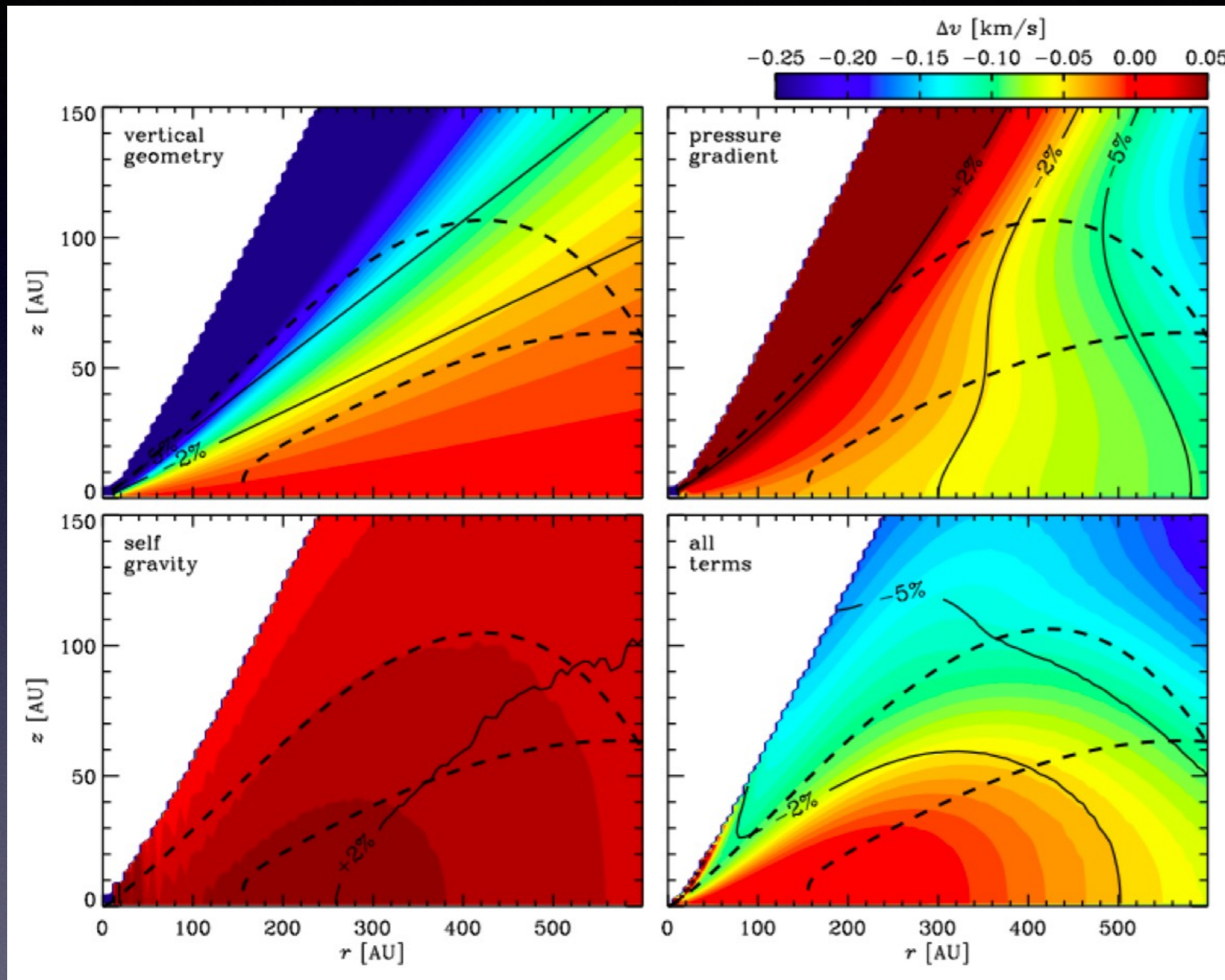
CO-based gas masses



(Miotello et al. 2022)

- Based on disk thermochemical modelling
- Truly low gas masses or “chemical” model deficit?

Gas kinematics



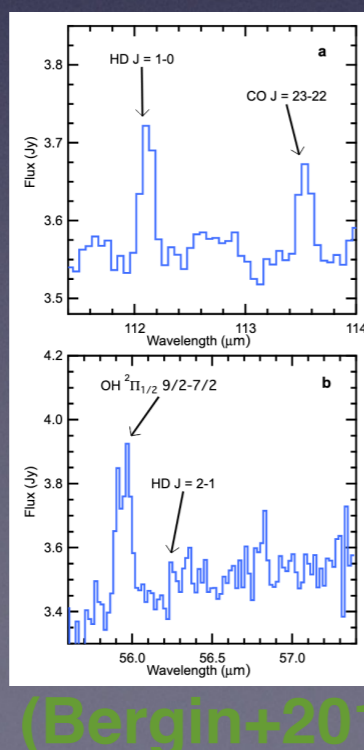
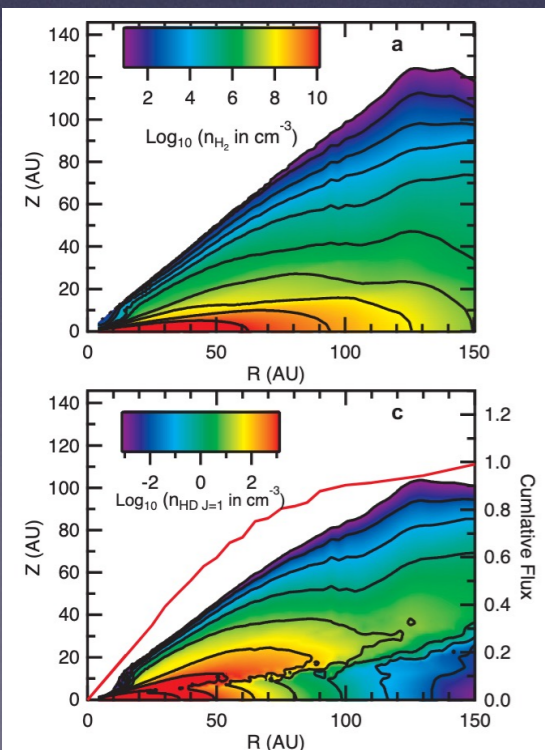
- Potentially a direct measurement of the disk self-gravity

(Rosenfeld et al. 2013)

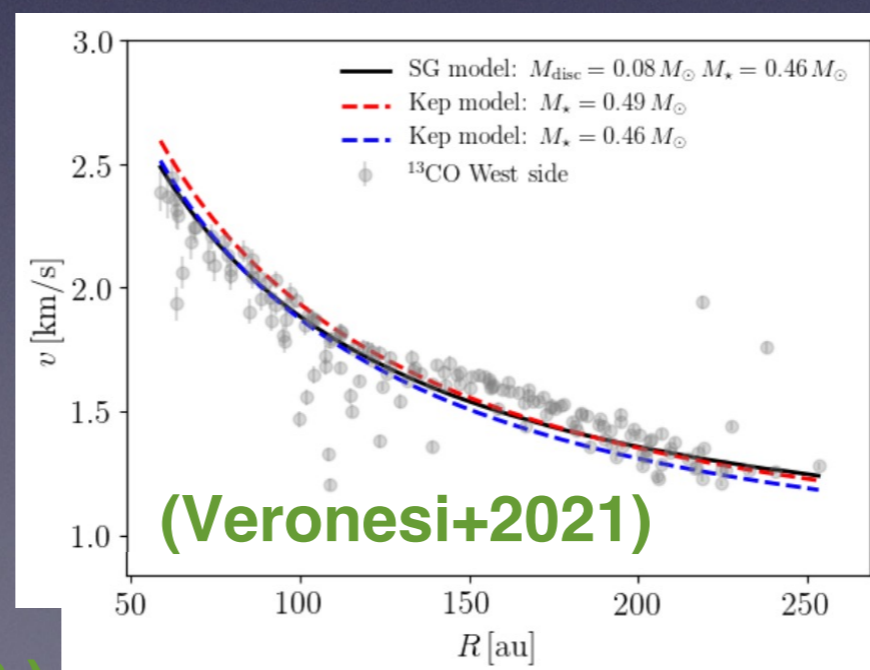
- Not exactly Keplerian
- Largest effect is the pressure term 5%, self gravity 0.1-0.5%

Dust mass and disk mass

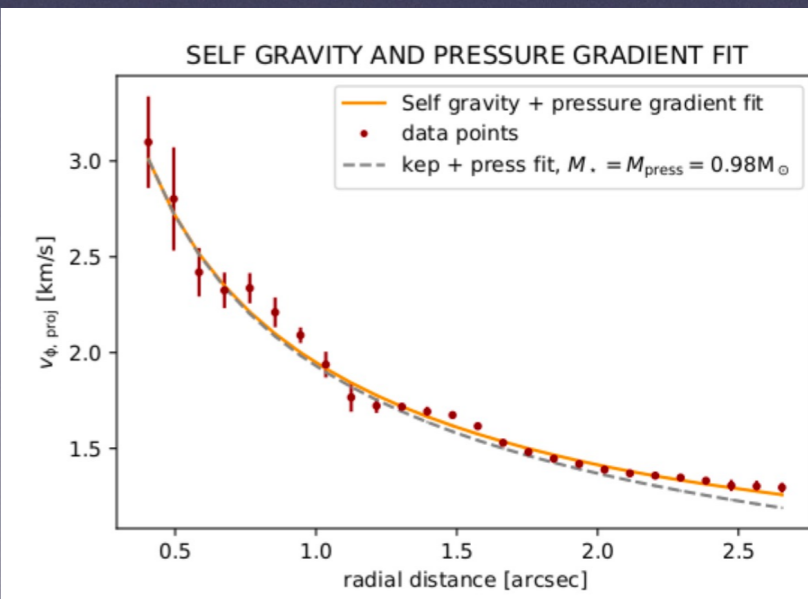
- Dust emission traces approx 0.01 of the H₂ mass
 - (by comparison, gas-phase CO emission traces $\llll 1e-5$, depending on how much of the CO mass is in solids and on the details of chemistry and photodissociation)
- Carefully estimated dust masses are within a factor 2-3 of “robust” disk mass estimates



(Bergin+2013)

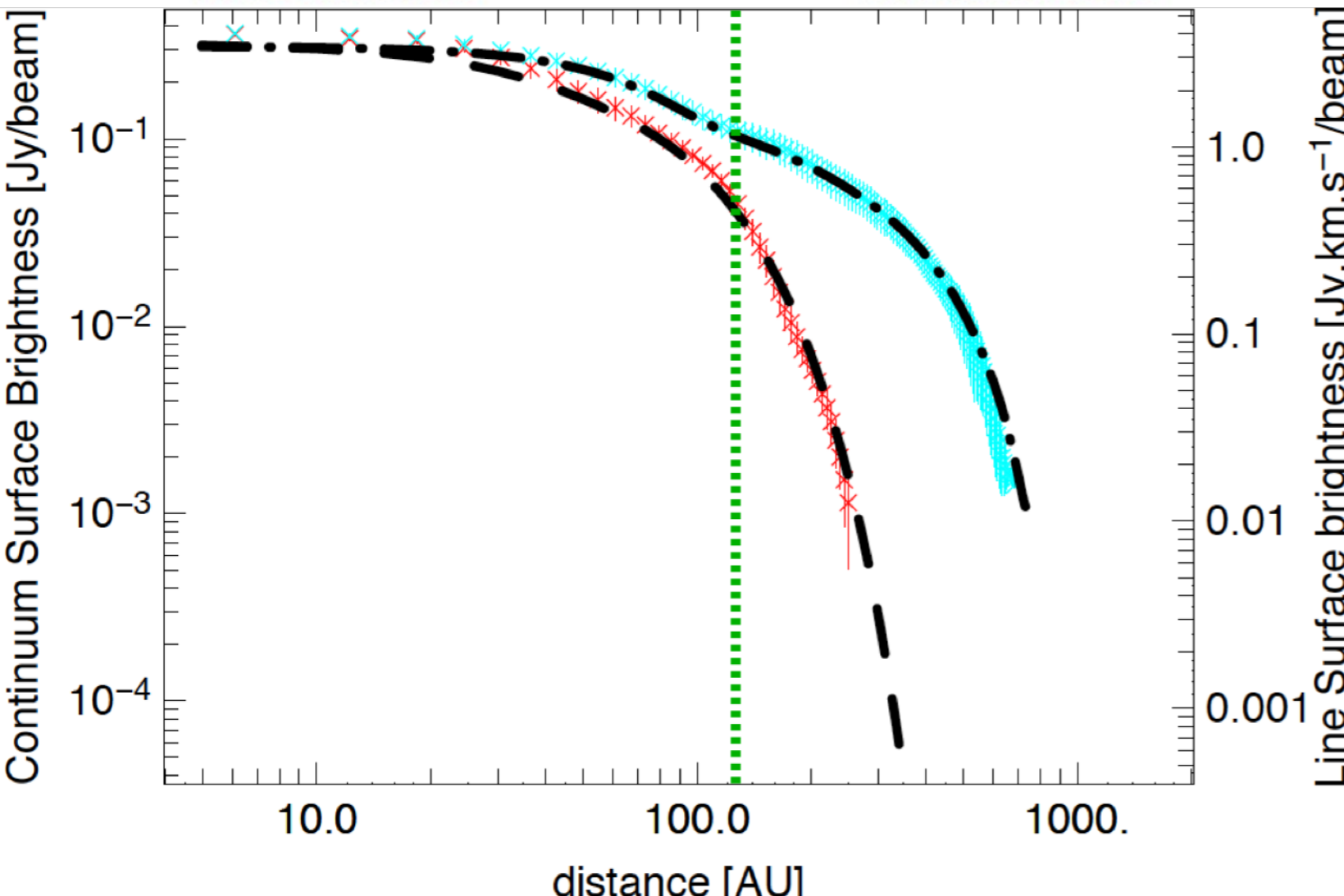
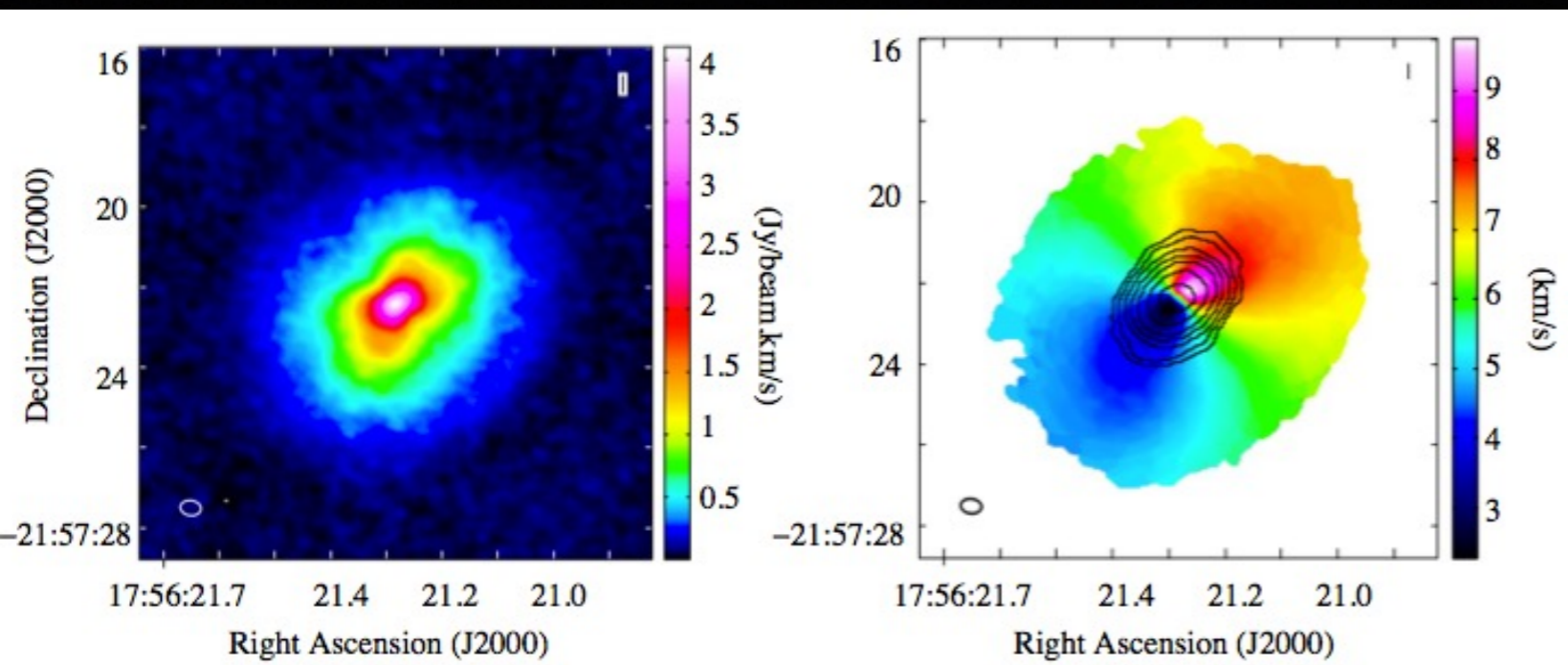


(Veronesi+2021)

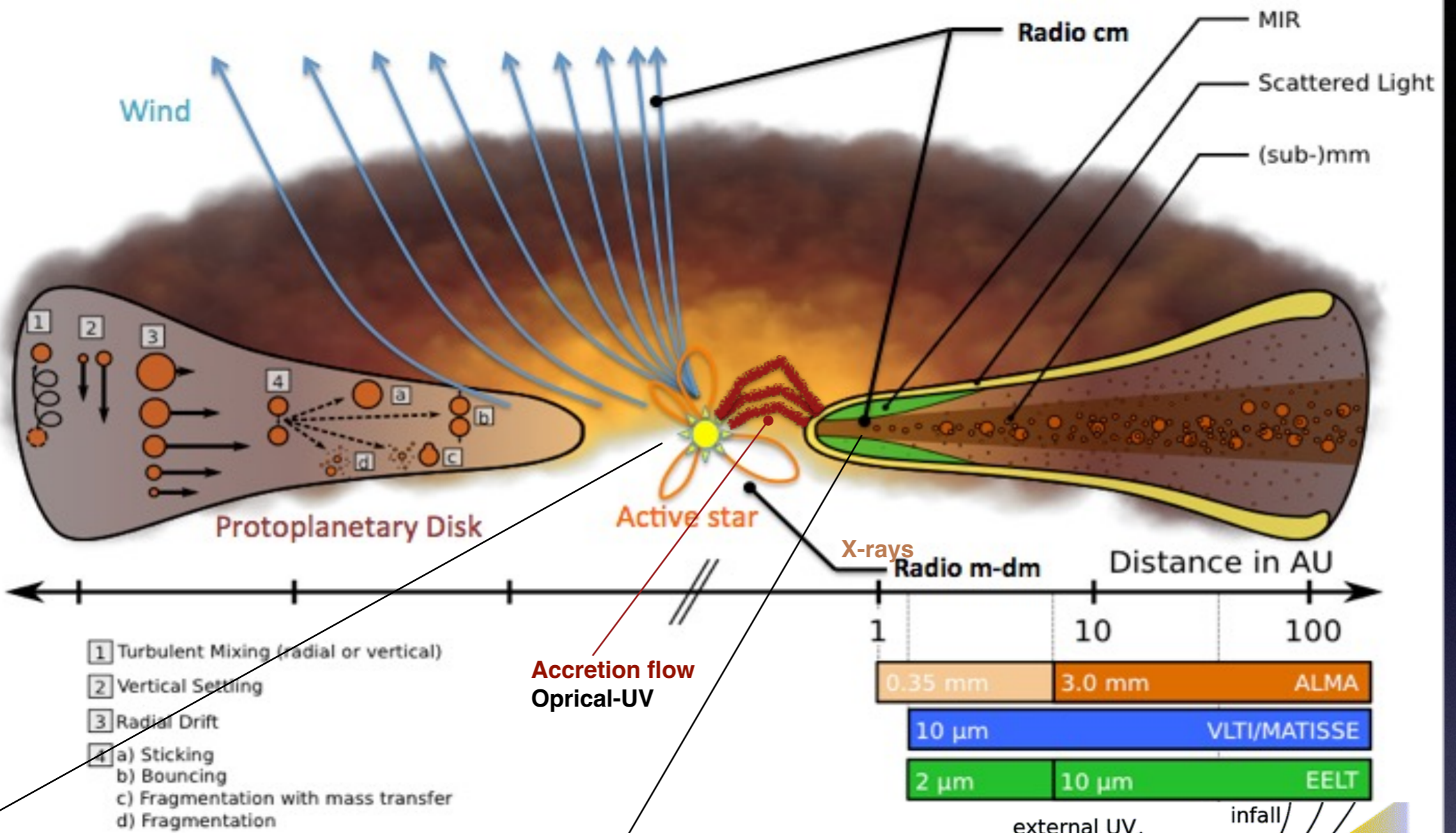


(Rampinelli+2022)

HD 163296 as seen by ALMA



- Extent of the CO disk is much larger than that of the mm-grains disk
- Qualitative behaviour as expected from viscous spreading and migration of the larger grains



Testi et al. 2014/15

