

# Protoplanetary Disks

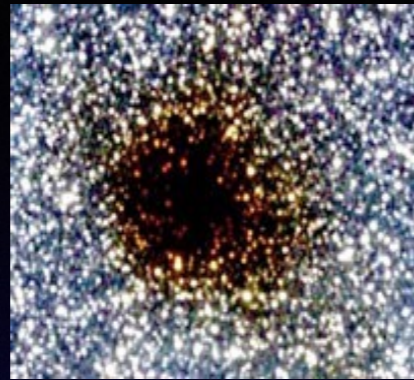
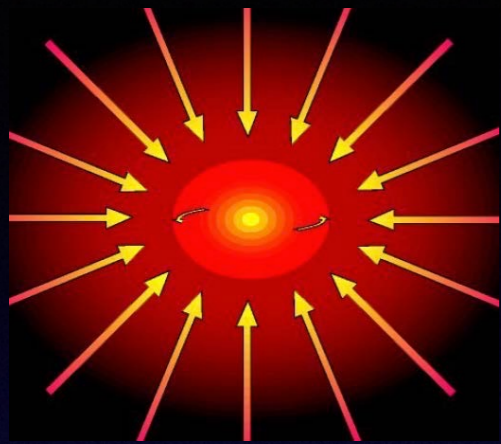
(the dirty job part II)

Leonardo Testi - UniBo  
[leonardo.testi@unibo.it](mailto:leonardo.testi@unibo.it)

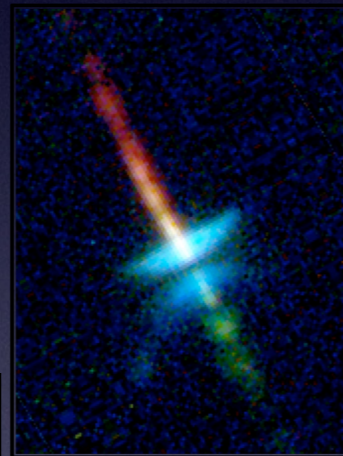
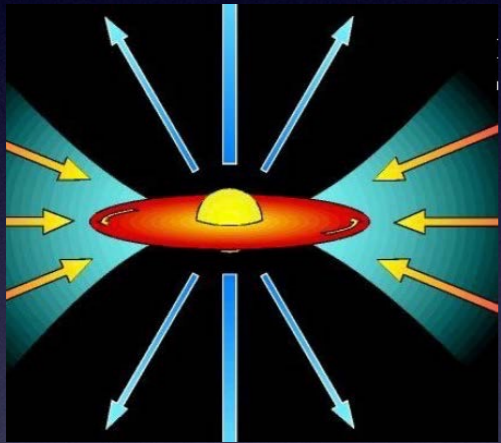
- Most of the focus will be on Class II disks
- How we determine the key properties of these systems
- Stellar masses and ages
- Disk physical parameters
- Evolution of the disk and its constituents



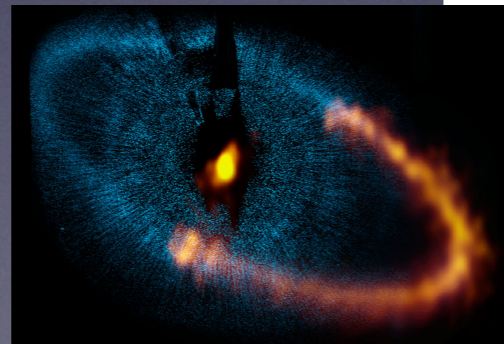
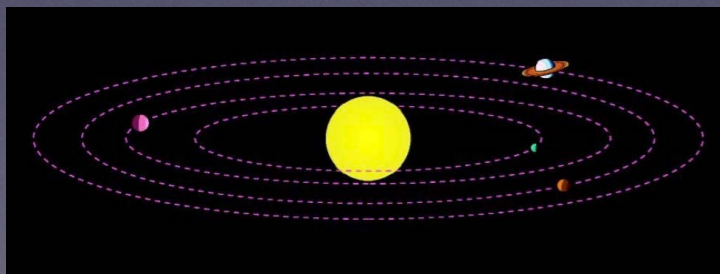
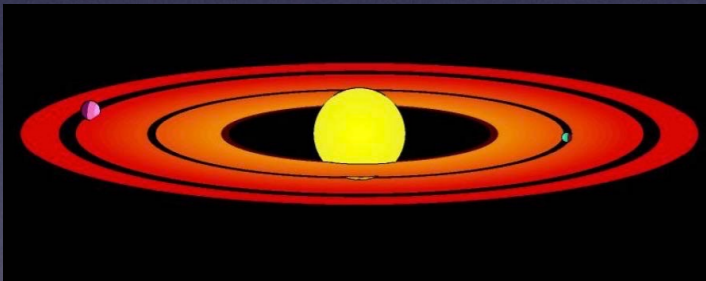
# From Cores to Planetary Systems



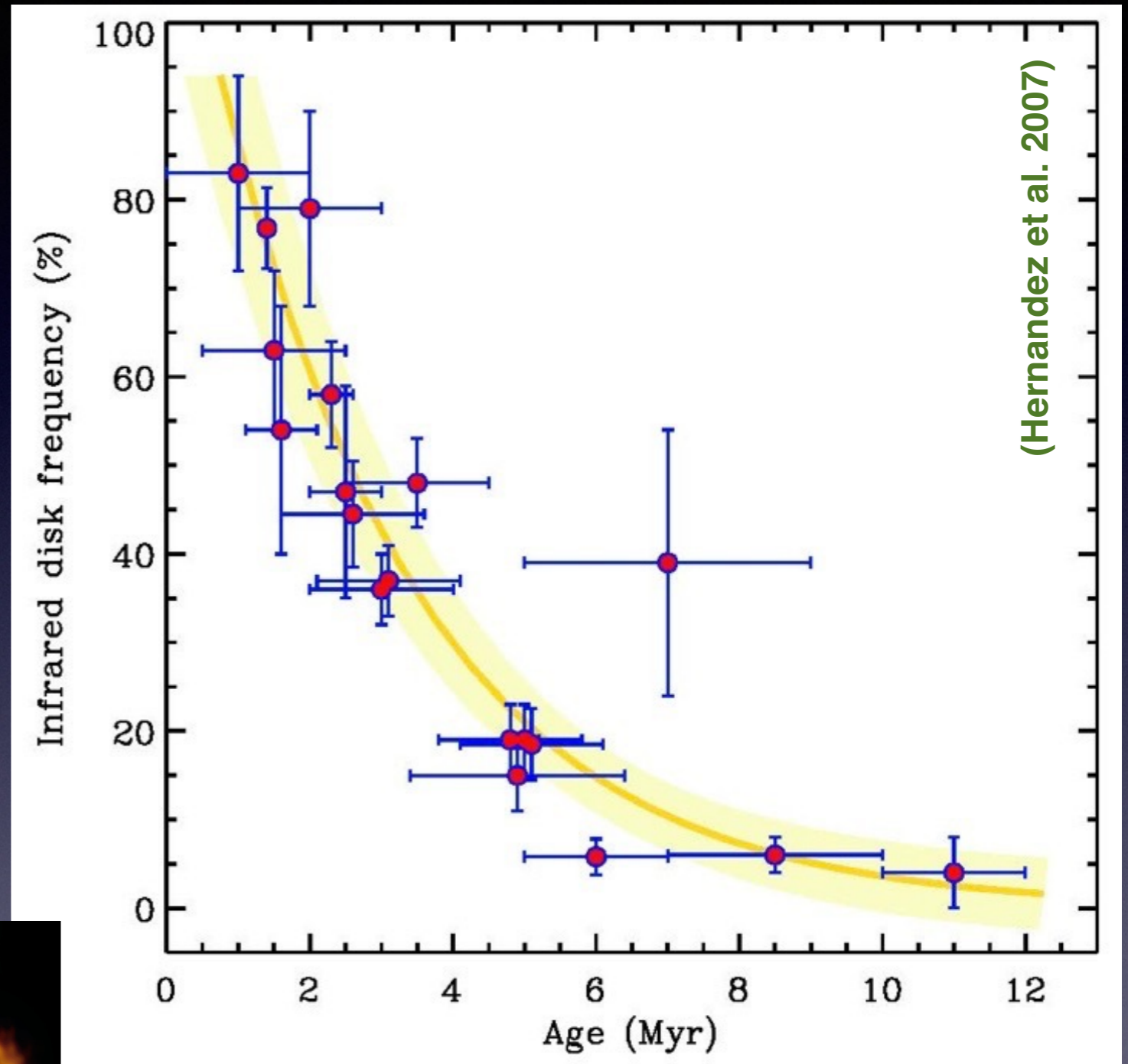
Core



Disk



Debris Disk

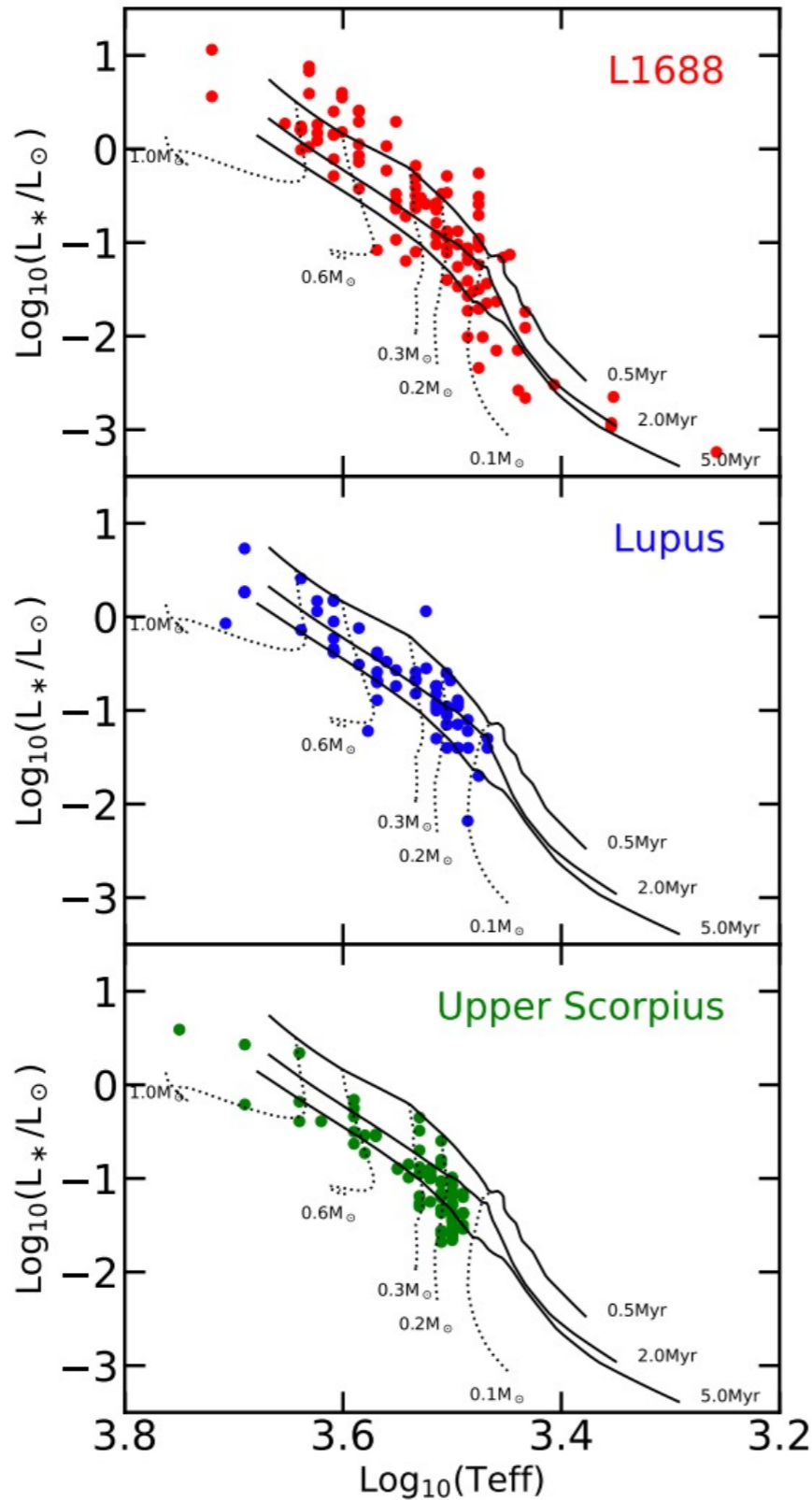


(Hernandez et al. 2007)

Inner disk clearing:  
e-folding time  $t \sim 2-3$  Myr

# Stellar parameters

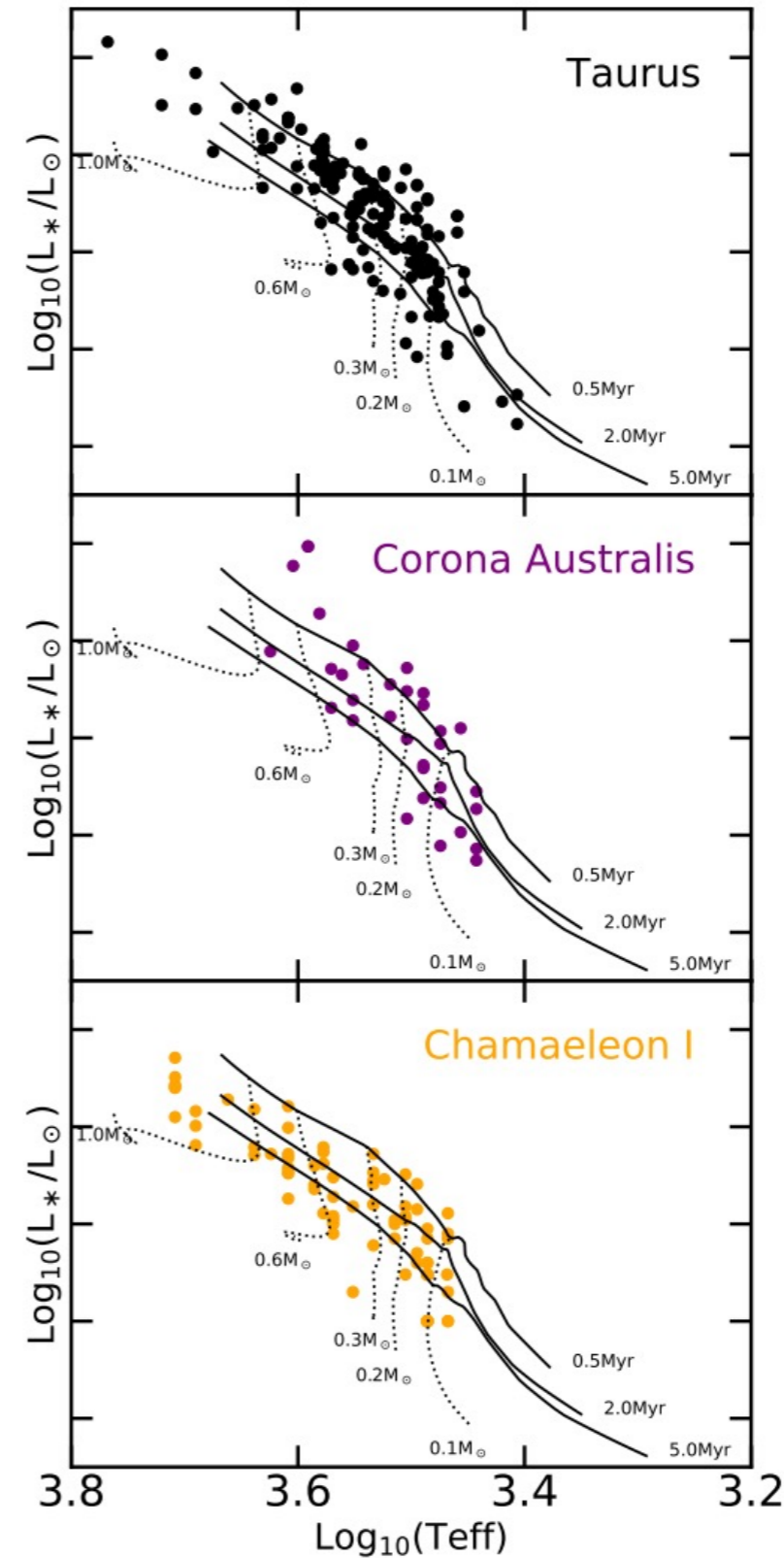
~1Myr



~2Myr

~5Myr

~0.9Myr



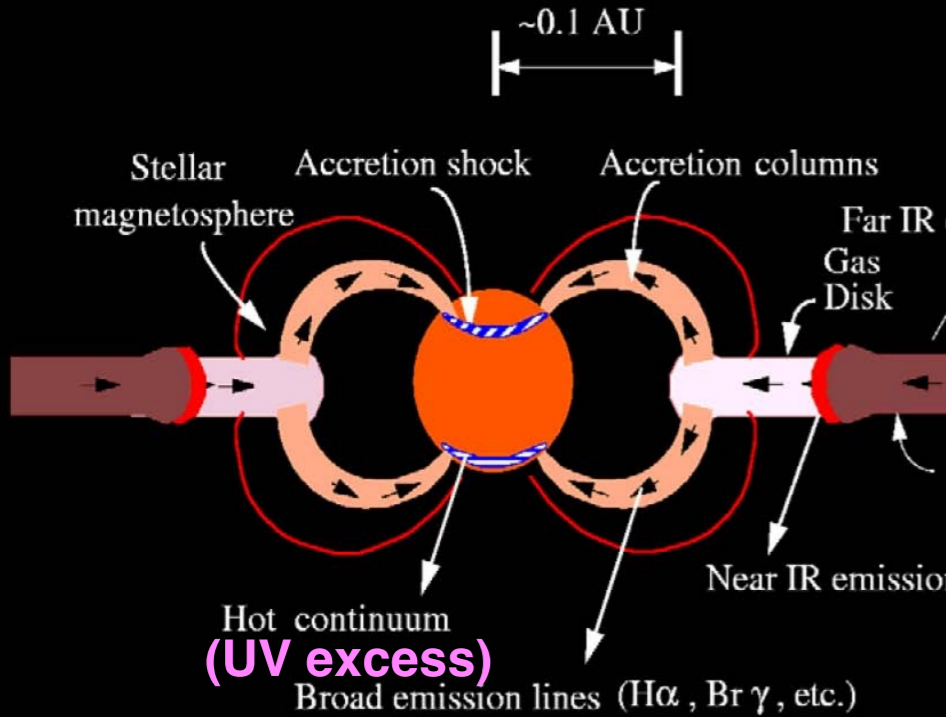
~0.6Myr

~3Myr

(Testi et al. 2022)

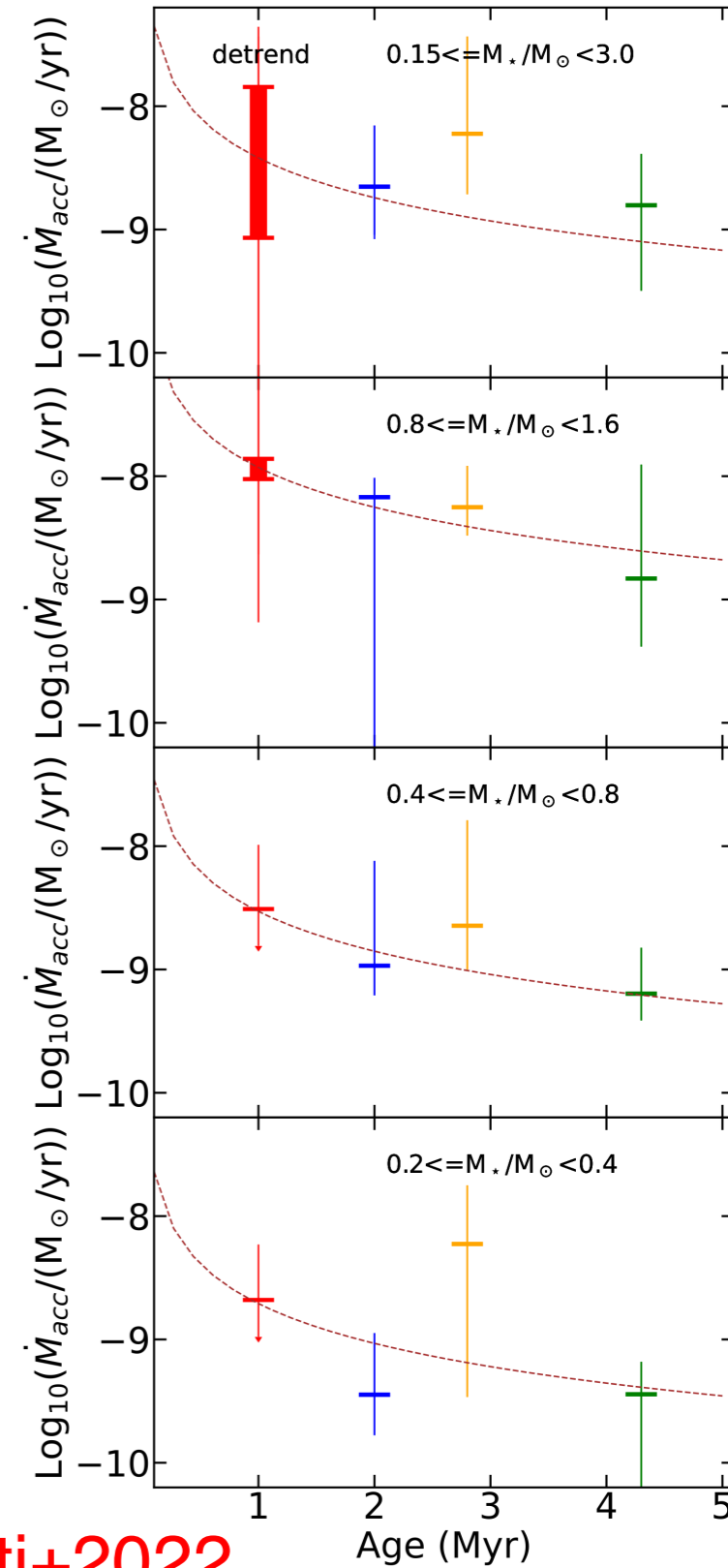
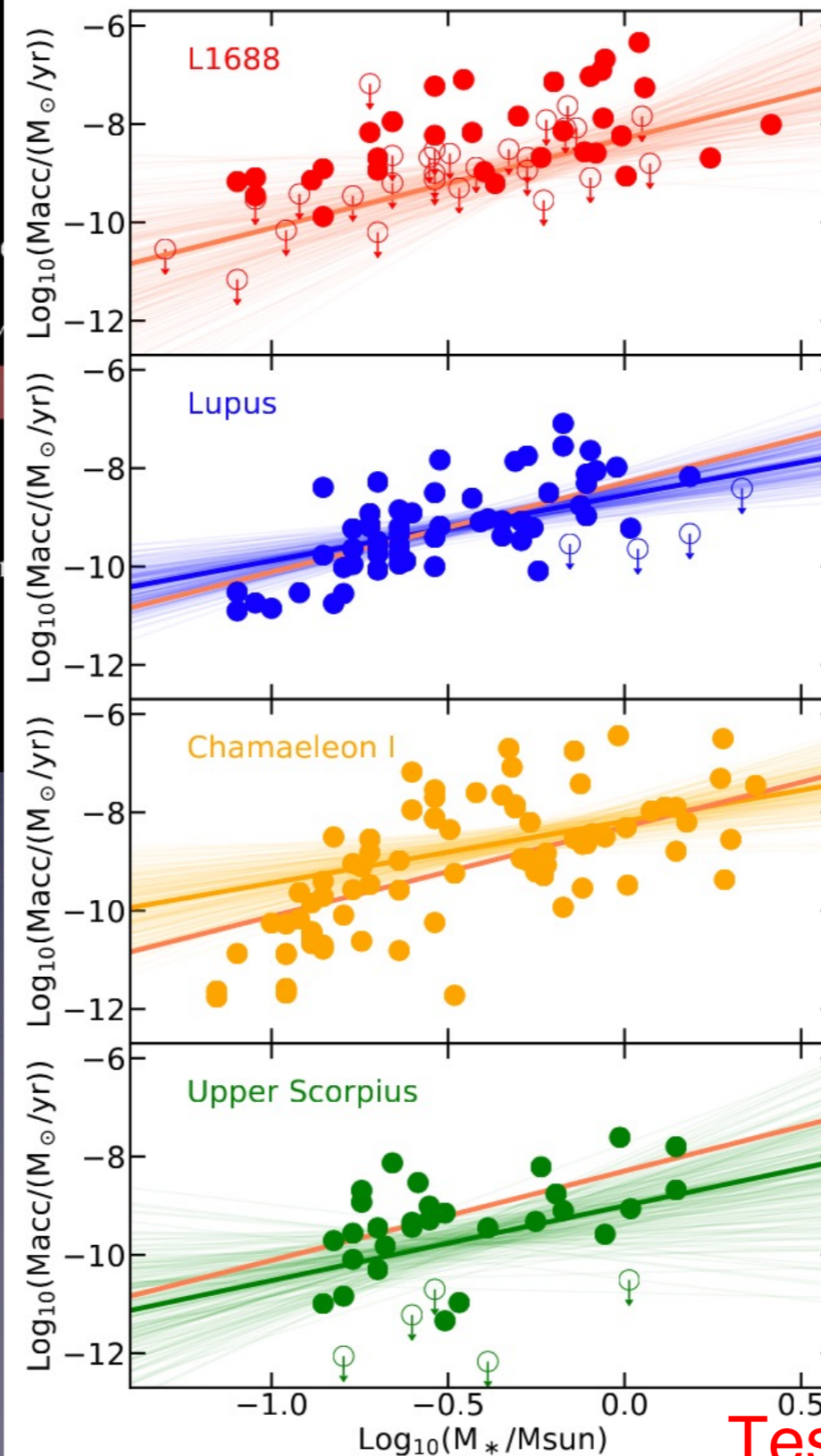
# Accretion

T Tauri star - magnetospheric accretion



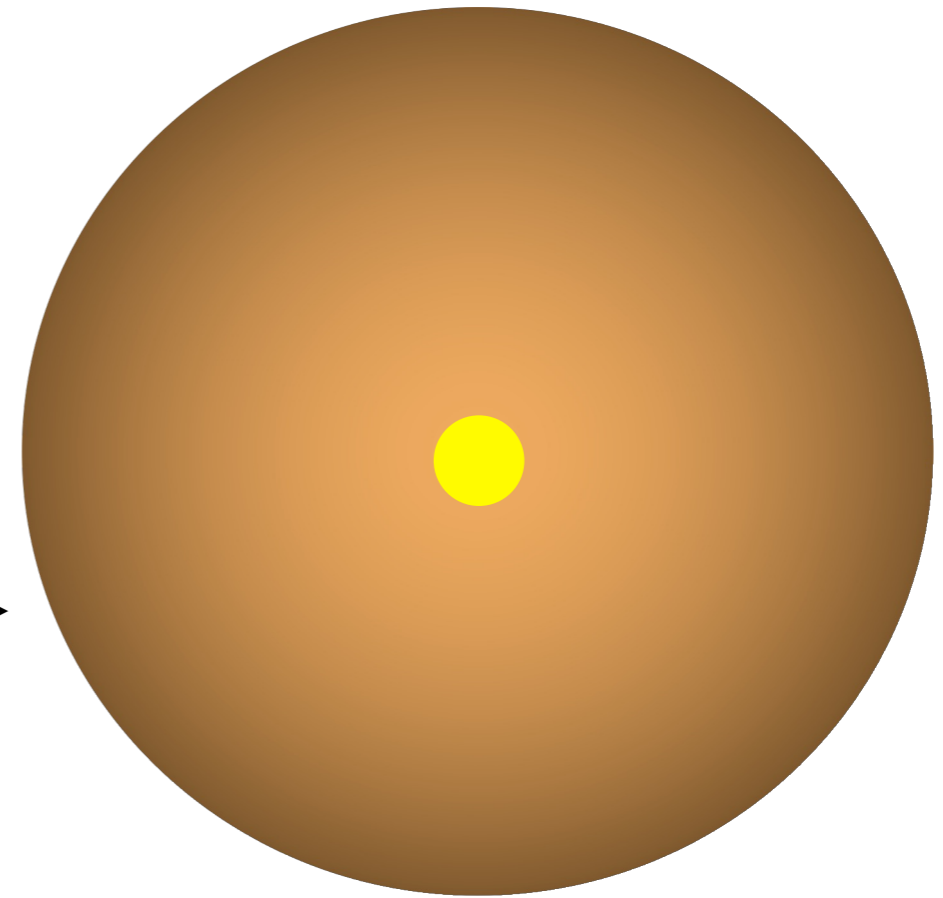
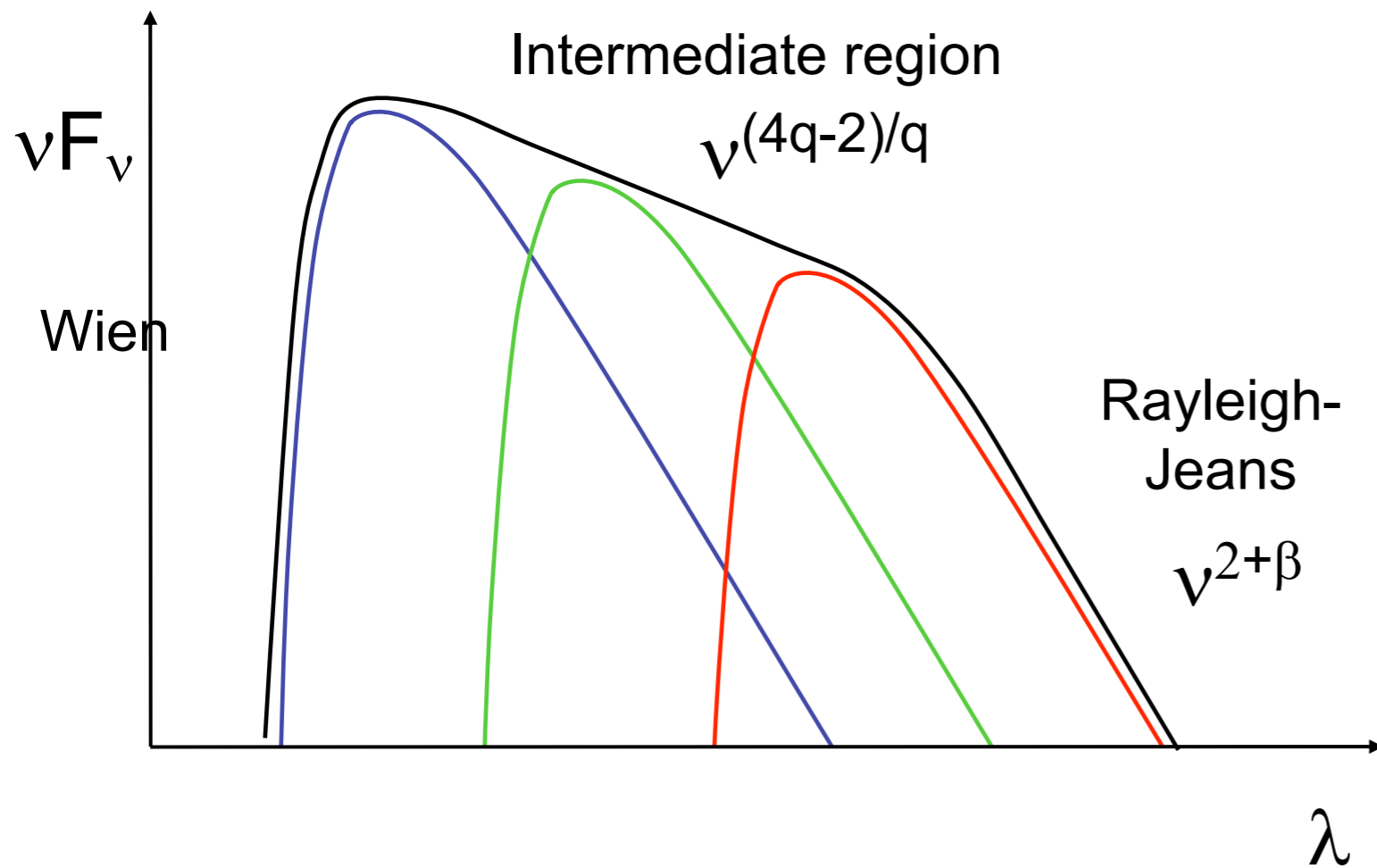
L. Hartmann

- Accretion rates fall “more or less” where predicted
- Evolution still hard to constrain (need better age/acc measurements)



Testi+2022

# SED for a locally isothermal disk



$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

$\tau_\nu \ll 1$

$$F_\nu \propto \Sigma(r) B_\nu(T_d(r)) \kappa_\nu$$

$T_d \sim \text{const.}$

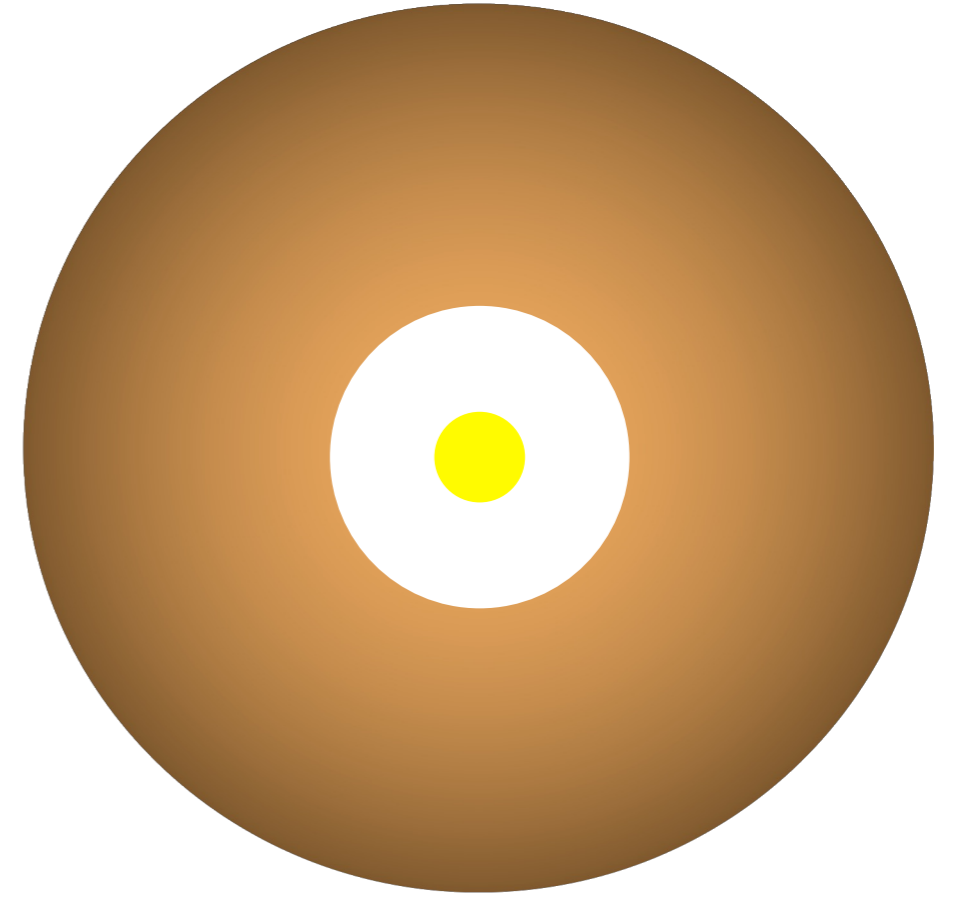
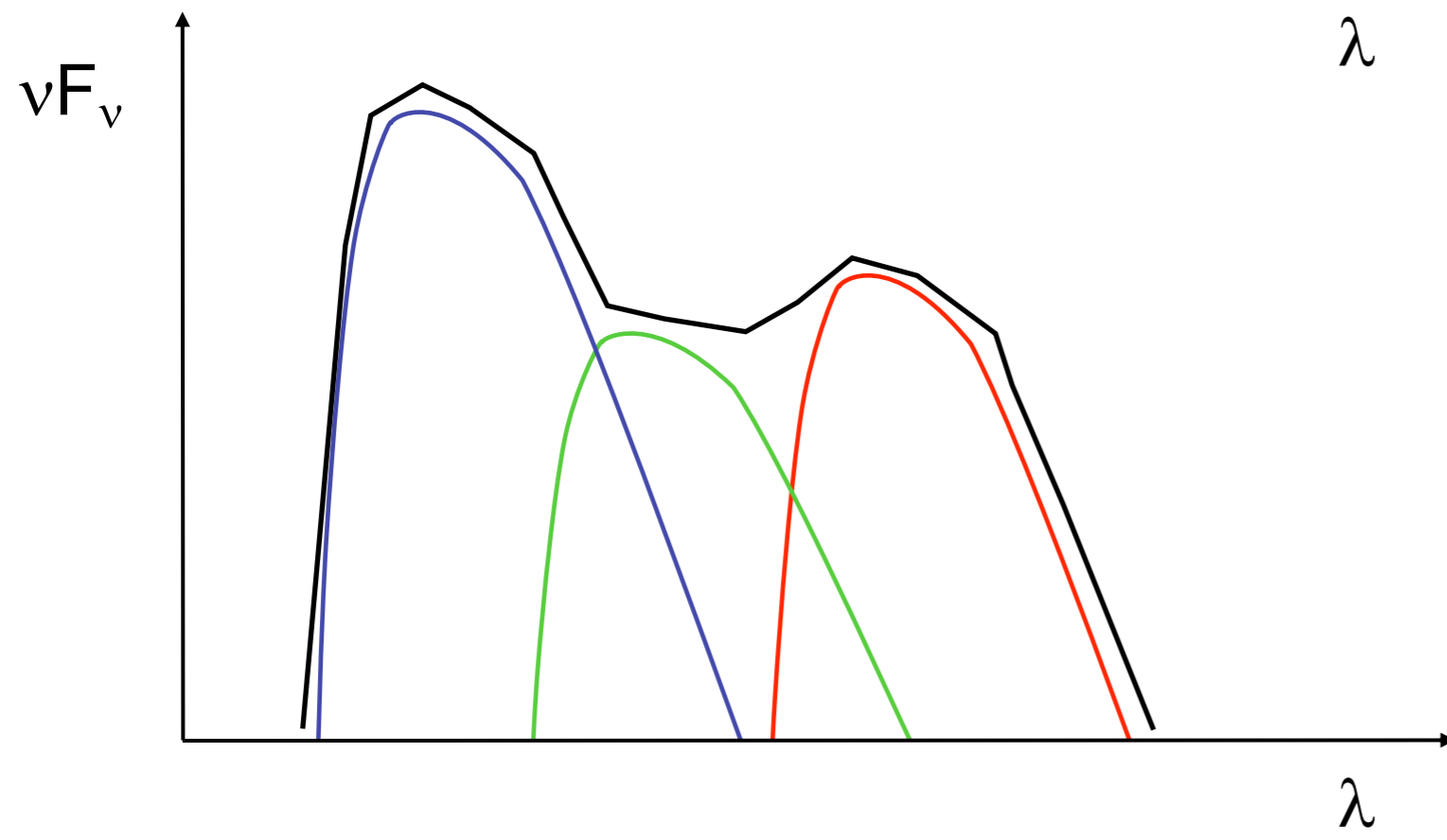
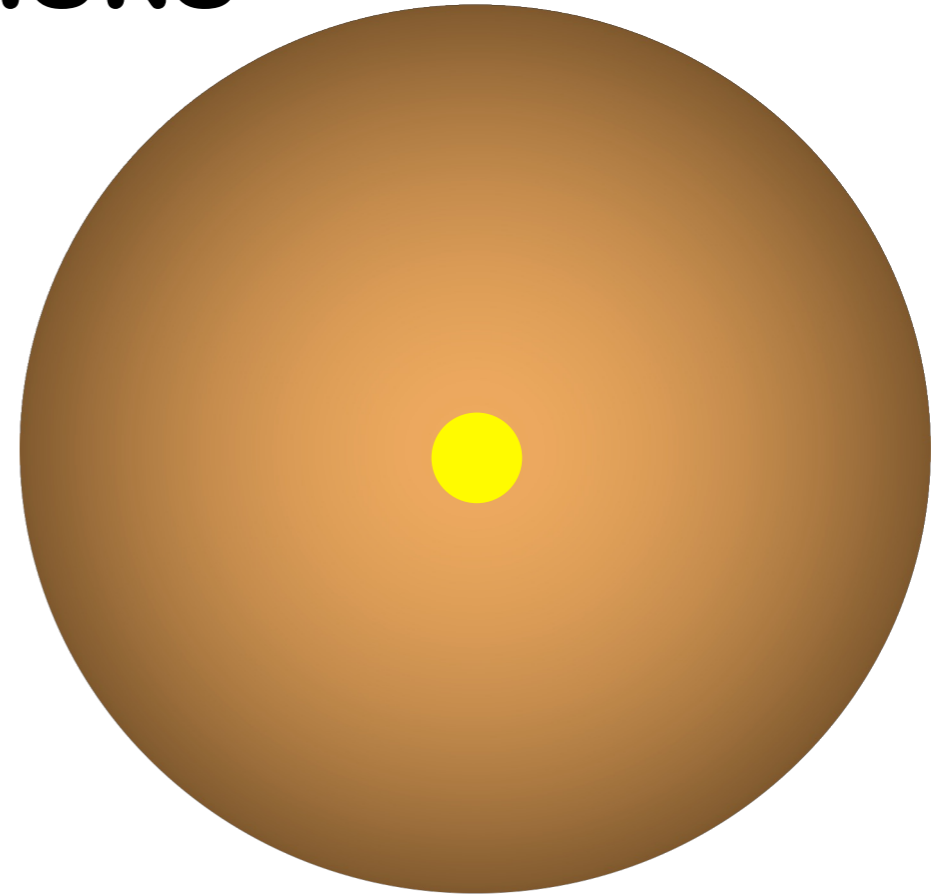
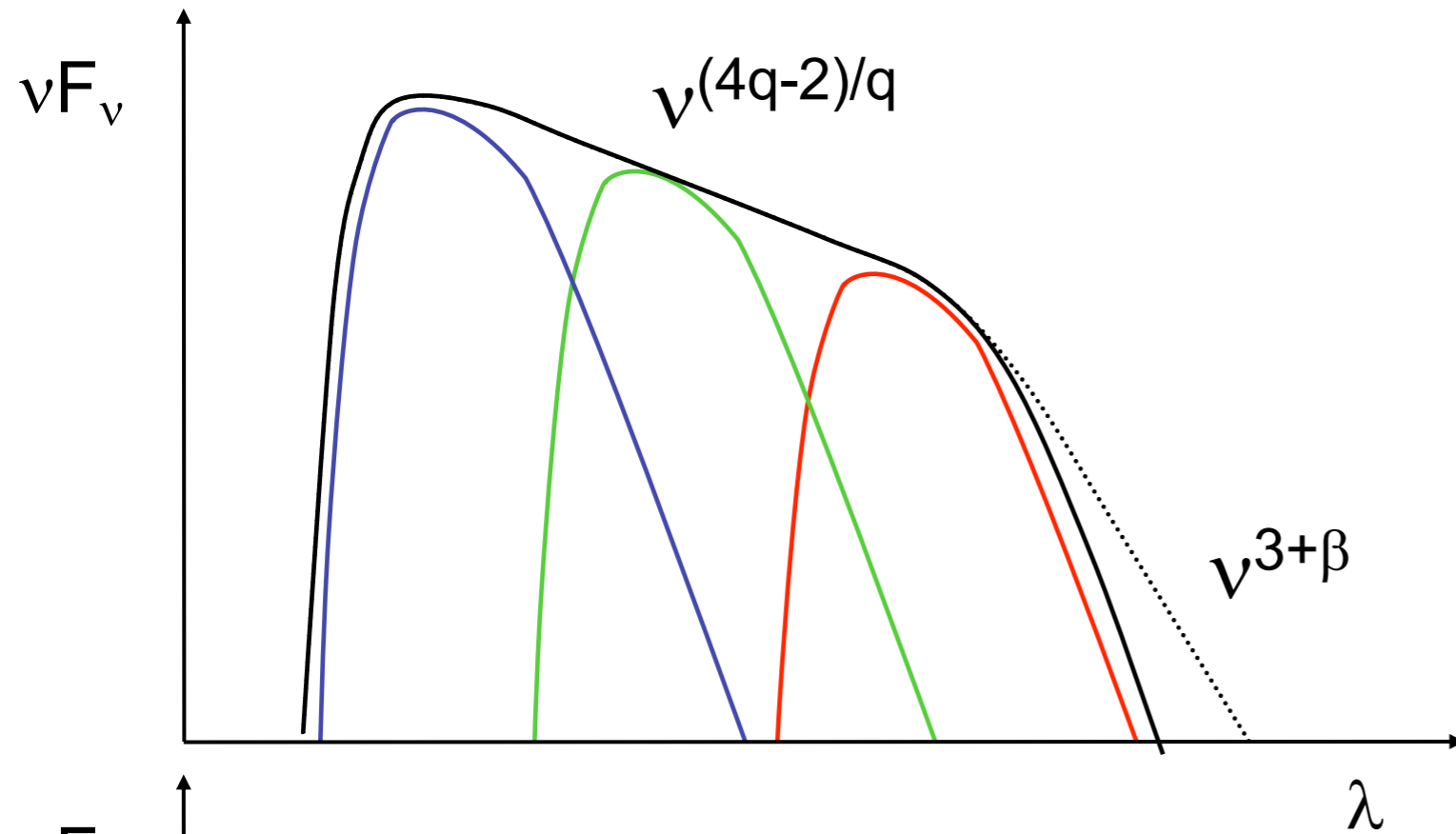
If  $\tau_\nu \ll 1$ :

$$F_\nu \propto \kappa_\nu \times B_\nu(T_d) \times M_d$$

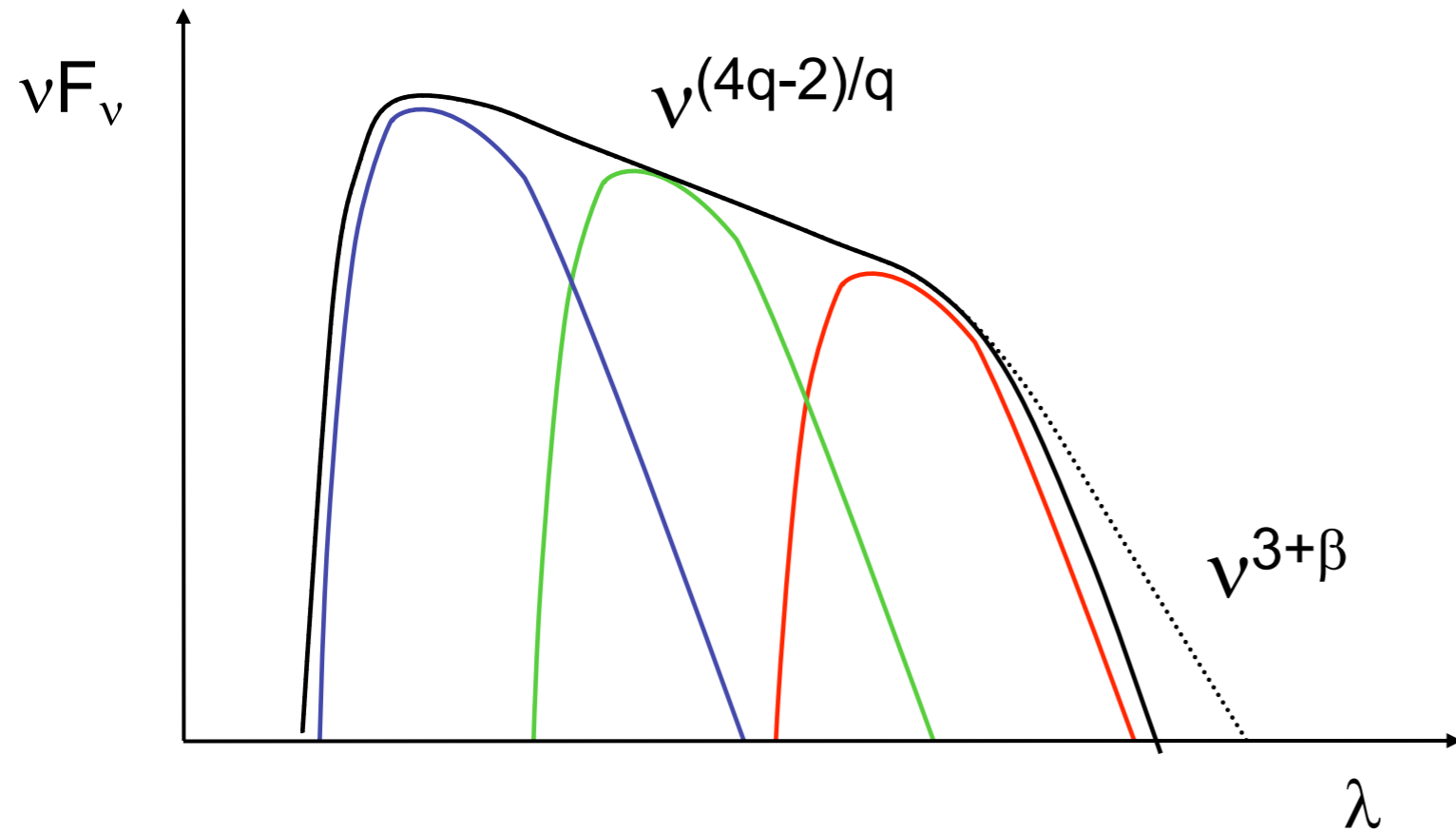
If  $\tau_\nu \gg 1$ :

$$F_\nu \propto B_\nu(T_d) \times \text{Area}$$

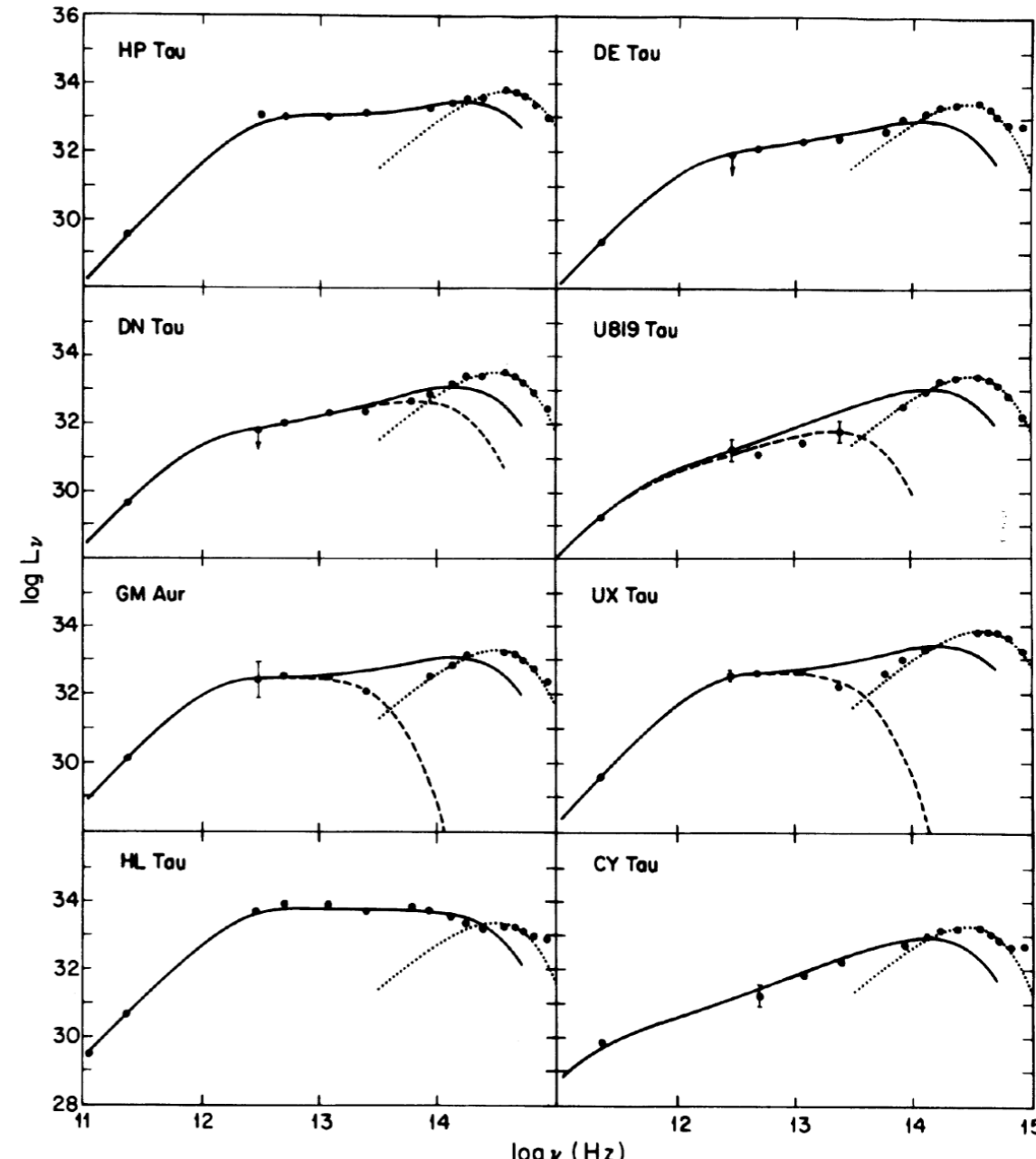
# Consequence: SED signature for Transition Disks



# SED of a locally isothermal disk



**Beckwith+ 1991**

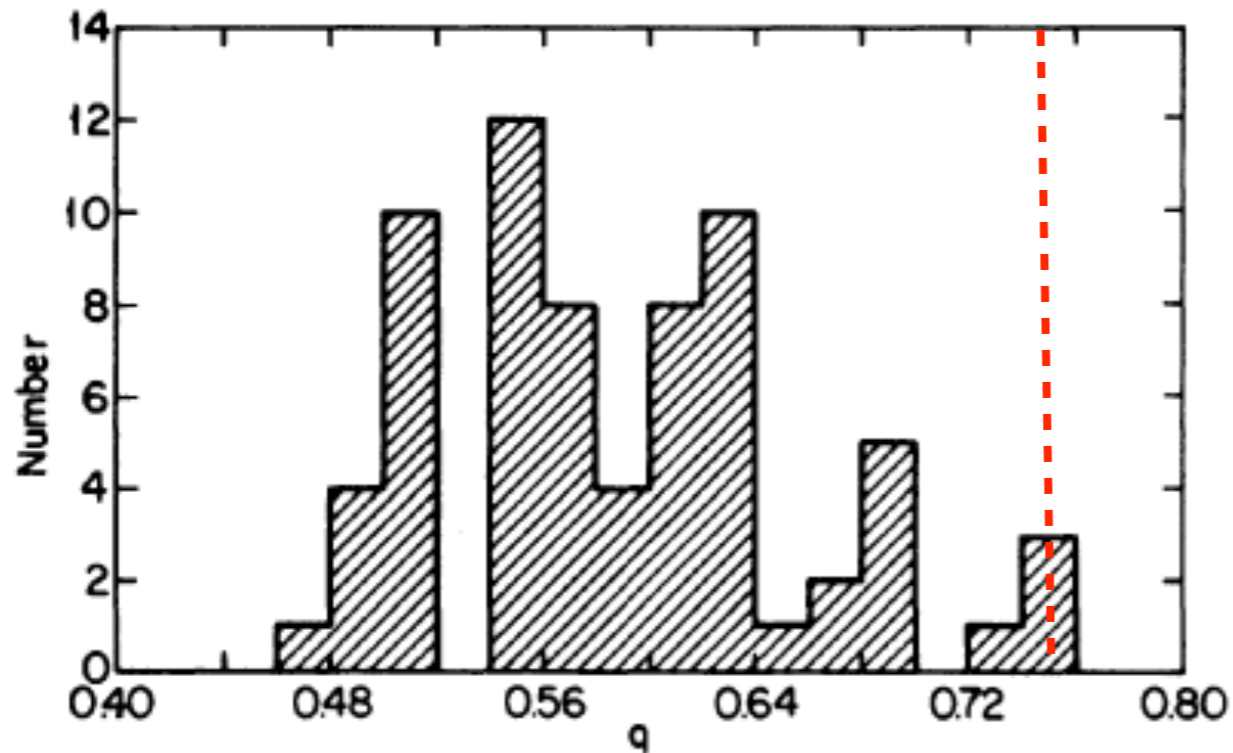


$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

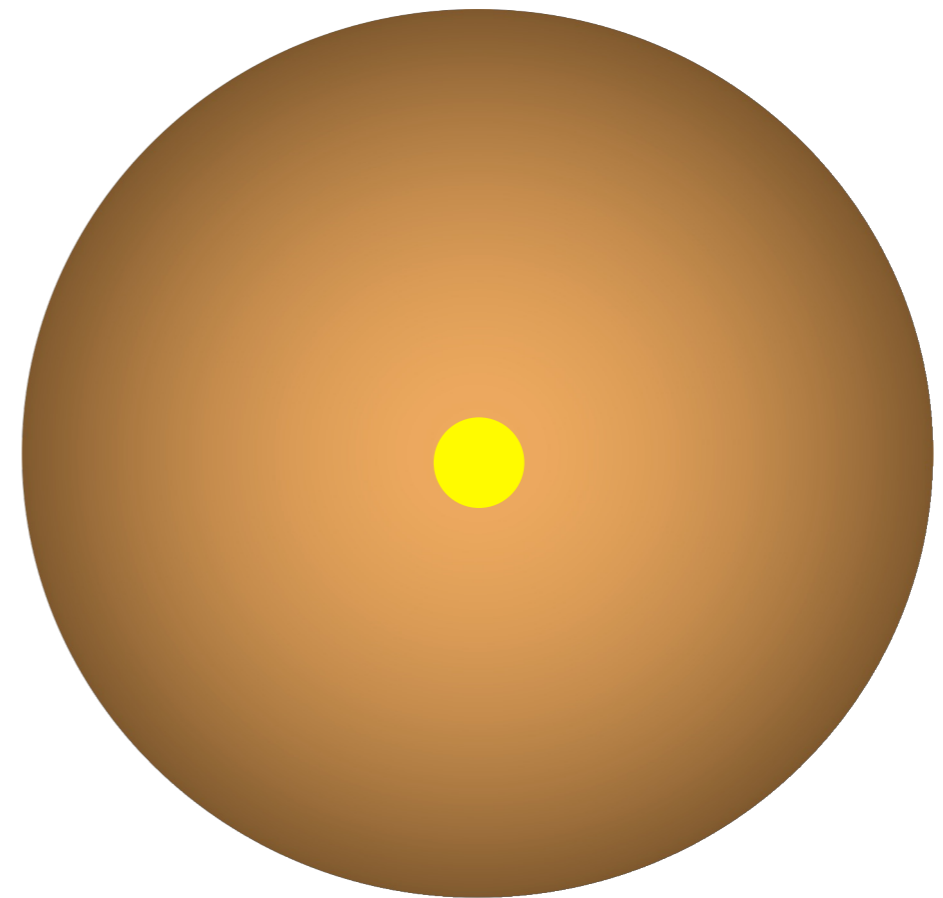
$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

# SED for a locally isothermal disk



Beckwith et al. (1991)



$$F_{\nu} = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_{\nu}(T_d)(1 - e^{-\tau_{\nu}})2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_{\nu} \propto \Sigma(r) \kappa_{\nu} \quad \Sigma(r) \propto r^{-p} \quad \kappa_{\nu} \propto \kappa_0 v^{\beta}$$

Viscous heating provides a poor fit of protoplanetary disc temperature: real disks are warmer than expected in the outer regions!



# “flat” passive disk

Irradiation flux:

$$F_{\text{irr}} = \alpha \frac{L_*}{4\pi r^2}$$

The flaring angle:

$$\alpha \cong \frac{0.4 r_*}{r}$$

$$T = \left( \frac{0.4 r_* L_*}{4\pi\sigma r^3} \right)^{1/4}$$

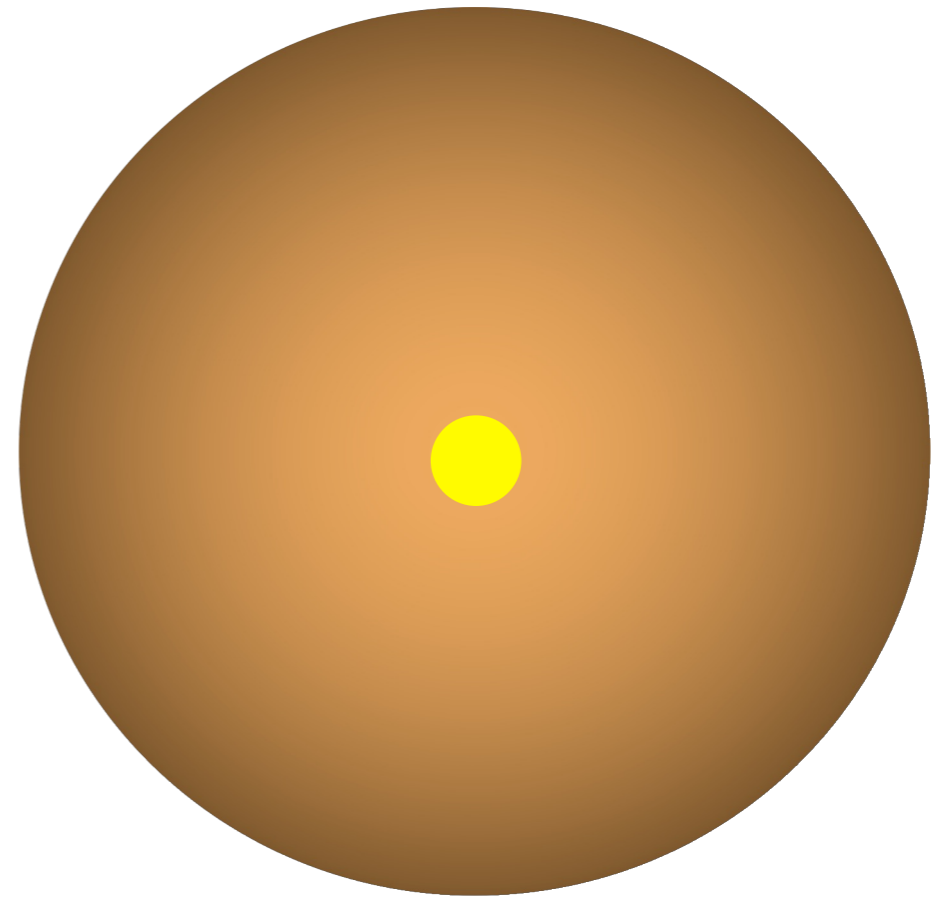
$$T \propto r^{-3/4}$$

Coincidentally, same profile as an  
viscously heated disk : not good!

$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d)(1 - e^{-\tau_\nu}) 2\pi r dr$$

$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 v^\beta$$



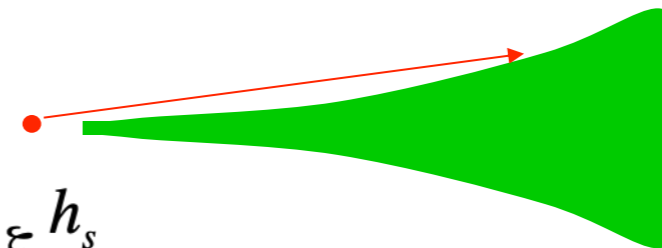
# “flared” passive disk

Irradiation flux:

$$F_{\text{irr}} = \alpha \frac{L_*}{4\pi r^2}$$

The flaring angle:

$$\alpha = r \frac{\partial}{\partial r} \left( \frac{h_s}{r} \right) \rightarrow \xi \frac{h_s}{r}$$

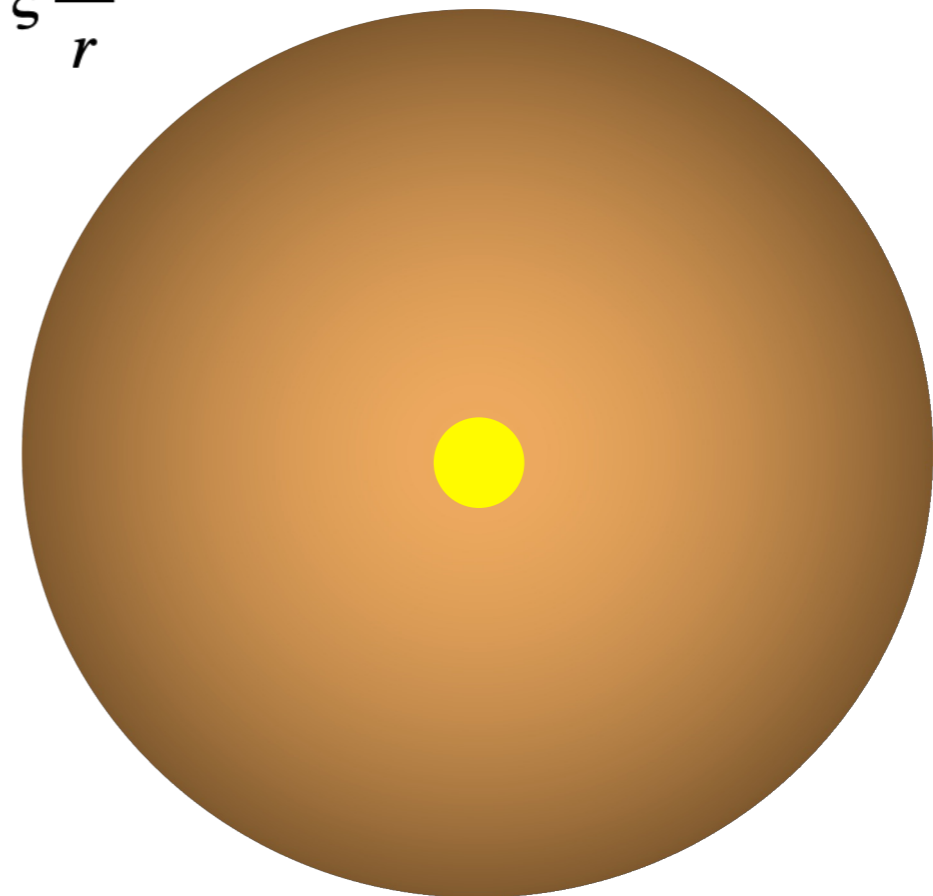


$$T^4 = \frac{\xi}{\sigma} \frac{h_s L_*}{4\pi r^3}$$

$$h_s = \chi h$$

Can work...

...depending on  $h_s(r)$

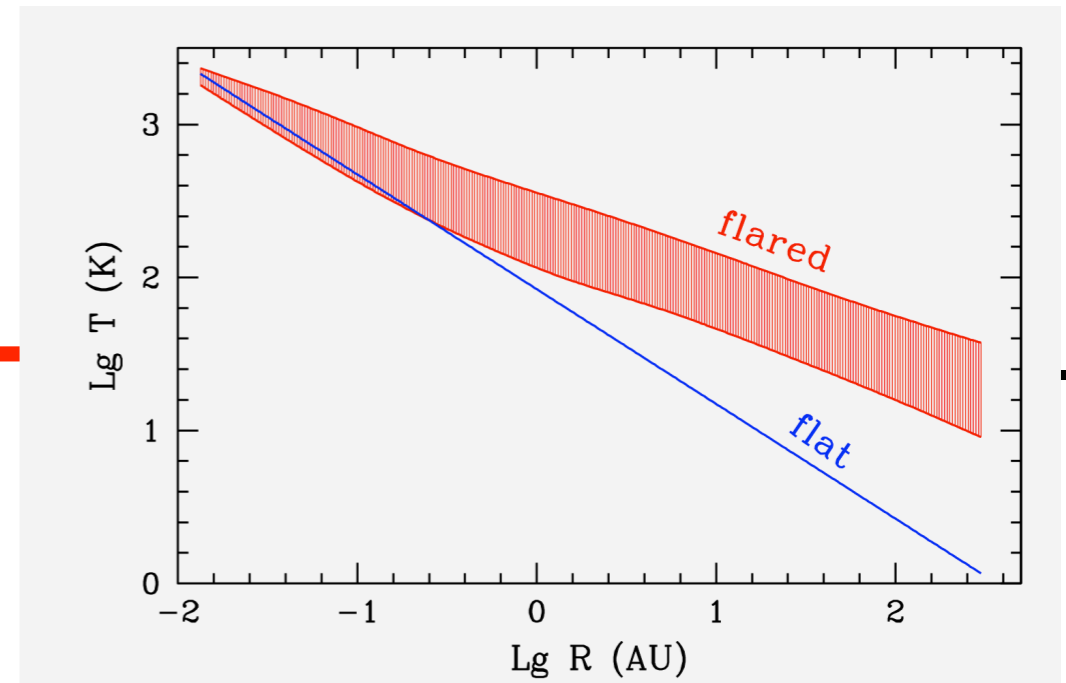
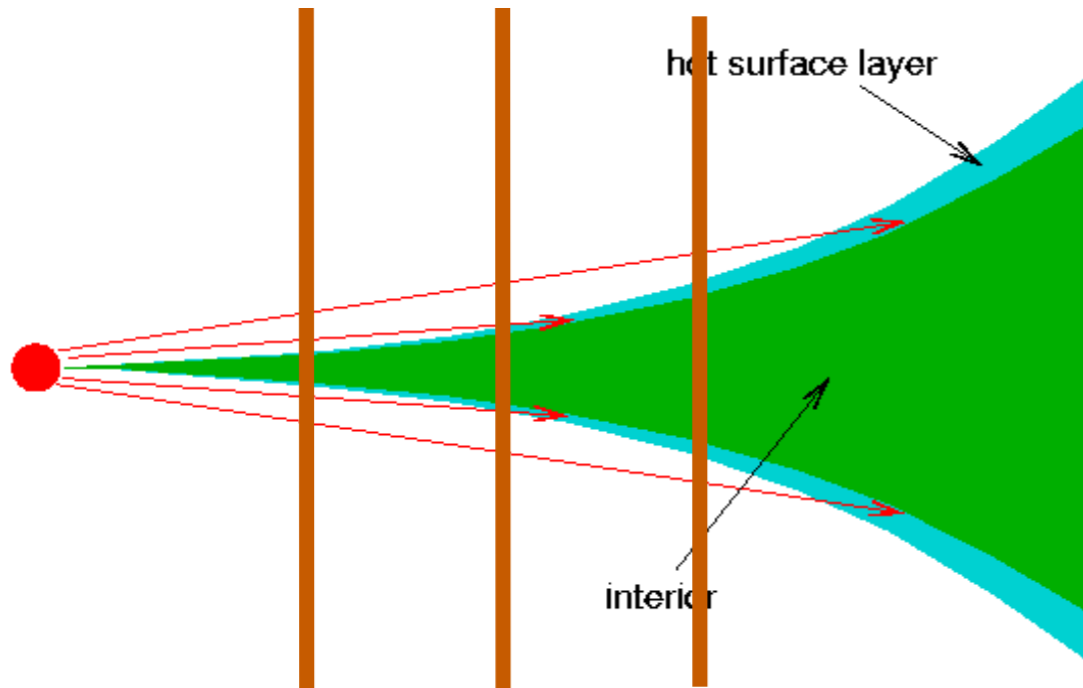


$$F_\nu = \frac{\cos\theta}{D^2} \int_{r_i}^{r_o} B_\nu(T_d) (1 - e^{-\tau_\nu}) 2\pi r dr$$

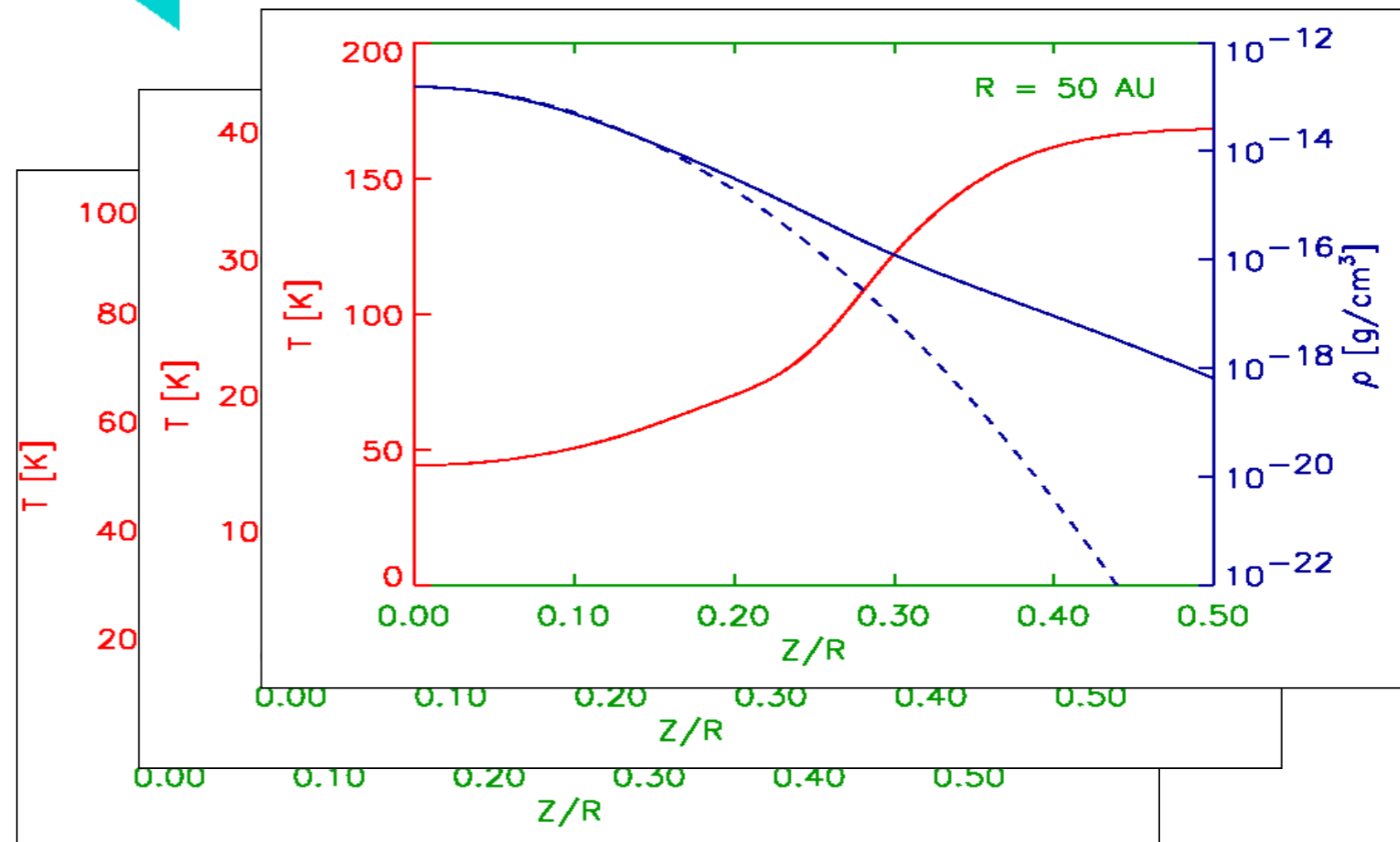
$$T_d \sim r^{-q}$$

$$\tau_\nu \propto \Sigma(r) \kappa_\nu \quad \Sigma(r) \propto r^{-p} \quad \kappa_\nu \propto \kappa_0 \nu^\beta$$

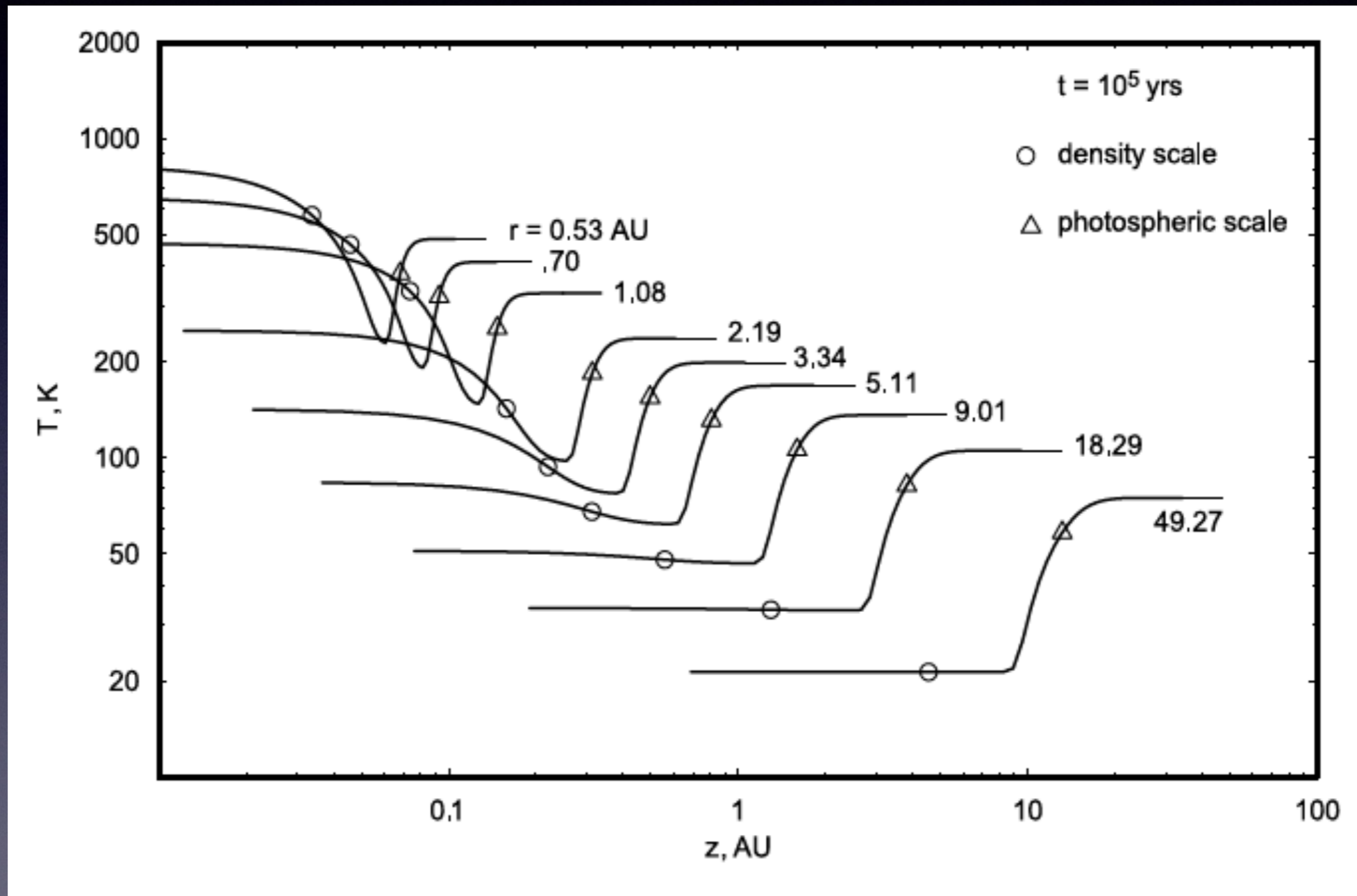
# Flared disks: detailed models



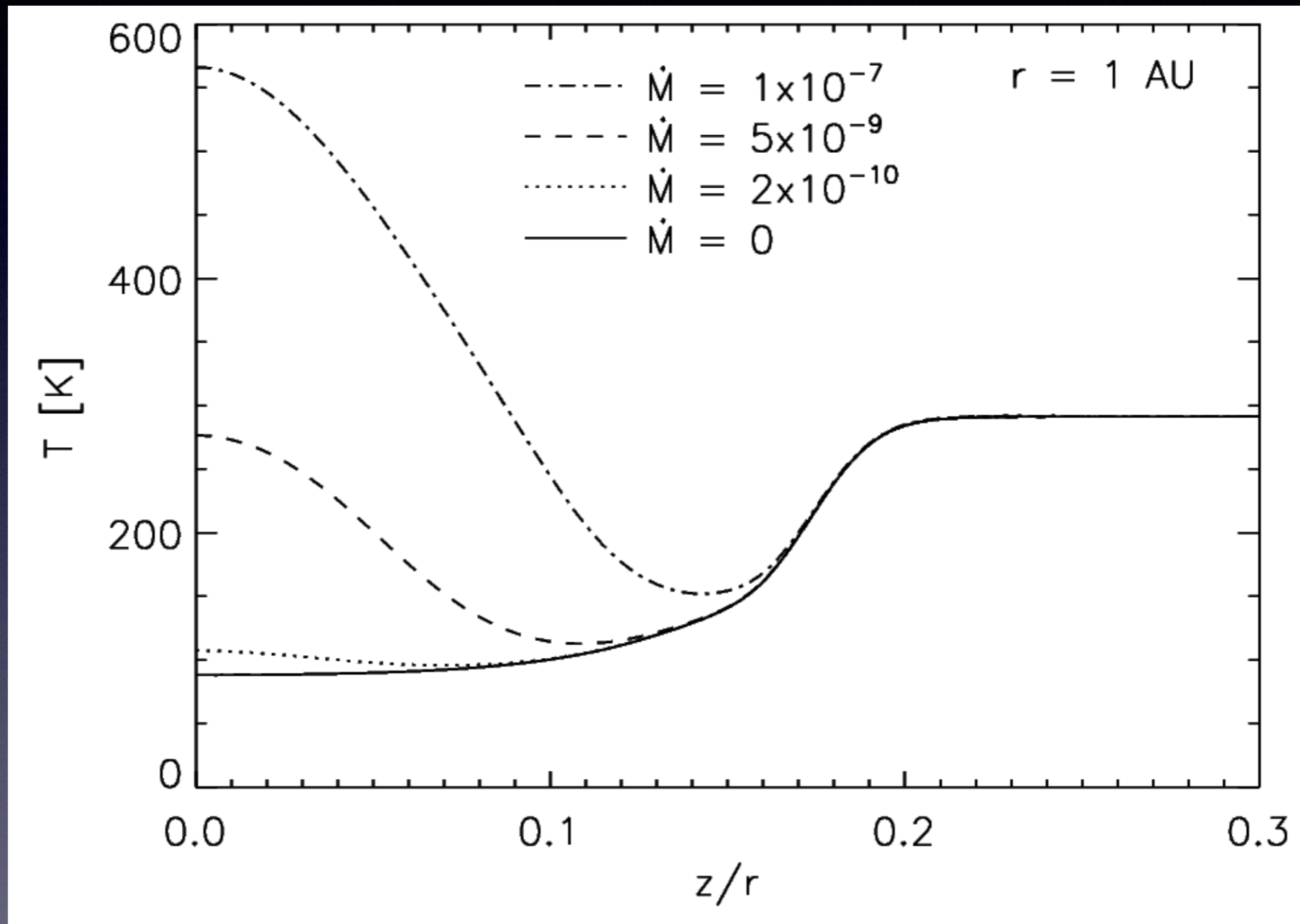
... consists of vertical slices, each forming a 1D problem. All slices are independent from each other.



# Including viscous heating



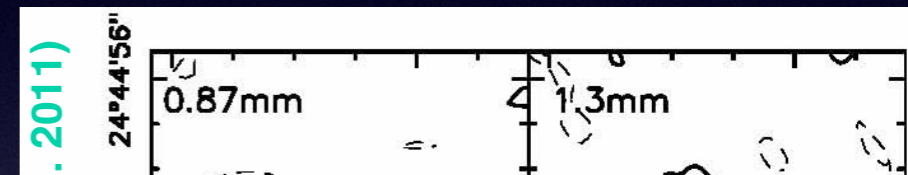
# Including viscous heating



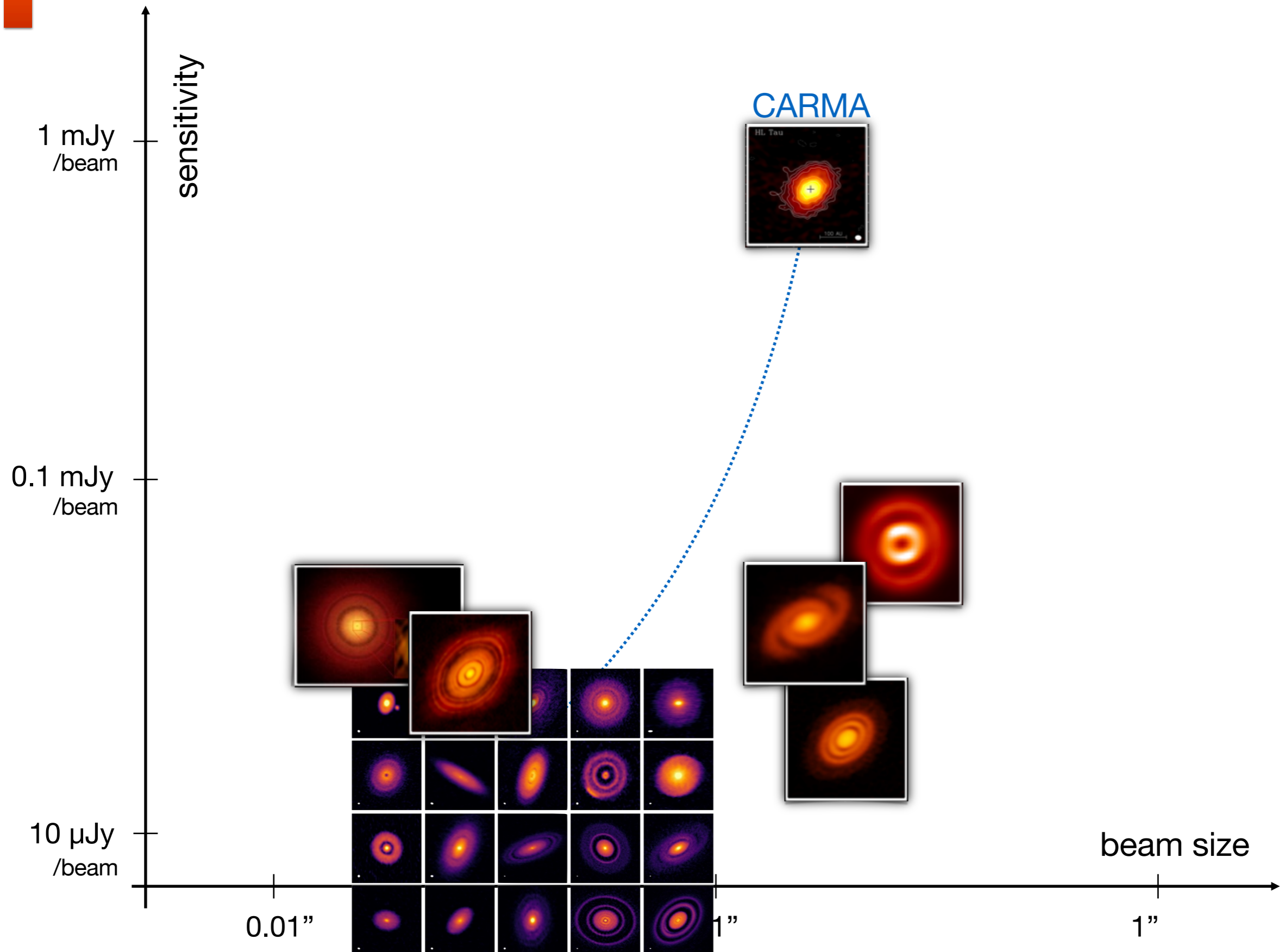
( $M_{\text{acc}} \sim 10^{-8} M_{\text{sun}}/\text{yr}$  @ 1 Myr)

# Resolving disk structure

- $10\text{AU}@140\text{pc}=0.14\text{ arcsec}$
- Diffraction:  $0.14\text{arcsec}@1\text{mm} \Rightarrow 1.5\text{km}$
- Need to use interferometry

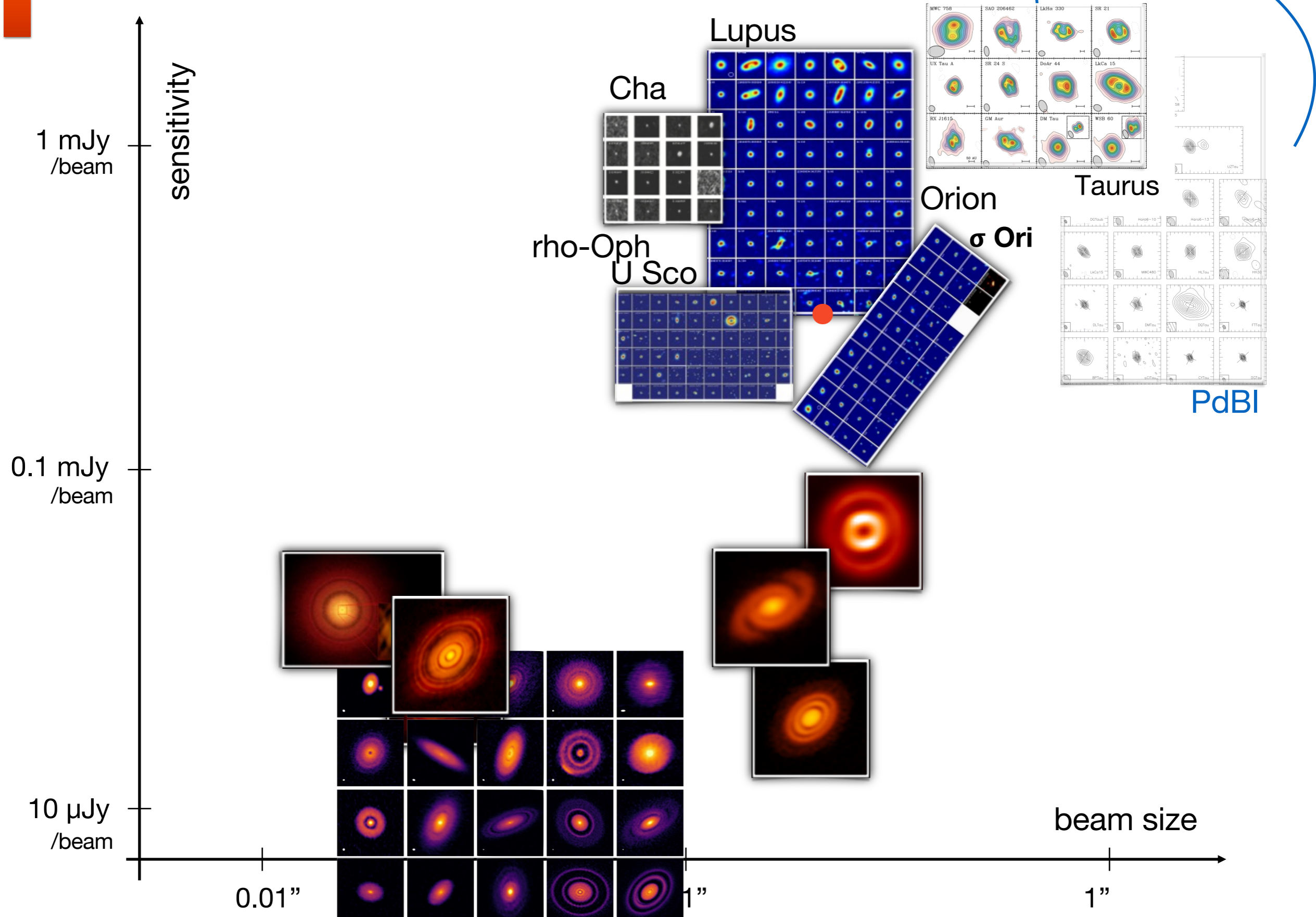


# The ALMA Revolutions



(slide thanks to M. Tazzari)

# The ALMA Revolutions

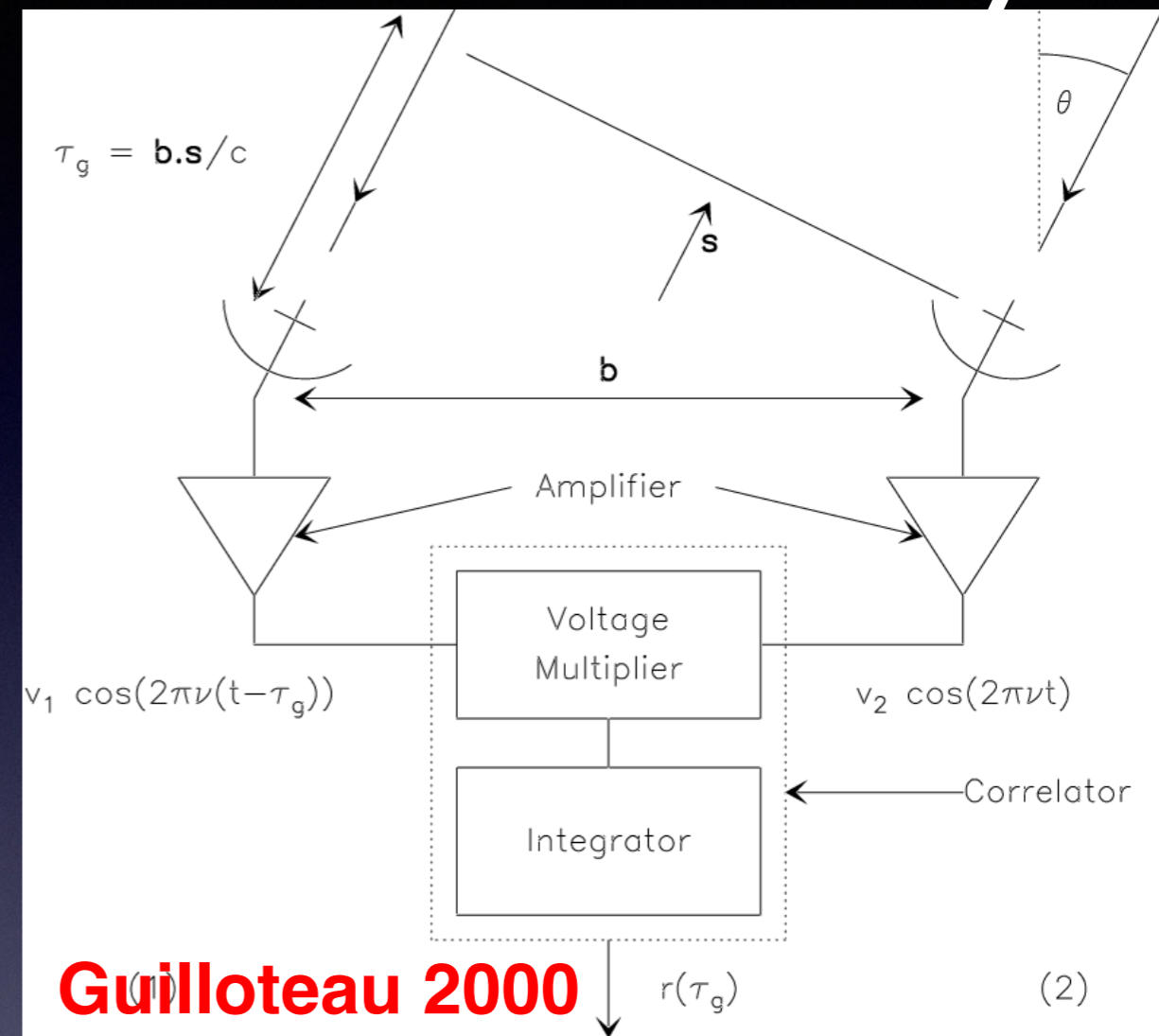


(slide thanks to M. Tazzari)



# Small digression on interferometry

- Interference pattern of the signal from two antennas separated by a baseline  $b$
- After correction for the optical path delay each pair of antennas measure the fringe visibility corresponding to the baseline  $b$  (as seen from the source)



$$V(u, v) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} P(x, y) I(x, y) \exp(-2i\pi (ux + vy)) dx dy$$

$(x, y)$  = Sky     $(u, v)$  = baselines plane

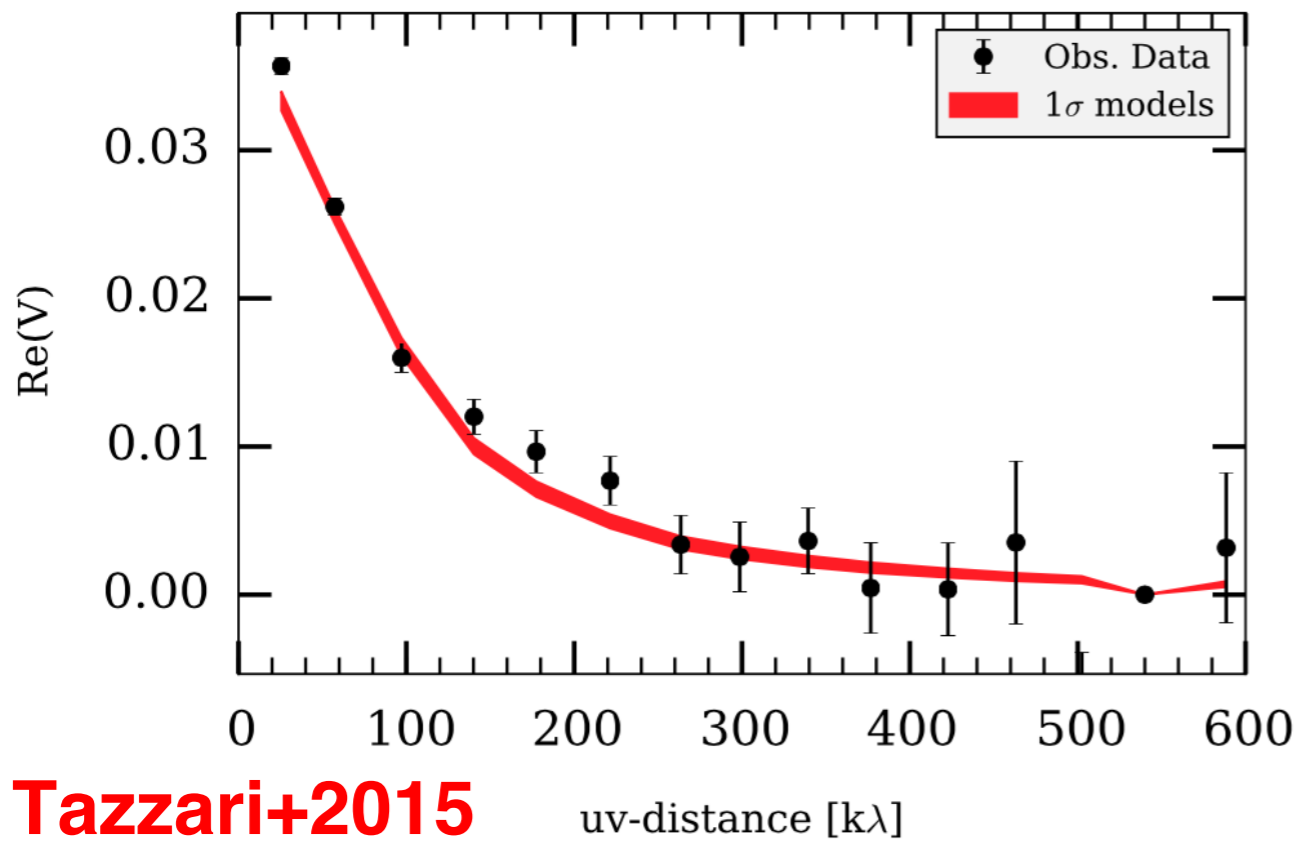
$P(x, y)$  = Antenna power pattern

$V(u, v)$  = Measured visibility

$I(x, y)$  = Brightness distribution on Sky

# Analysis of interferometric data

2.8mm CARMA



$$\Sigma(R, t) = \Sigma_t \left( \frac{R_t}{R} \right)^\gamma \times \exp \left\{ -\frac{1}{2(2-\gamma)} \left[ \left( \frac{R}{R_t} \right)^{(2-\gamma)} - 1 \right] \right\}$$

## Bayesian Fitting Tool

### Disk model

computes disk emission at different wavelengths

### Fourier Transform

### Synthetic visibilities

in the (u,v) plane sampled at the P.A.

### Interferometric data

Visibilities in the (u,v) plane

posterior  $\propto \exp(-\chi^2/2)$

- Models solve for the self consistent structure, given Sigma (and star)
- See also Isella+2007;2009

# galarío: a Gpu Accelerated Library for Analysing Radio Interferometry Observations

Marco Tazzari<sup>1</sup>★, Frederik Beaujean<sup>2</sup> and Leonardo Testi<sup>2,3</sup>

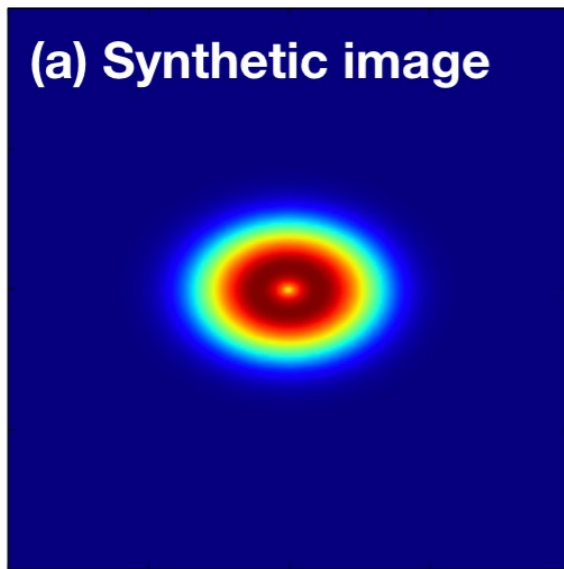
<sup>1</sup>*Institute of Astronomy, University of Cambridge, Madingley Road, CB3 0HA, Cambridge, UK*

<sup>2</sup>*Excellence Cluster Universe, Boltzmannstr. 2, D-85748 Garching, Germany*

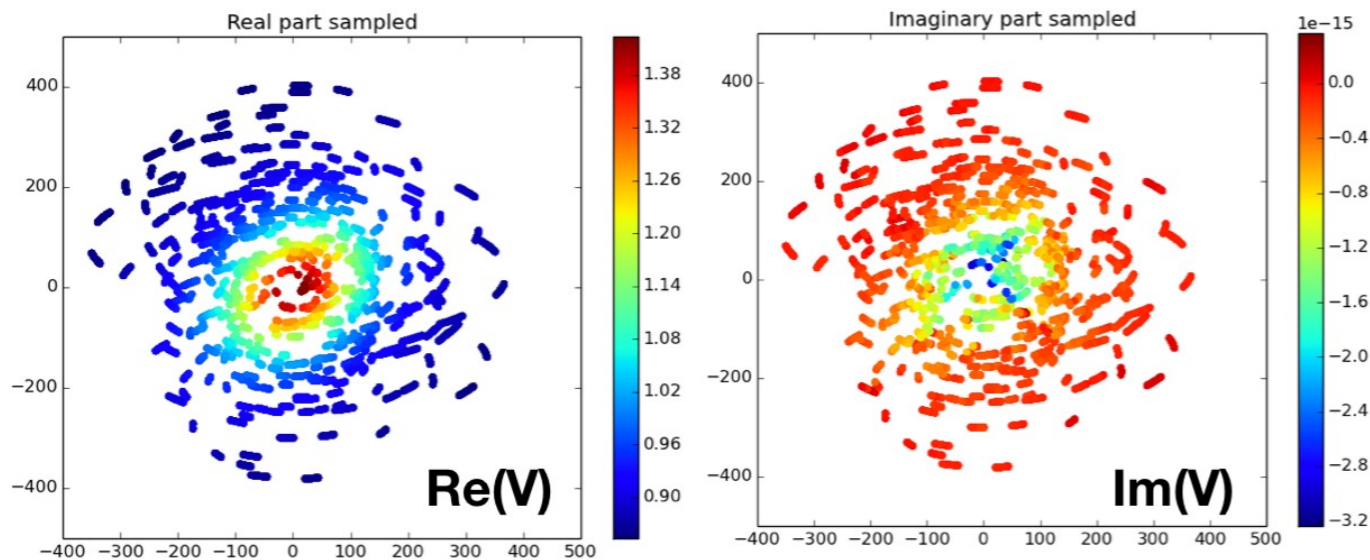
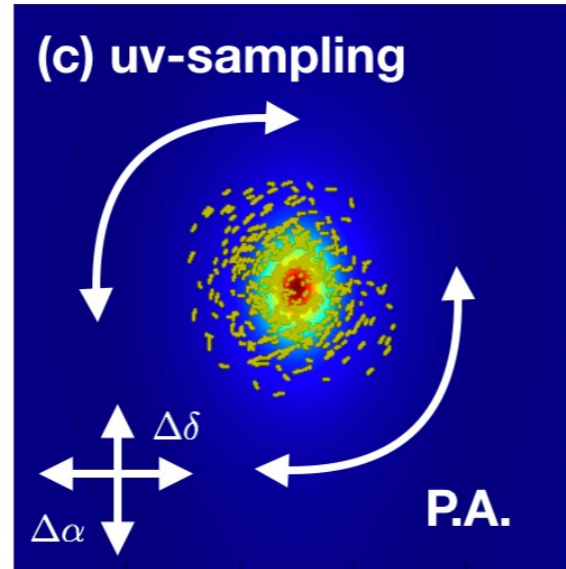
<sup>3</sup>*European Southern Observatory, Karl Schwarzschild Str. 2, D-85748 Garching, Germany*



(a) Synthetic image



(c) uv-sampling



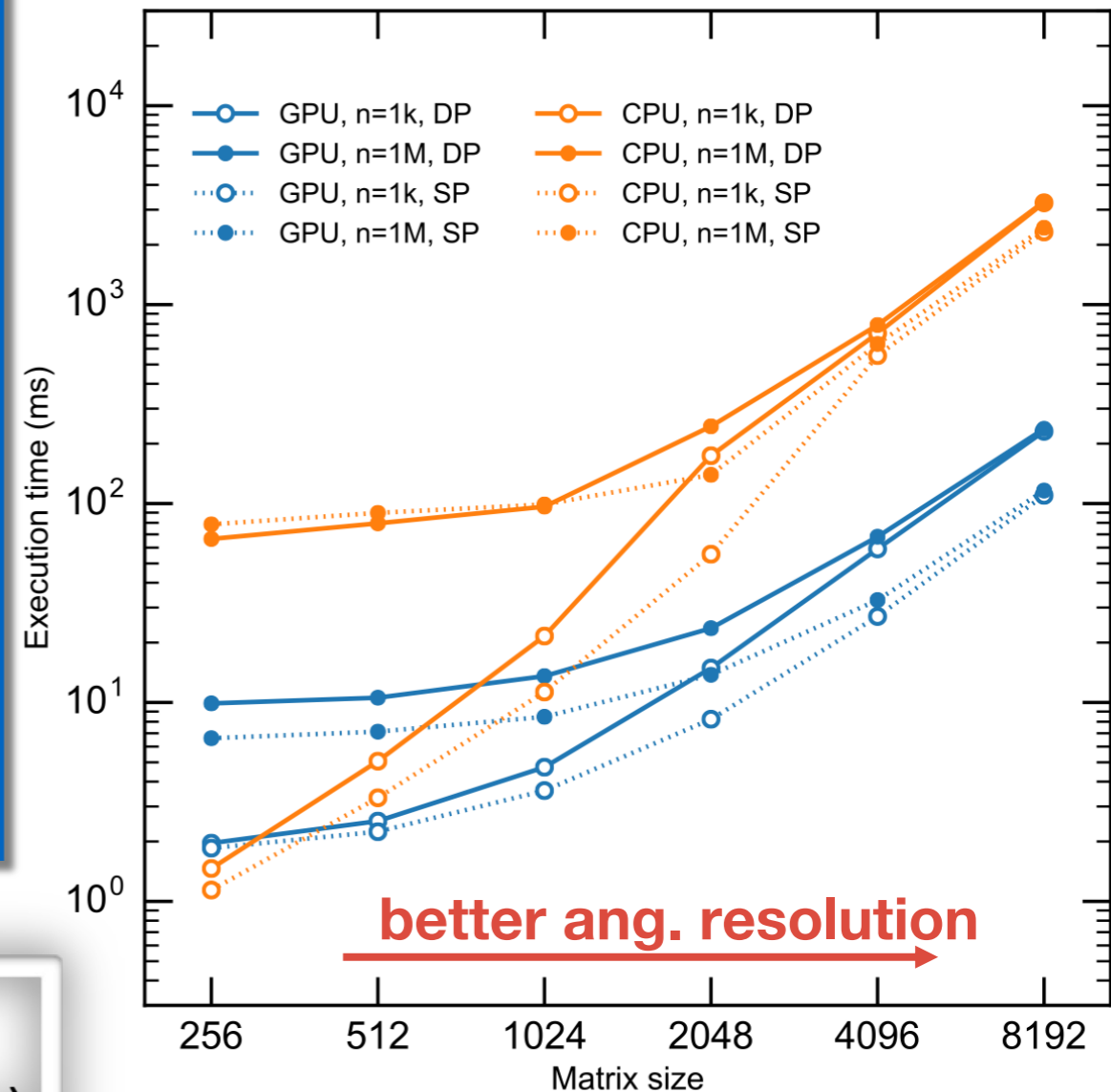
• example:

```
from galarío import double_cuda, single_cuda
double_cuda.chi2(image, d_alpha, d_delta, uv, obs_vis)
```

ility sampling)

is tools

<https://github.com/mtazzari/galarío>



# GALARIO: a GPU Accelerated Library for Analysing Radio Interferometry Observations



Marco Tazzari<sup>1\*</sup>, Frederik Beaujean<sup>2</sup> and Leonardo Testi<sup>2,3</sup>

<https://github.com/mtazzari/galario>

## ► Easy to use:

- compute **visibilities** from 2D image:
- compute  $\chi^2$  from 2D image:
- compute  $\chi^2$  from 1D profile:

```
V_mod = sampleImage(image, dxy, u, v)
```

```
chi2 = chi2Image(image, dxy, u, v, ReV, ImV, w)
```

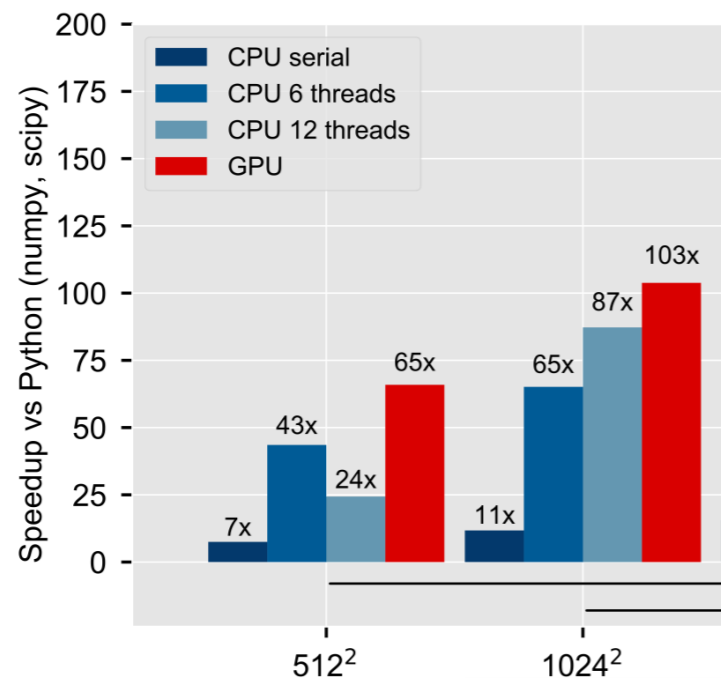
```
chi2 = chi2Profile(l, Rmin, dR, nxy, dxy, u, v, ReV, ImV, w)
```

## ► Easy to install:

```
conda install -c conda_forge galario
```

## ► *Fouriously* fast:

up to 150x faster than



## ► Simple switch to GPU:

```
import galar
```

## ► many applications:

- **protoplanetary** disks
- **debris** disks
- **high redshift** galaxies
- **massive** stars cores

## ► ready to exploit the ALMA wavelength coverage:

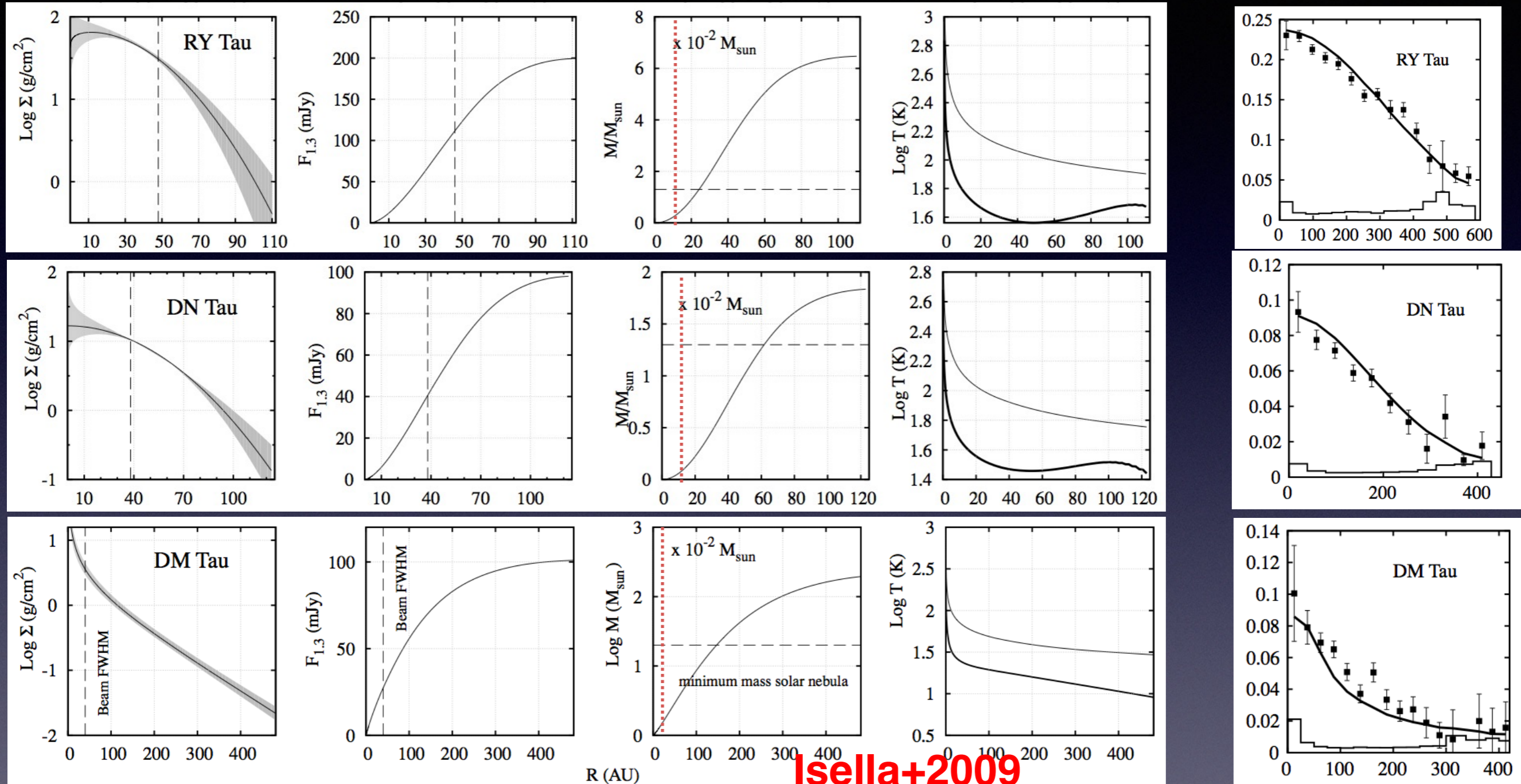
- **single**-wavelength continuum
- **multi**-wavelength continuum
- gas emission **spectral cubes**

## ► single or multiple sources in the FOV

## ► fast enough for survey analysis



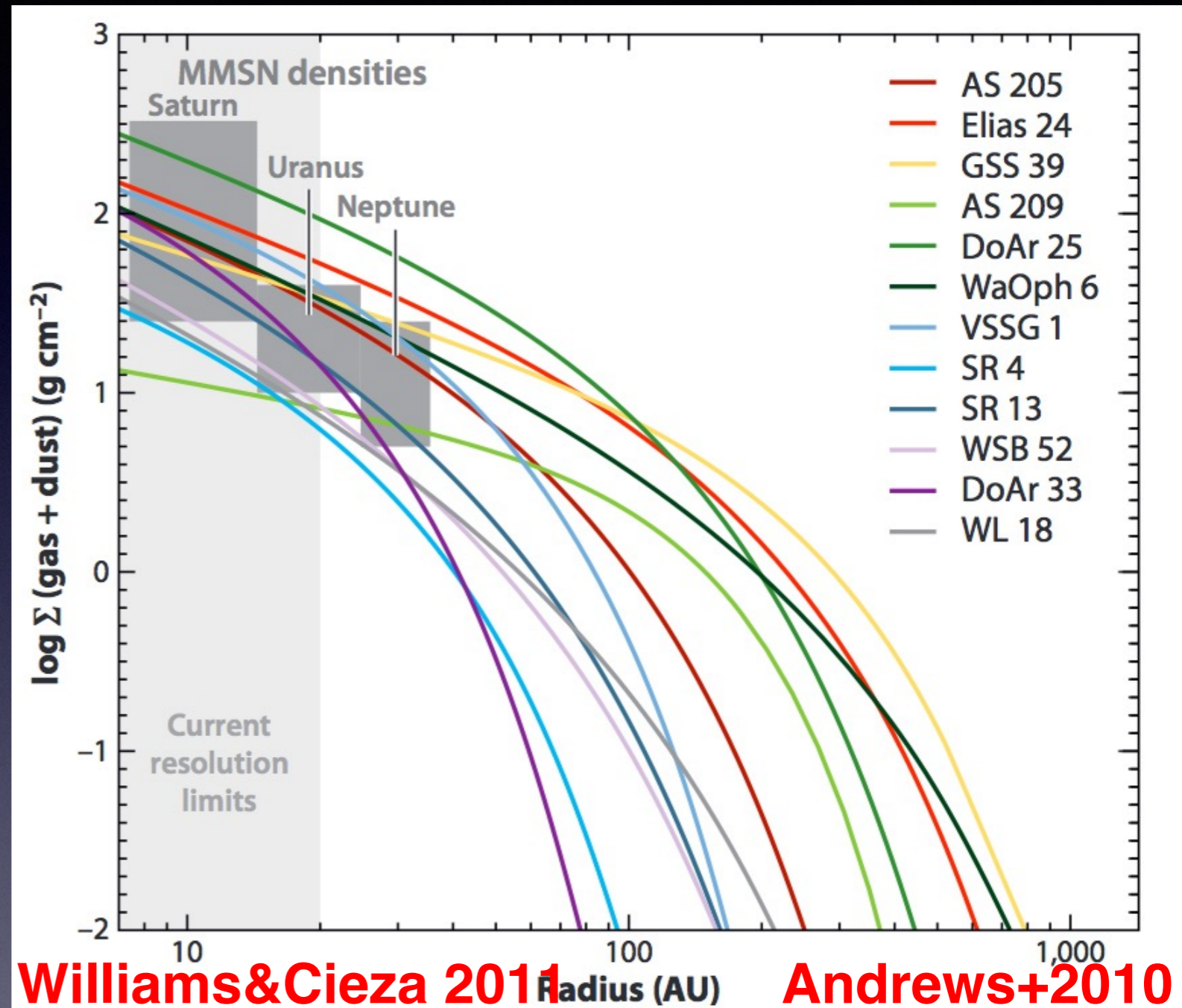
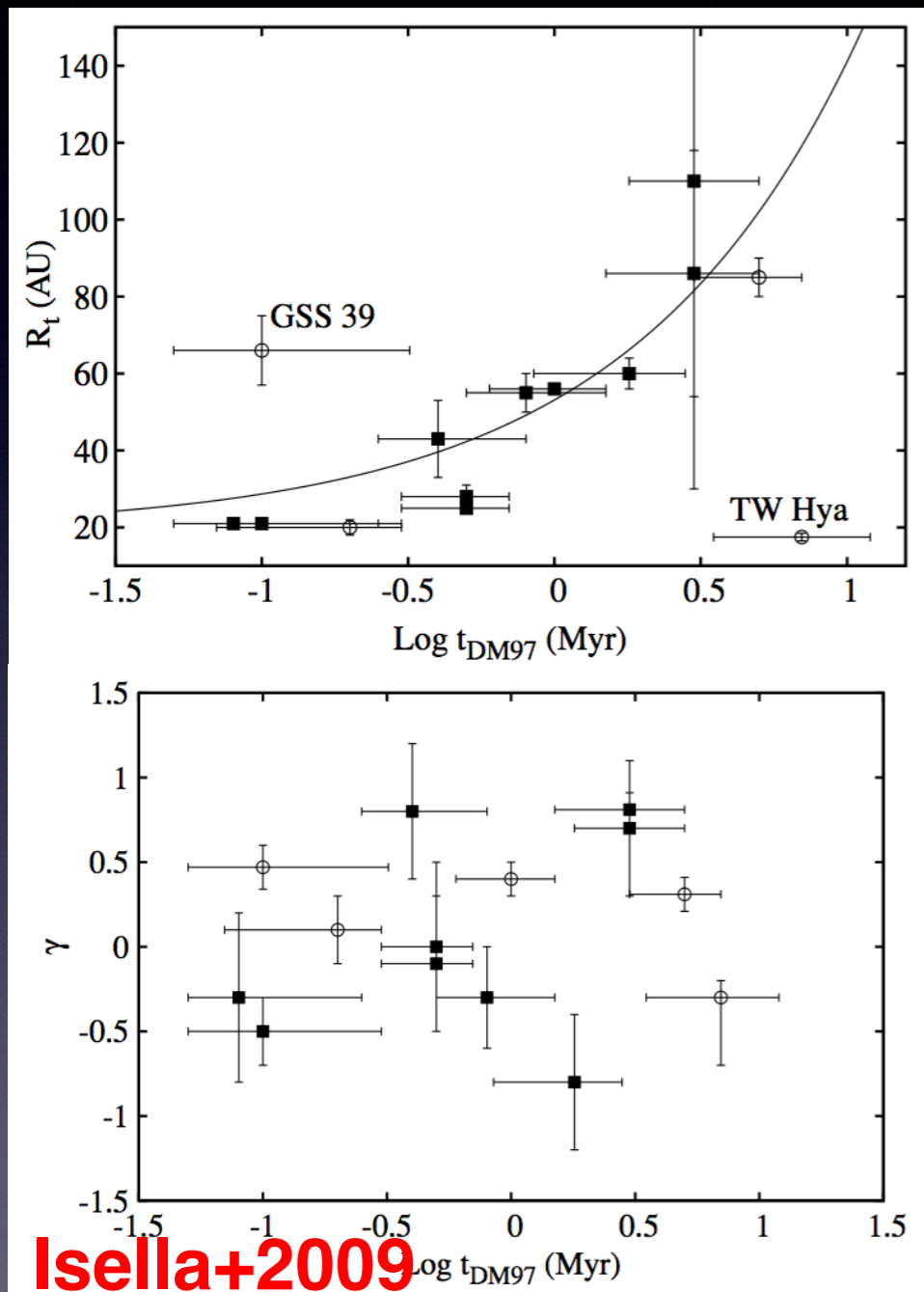
# Examples of pre-ALMA results



$$\Sigma(R, t) = \Sigma_t \left( \frac{R_t}{R} \right)^\gamma \times \exp \left\{ -\frac{1}{2(2-\gamma)} \left[ \left( \frac{R}{R_t} \right)^{(2-\gamma)} - 1 \right] \right\}$$

- Data generally well described, note limited angular resolution

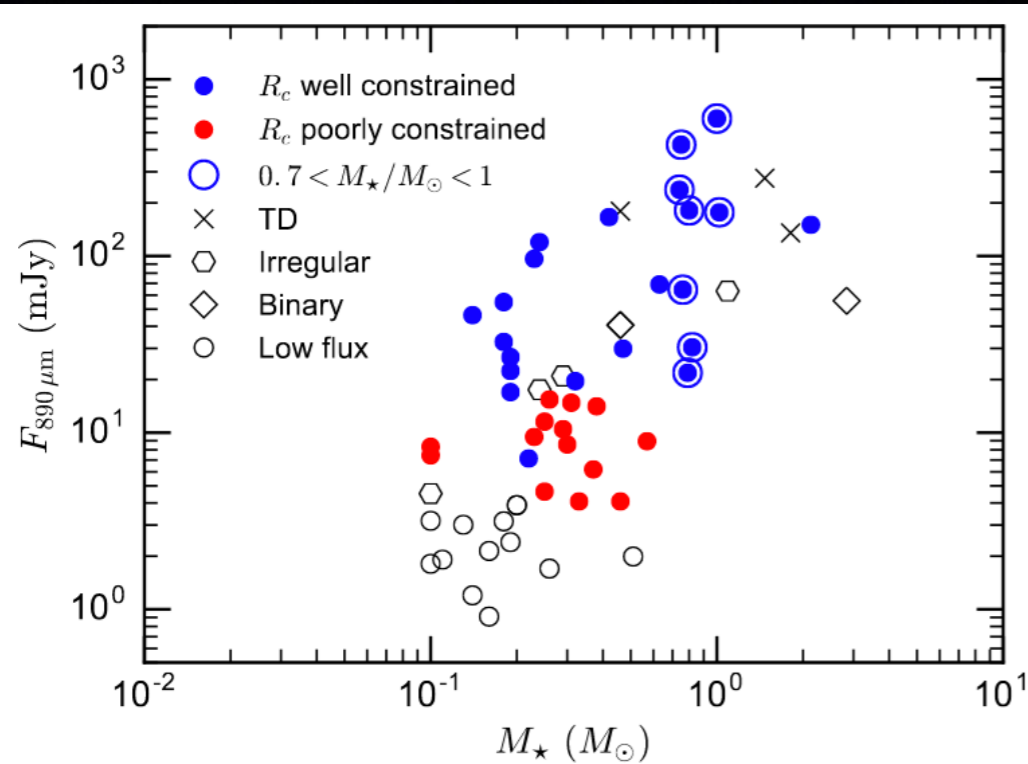
# Examples of pre-ALMA results



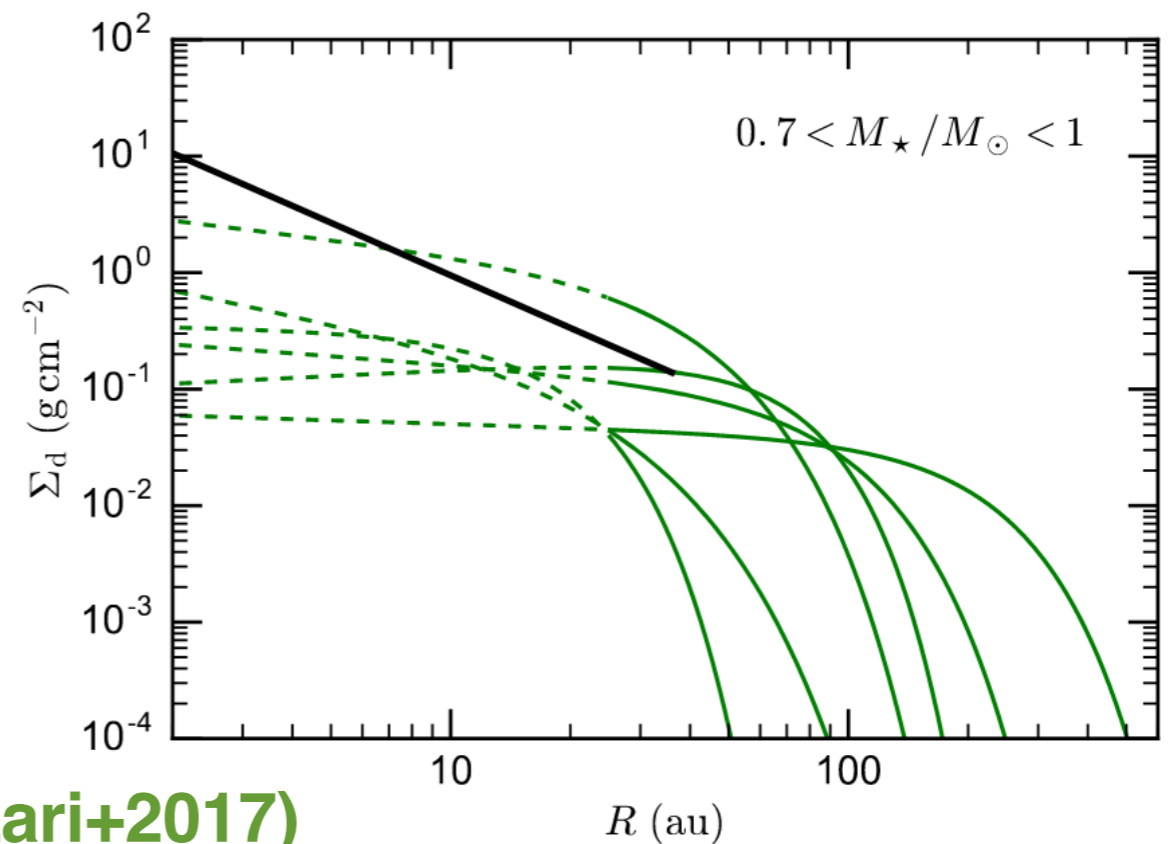
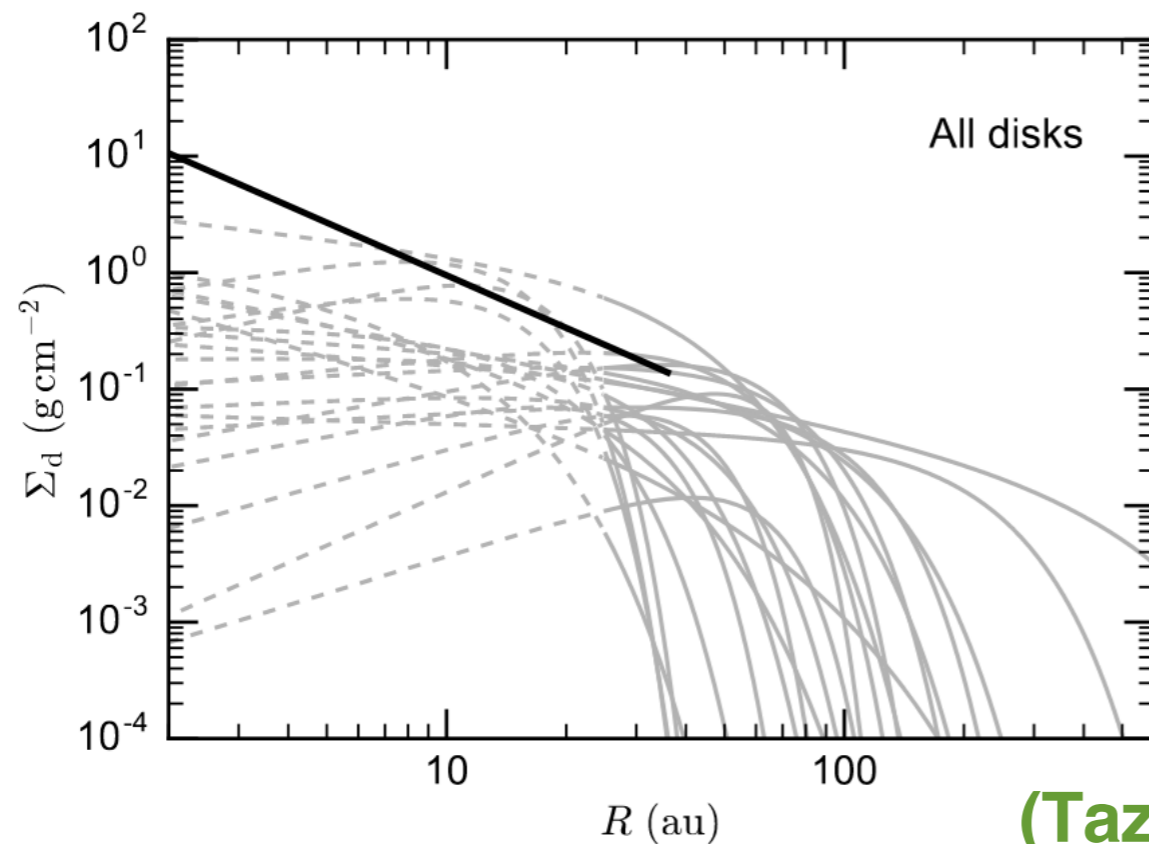
- Extract  $N$  random samples from “Taurus” applying the same selection biases as expected in the other region. Method first applied by Andrews+2013

# Surface density distribution

Powered by  
Galaro  
(Tazzari+2018)



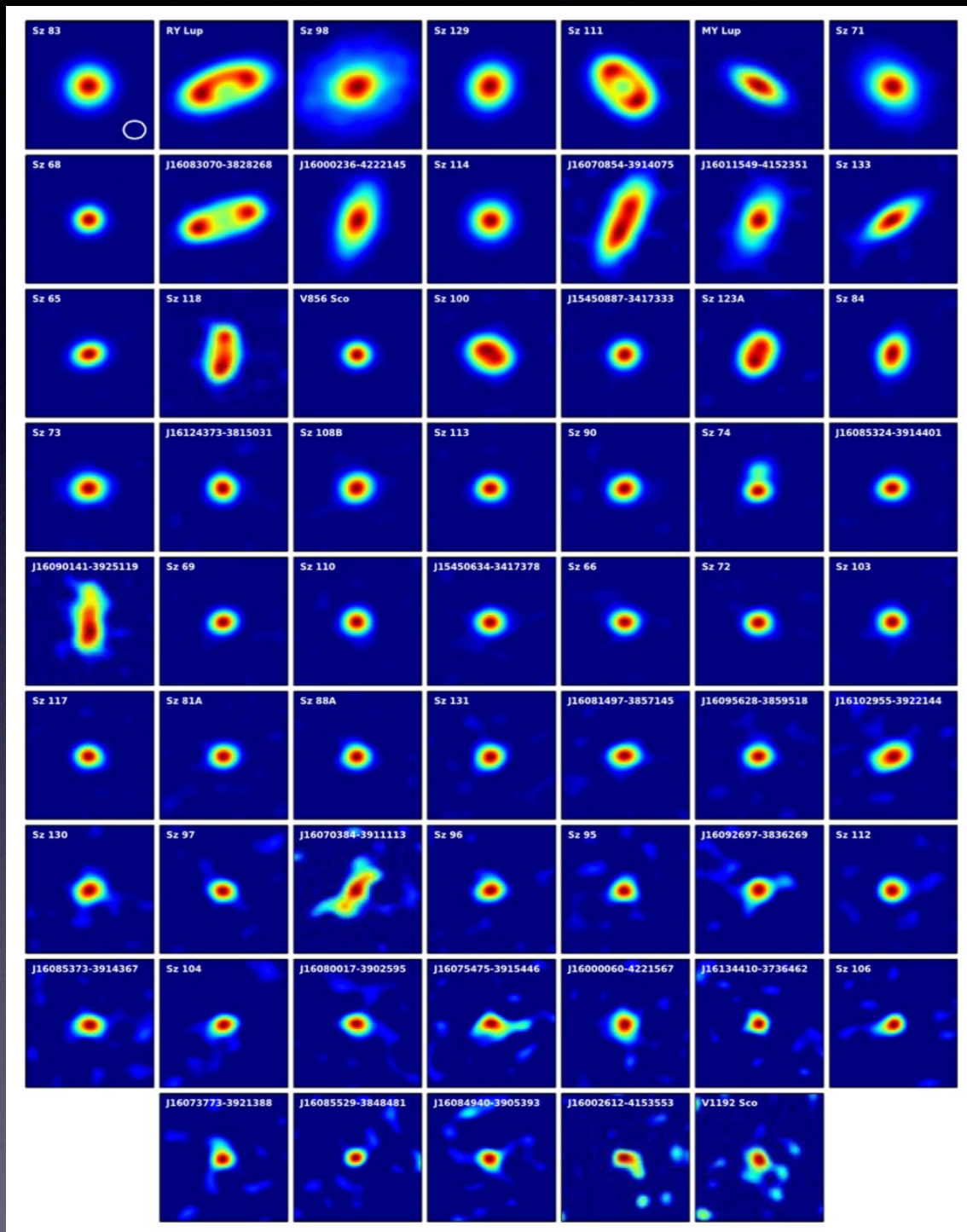
- First systematic/complete analysis of surface density distribution of solids in disks
- Compact disks ( $R < 50 \text{ AU}$ ) are up to  $\sim 30\text{-}40\%$  of the population



(Tazzari+2017)

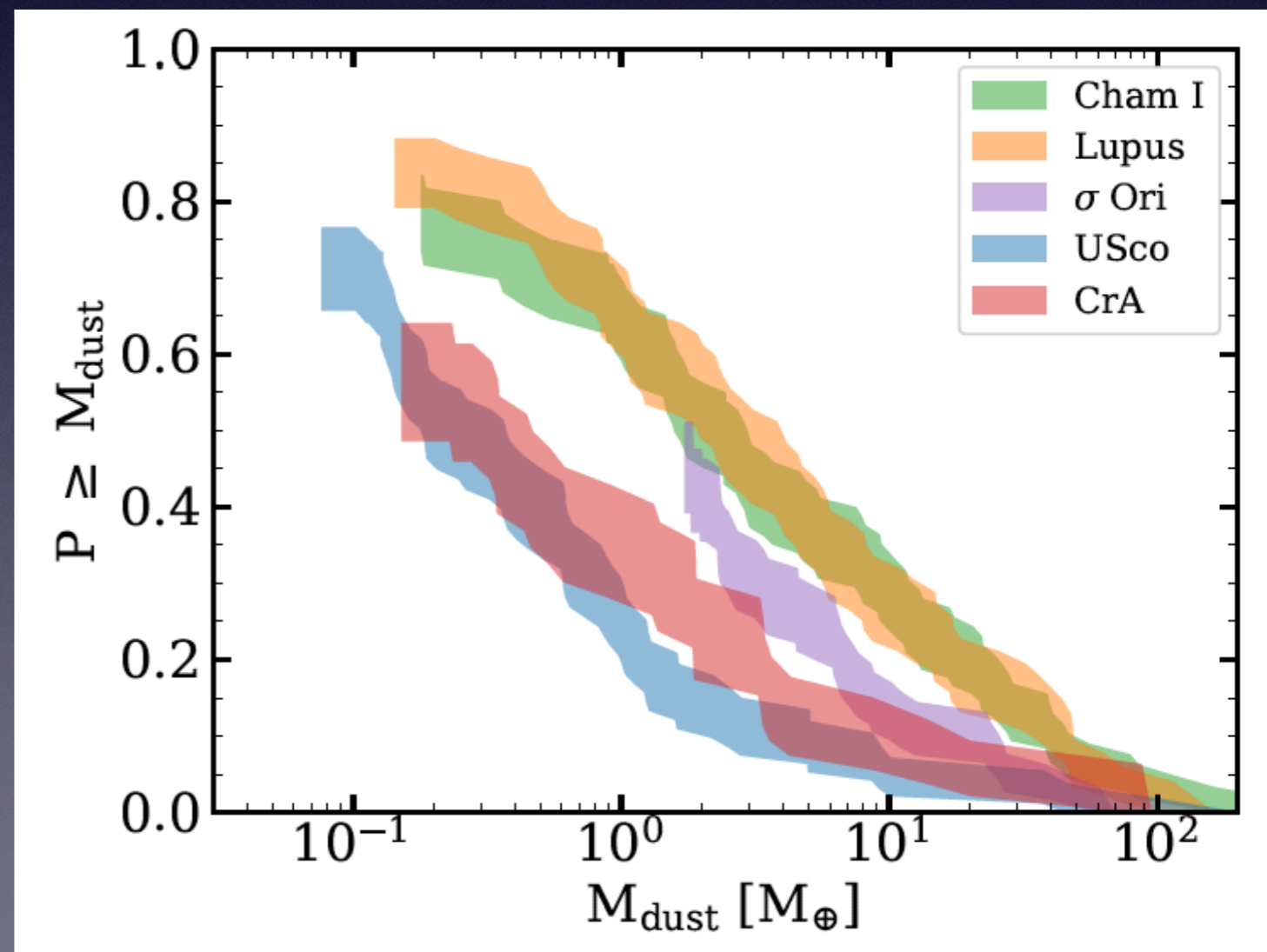
# Full fit not always possible: order of magnitude estimates technique

- Initial surveys revealed a gradual decay (factor  $\sim 4$  in  $\sim 5$  Myr)
- Dust content is relatively low
- Estimates rely on simple assumption on temperature structure and dust opacity



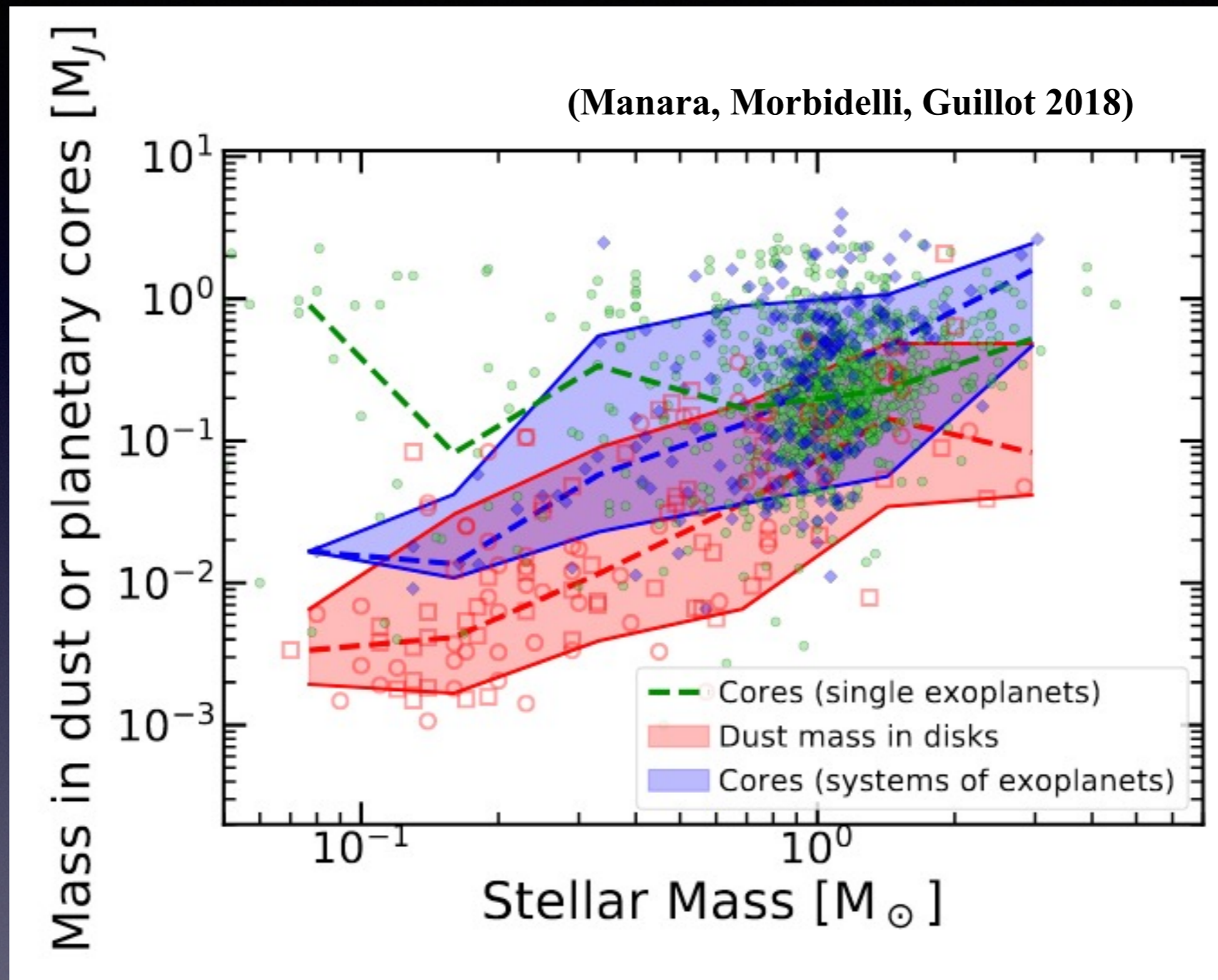
Andsell+2016

(see also Pascucci+2016, Andsell+2017, Barenfeld+2016, Cazzoletti+2019, Williams+2019, Testi+2022)



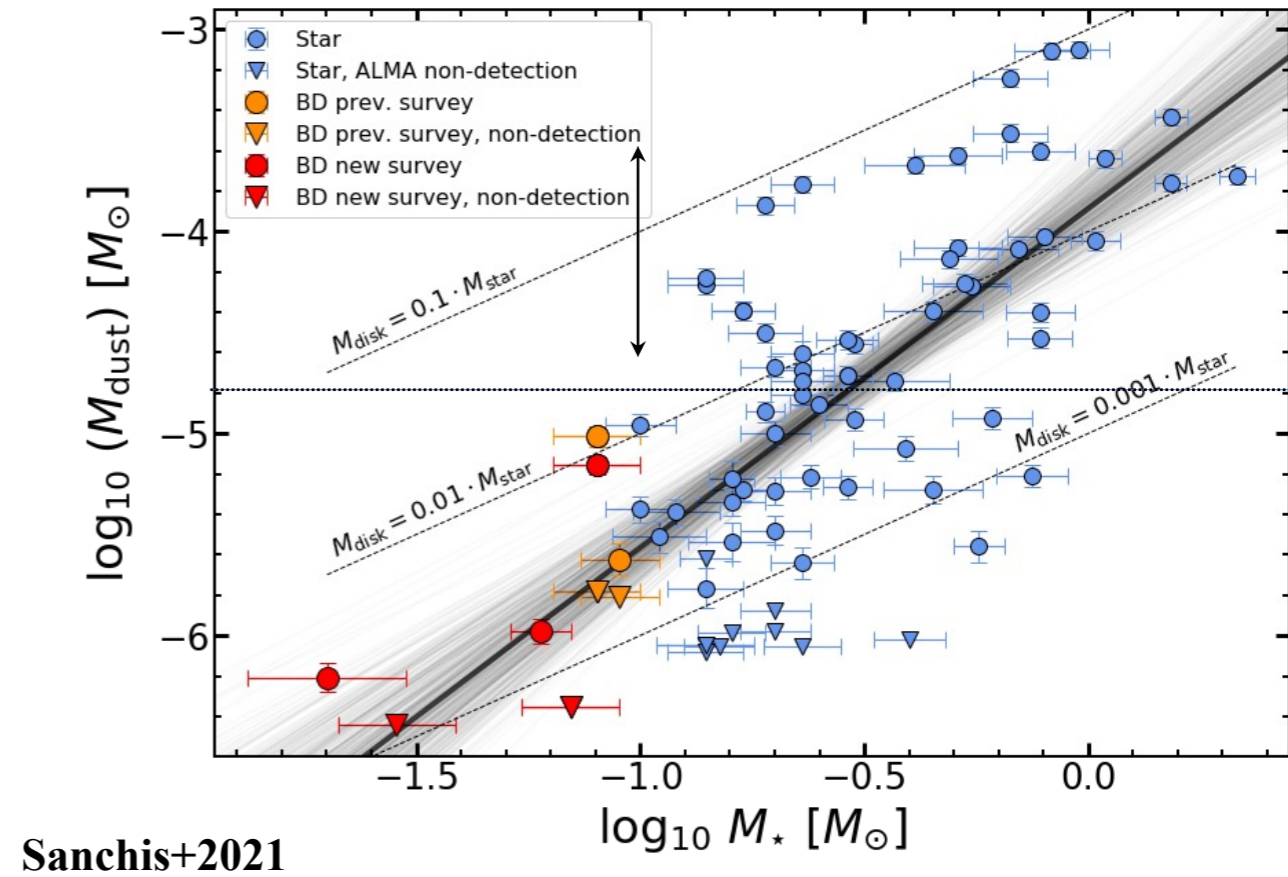
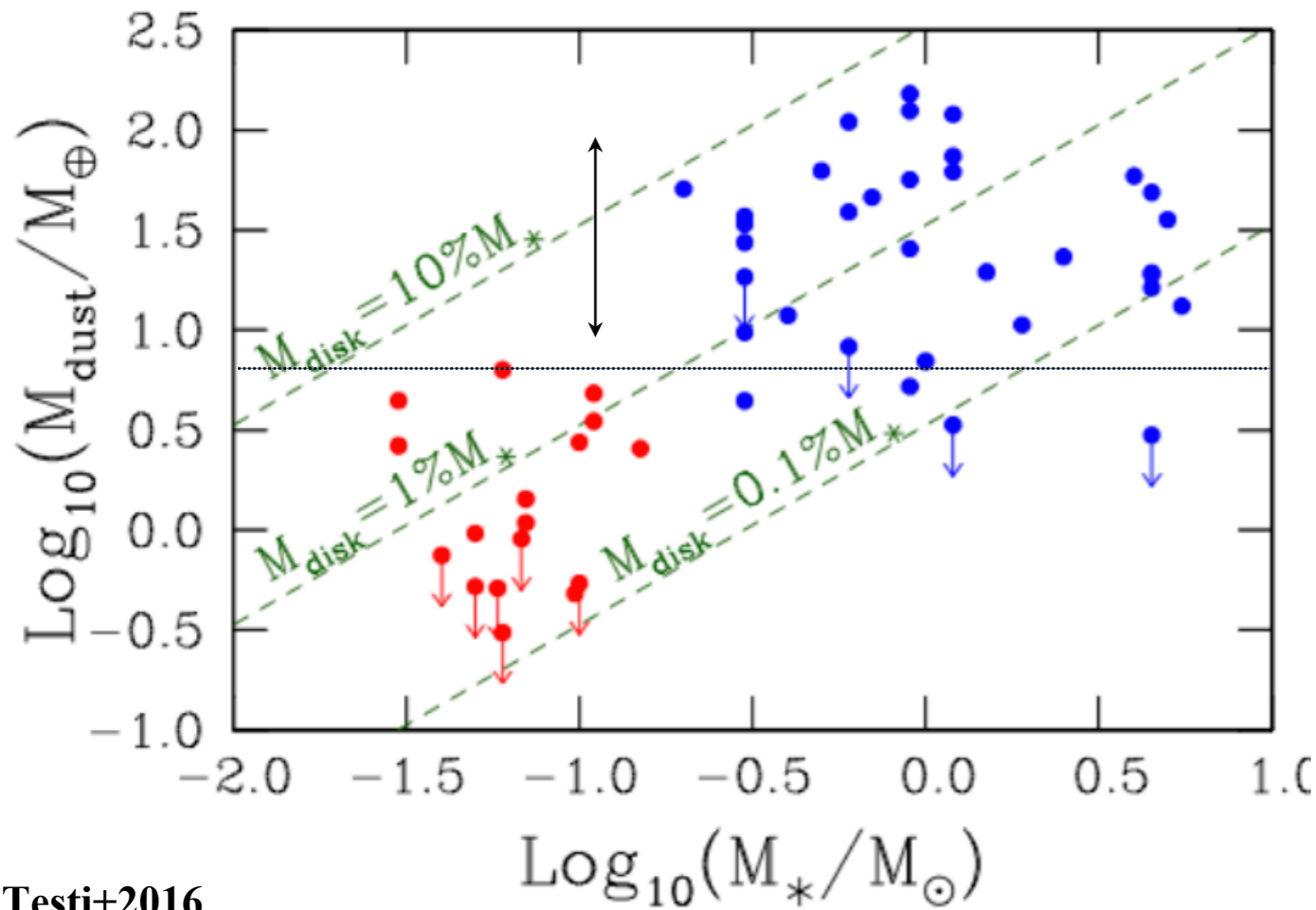


# Solids in planets and disks



- 1-2Myr old disks do not contain enough solids
  - Consistent with the latest suggestions of Jupiter core growth (Kruijer+2017)

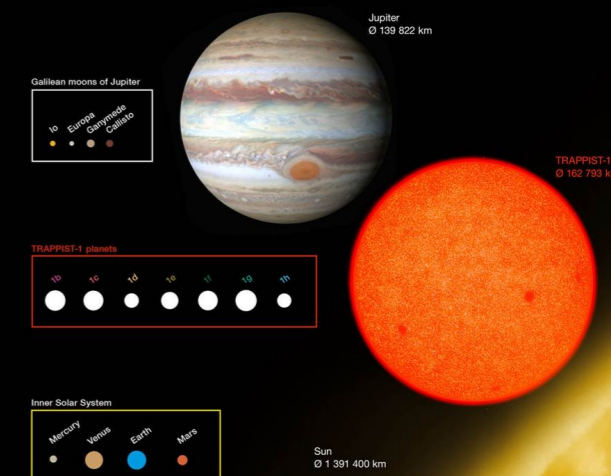
# Deficit of solids in BD disks



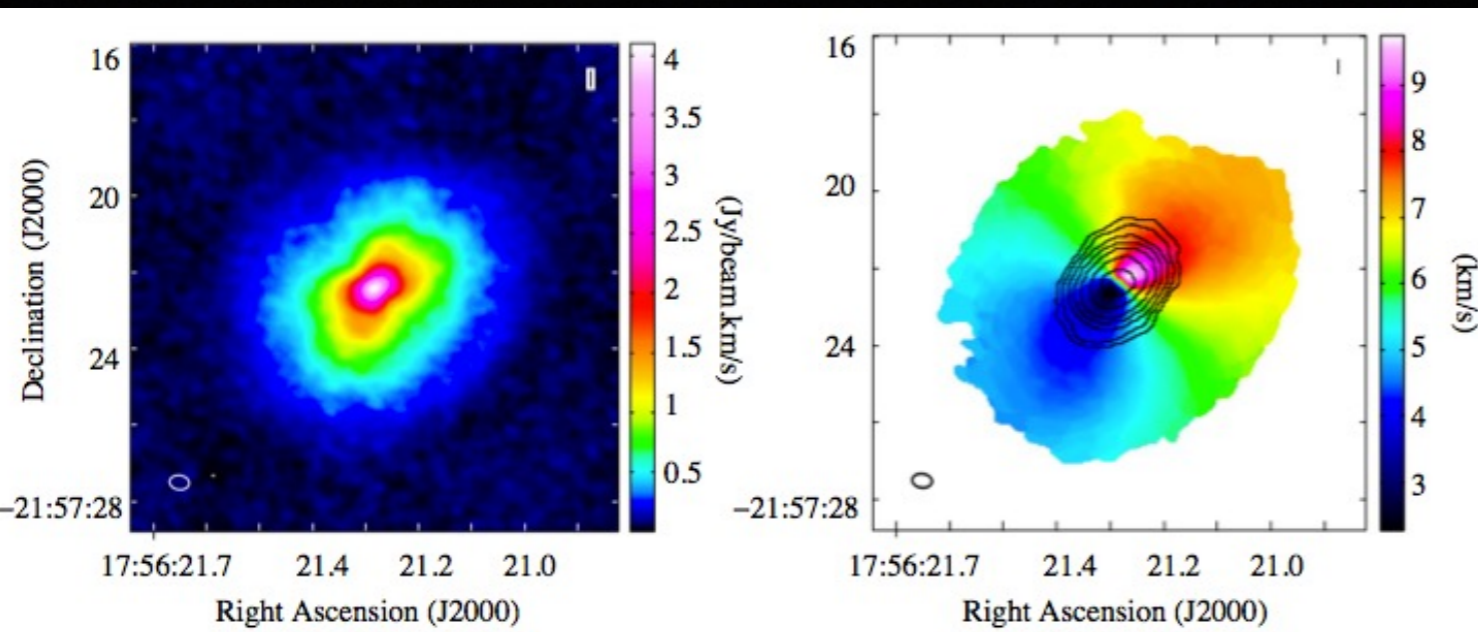
- Estimated solids mass in BD disks is too low to form the known exoplanets around BDs

## Size Comparison

between TRAPPIST-1 system, Galilean moons of Jupiter and the inner Solar System

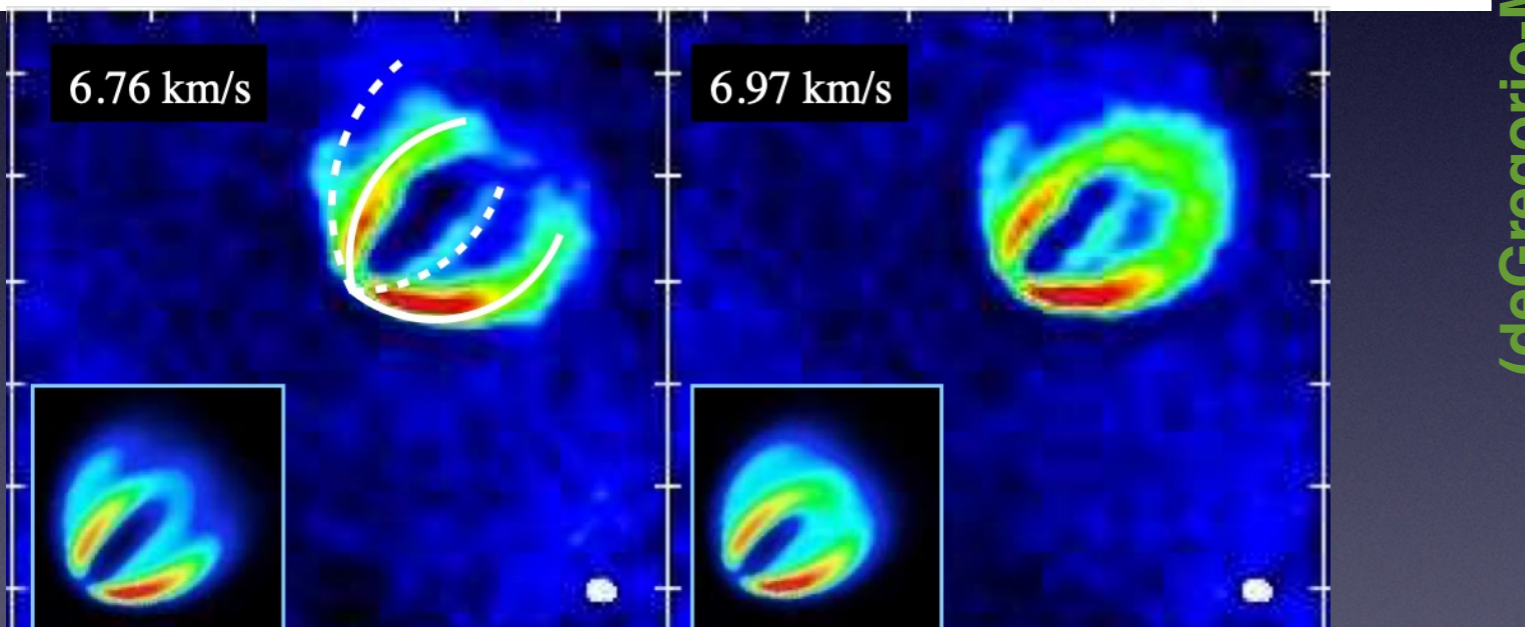


# HD 163296 as seen by ALMA

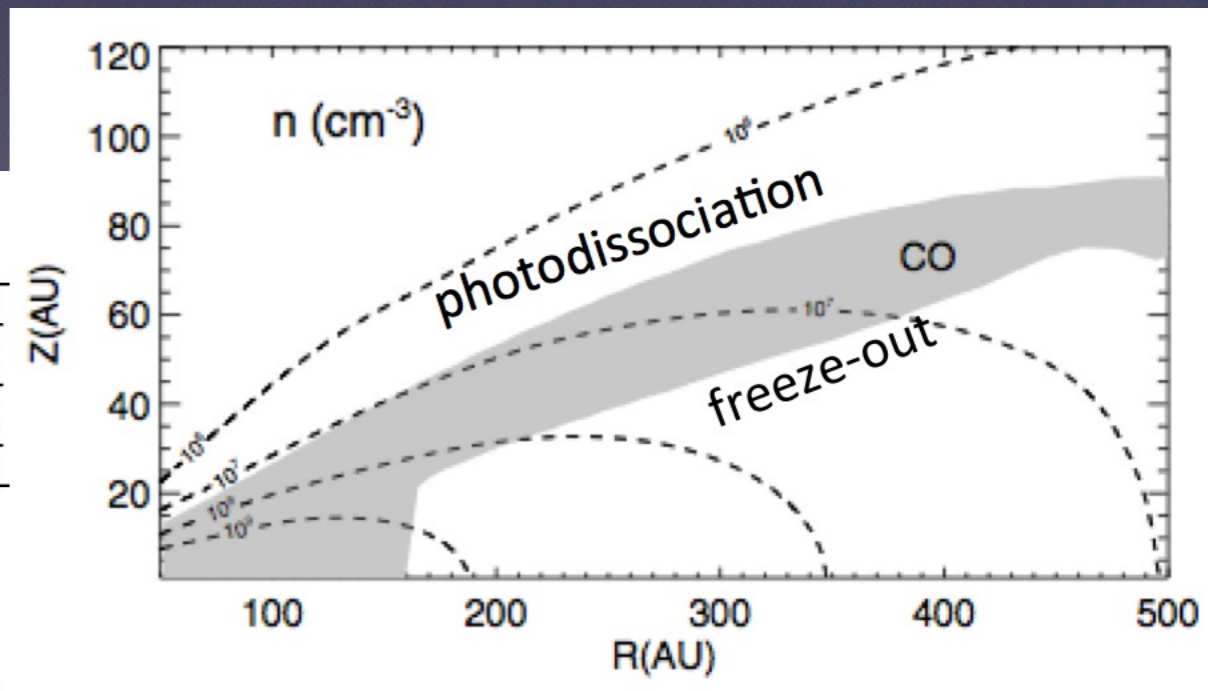
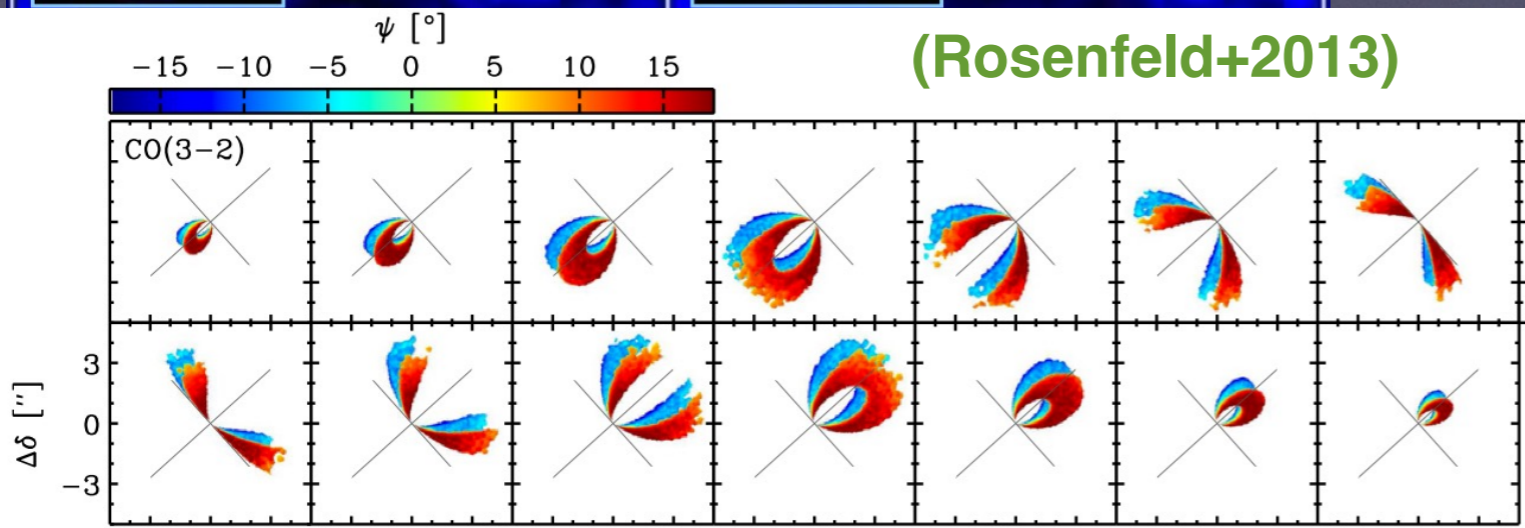


(deGregorio-Monsalvo+2013)

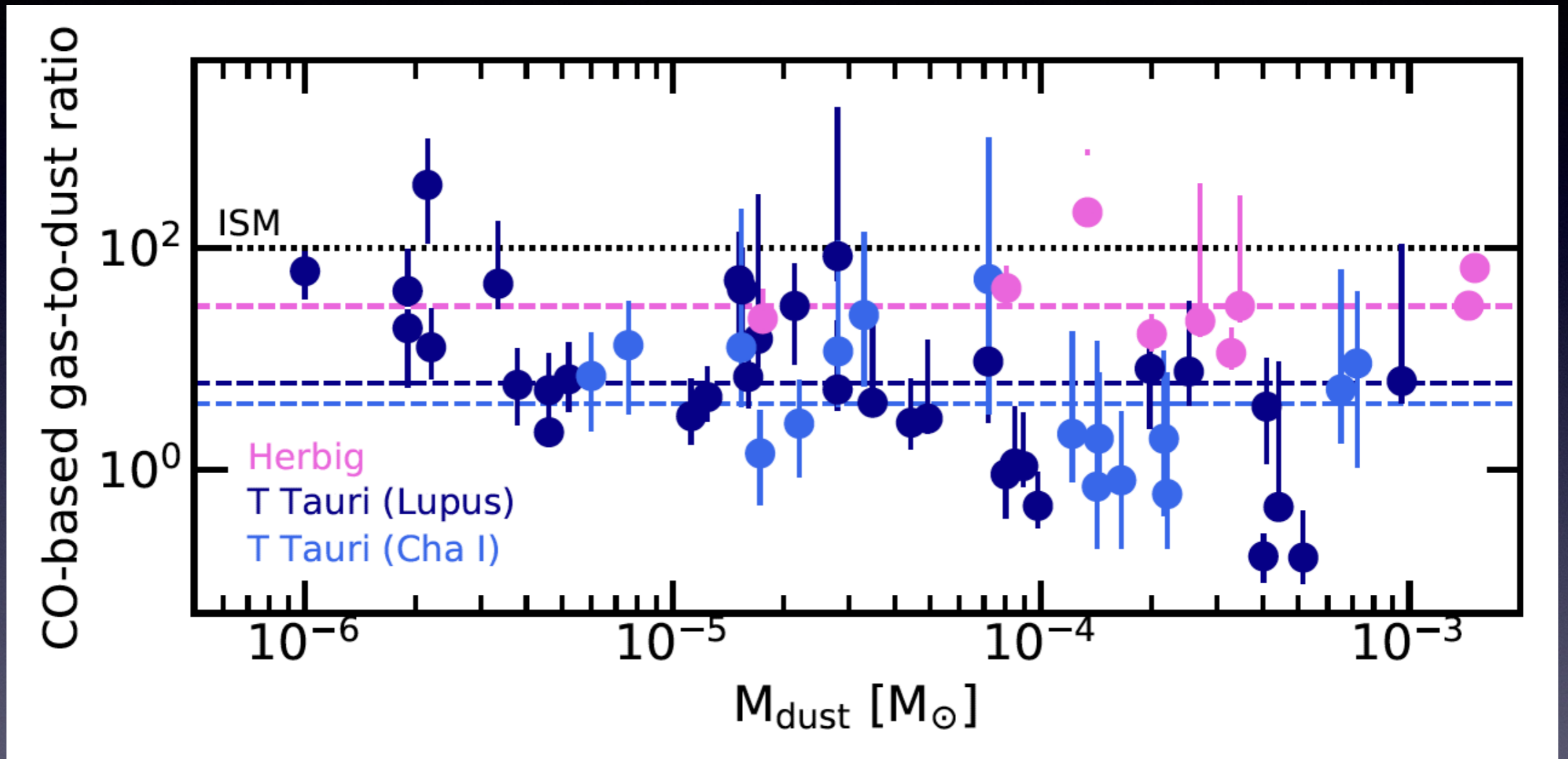
- Direct measurement of disk flaring and CO depletion on the mid plane



(Rosenfeld+2013)



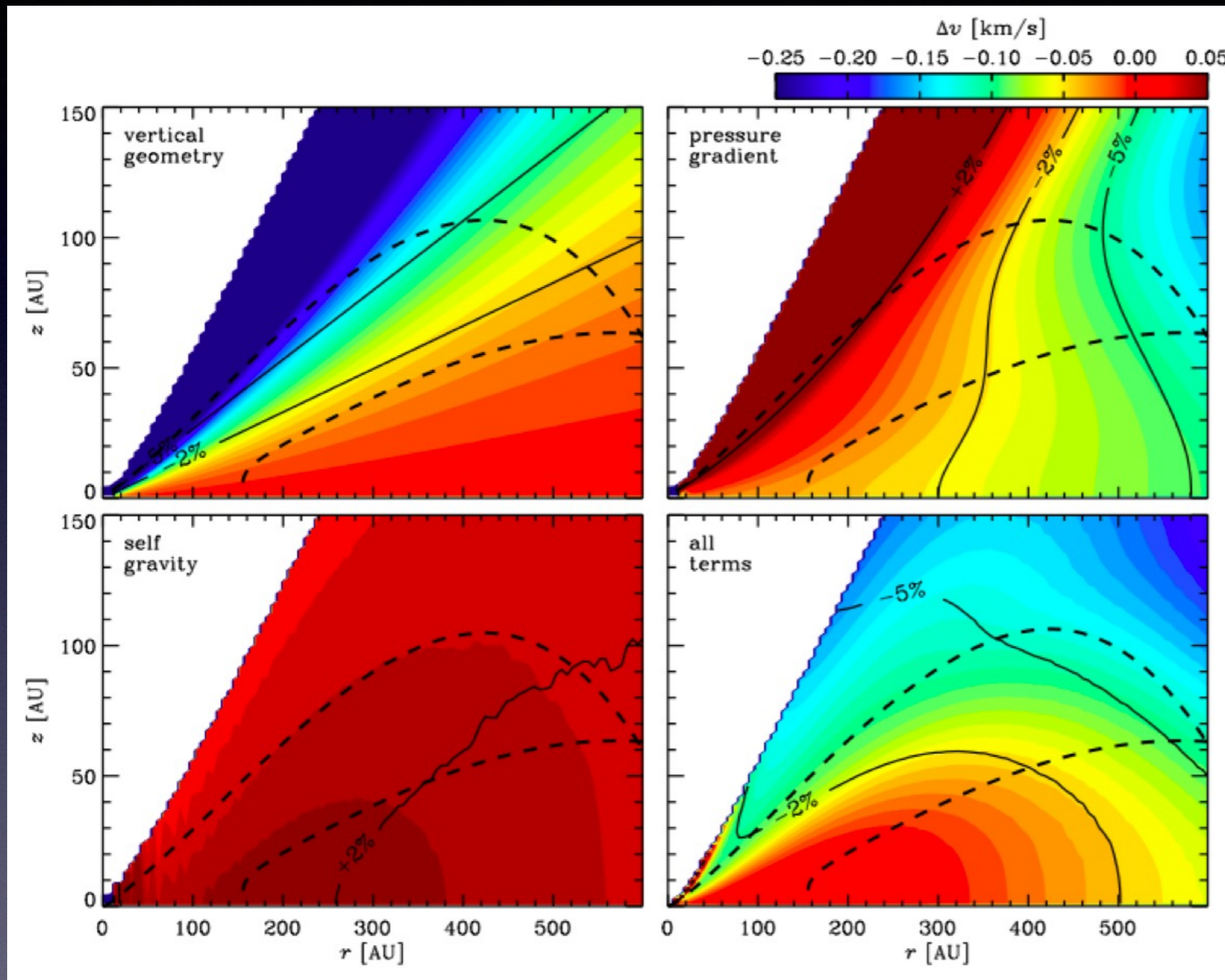
# CO-based gas masses



(Miotello et al. 2022)

- Based on disk thermochemical modelling
- Truly low gas masses or “chemical” model deficit?

# Gas kinematics



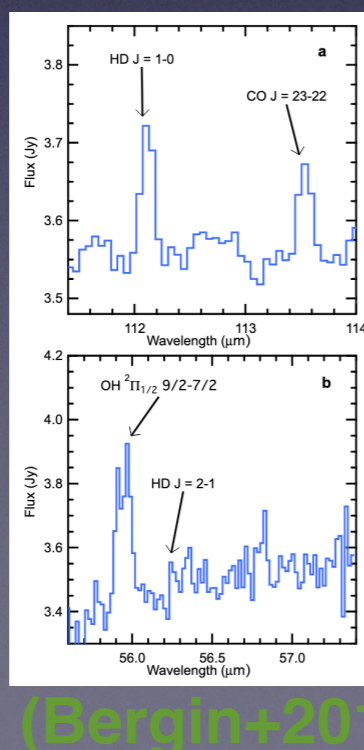
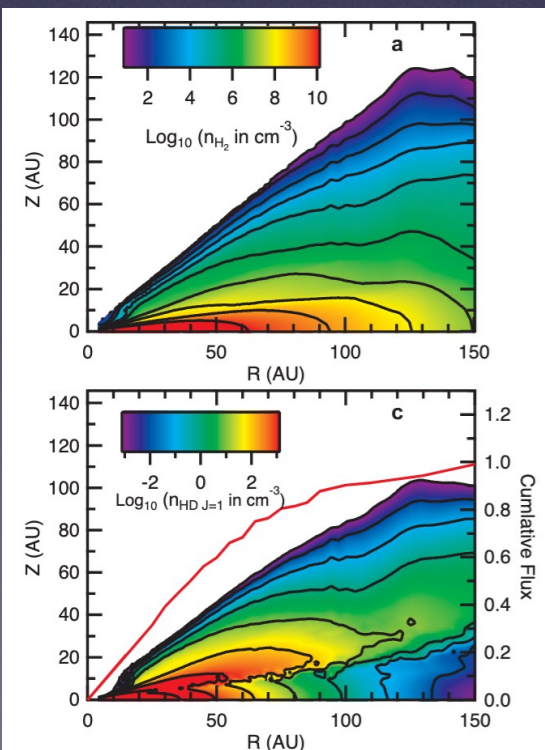
- Potentially a direct measurement of the disk self-gravity

(Rosenfeld et al. 2013)

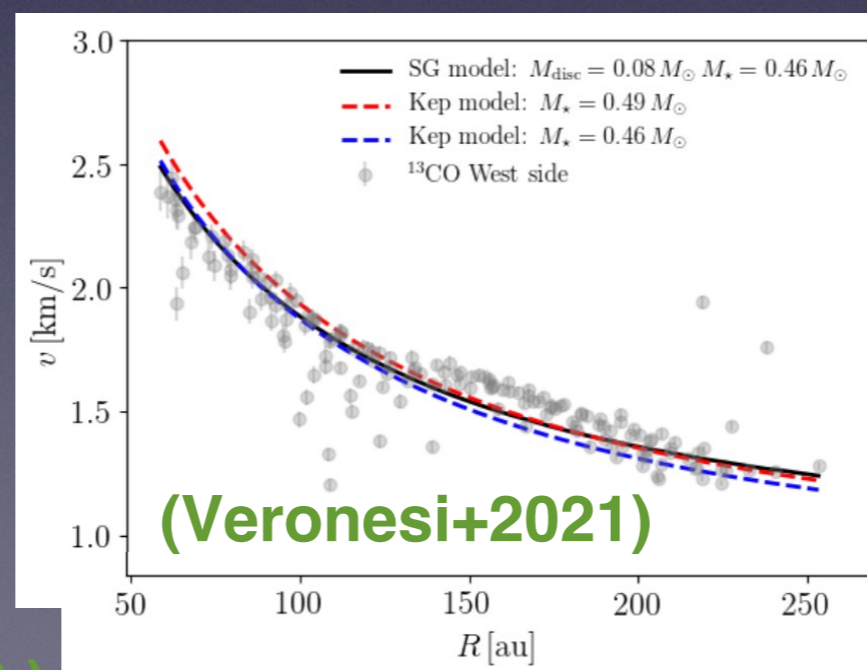
- Not exactly Keplerian
- Largest effect is the pressure term 5%, self gravity 0.1-0.5%

# Dust mass and disk mass

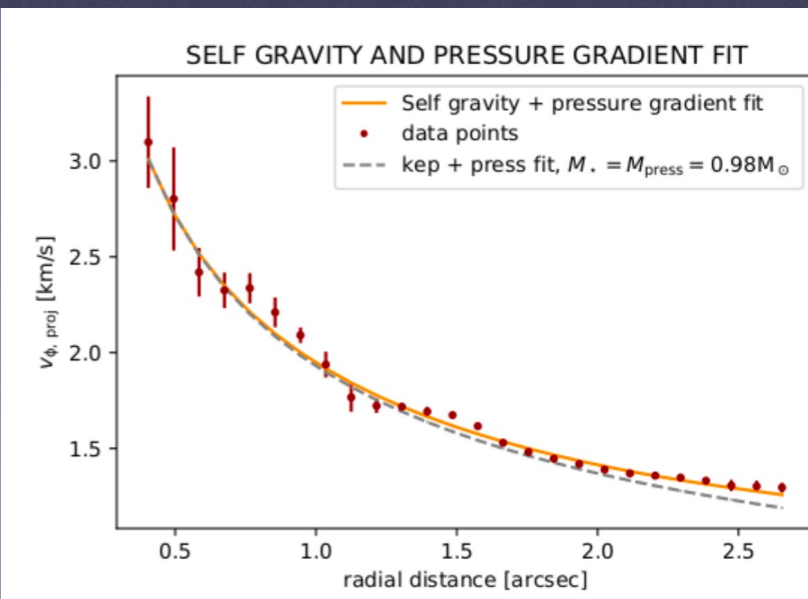
- Dust emission traces approx 0.01 of the H<sub>2</sub> mass
  - (by comparison, gas-phase CO emission traces  $\llll 1e-5$ , depending on how much of the CO mass is in solids and on the details of chemistry and photodissociation)
- Carefully estimated dust masses are within a factor 2-3 of “robust” disk mass estimates



(Bergin+2013)

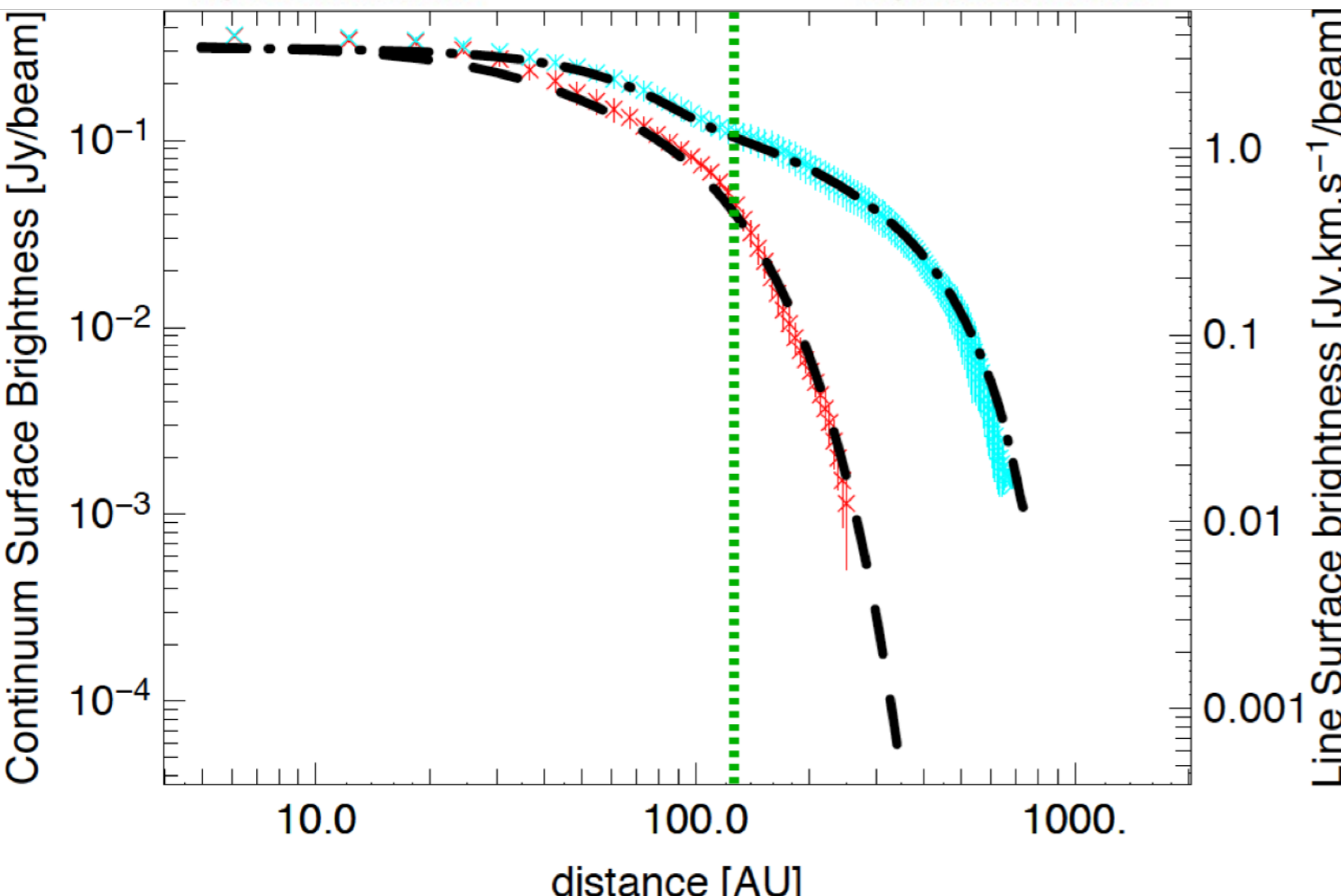
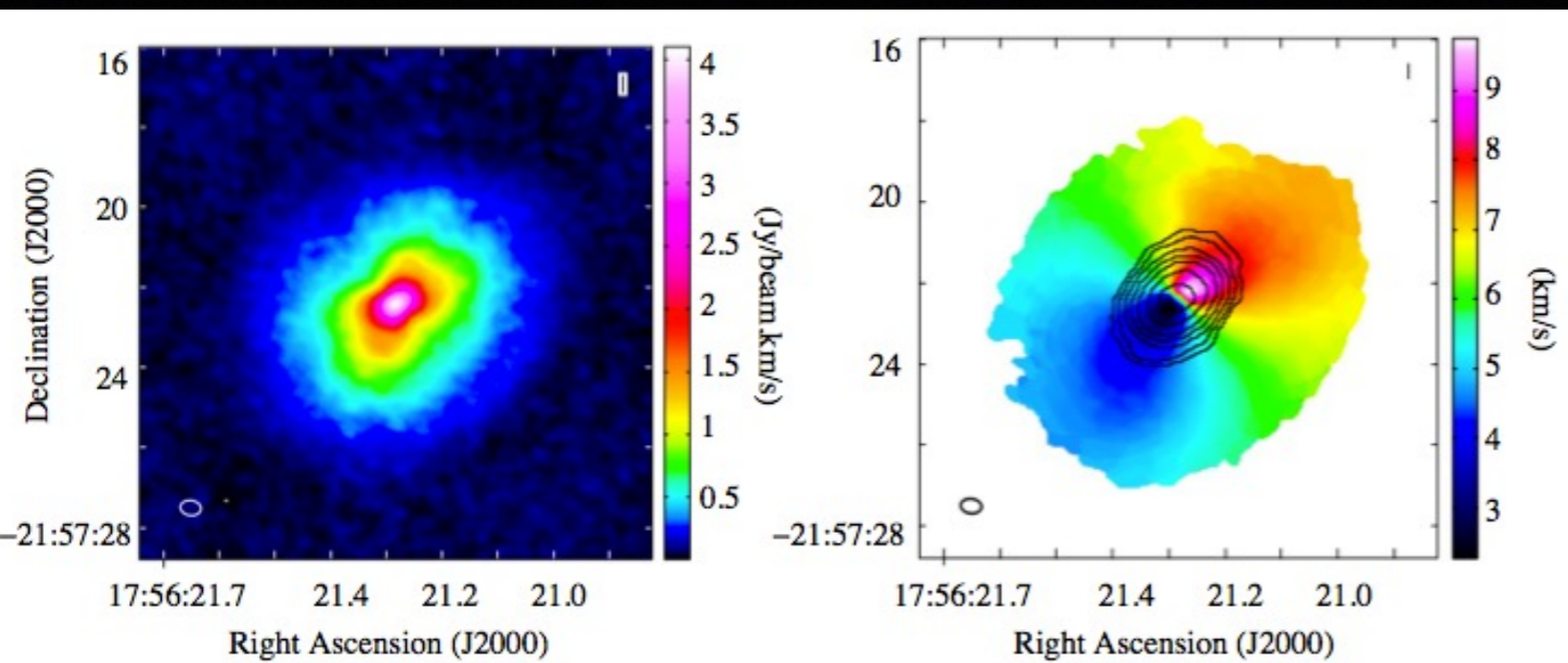


(Veronesi+2021)

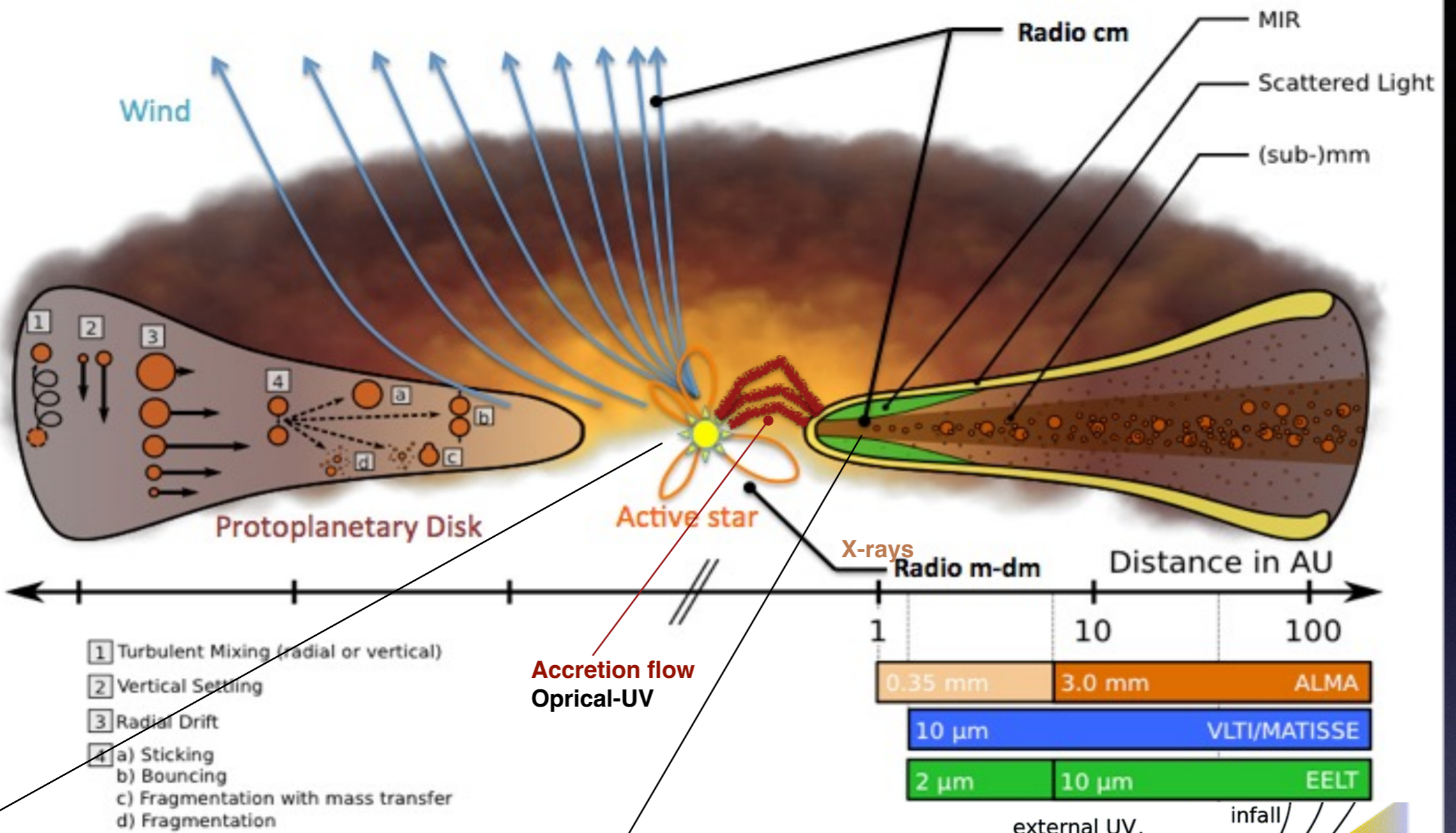


(Rampinelli+2022)

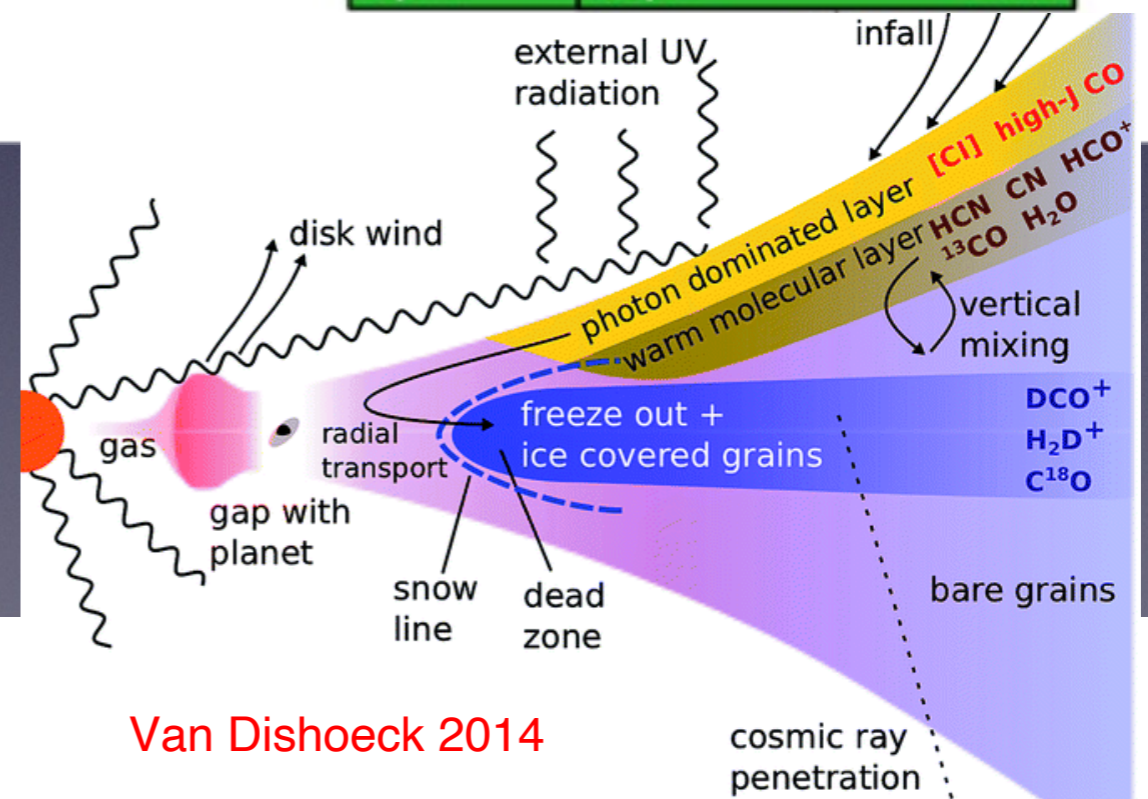
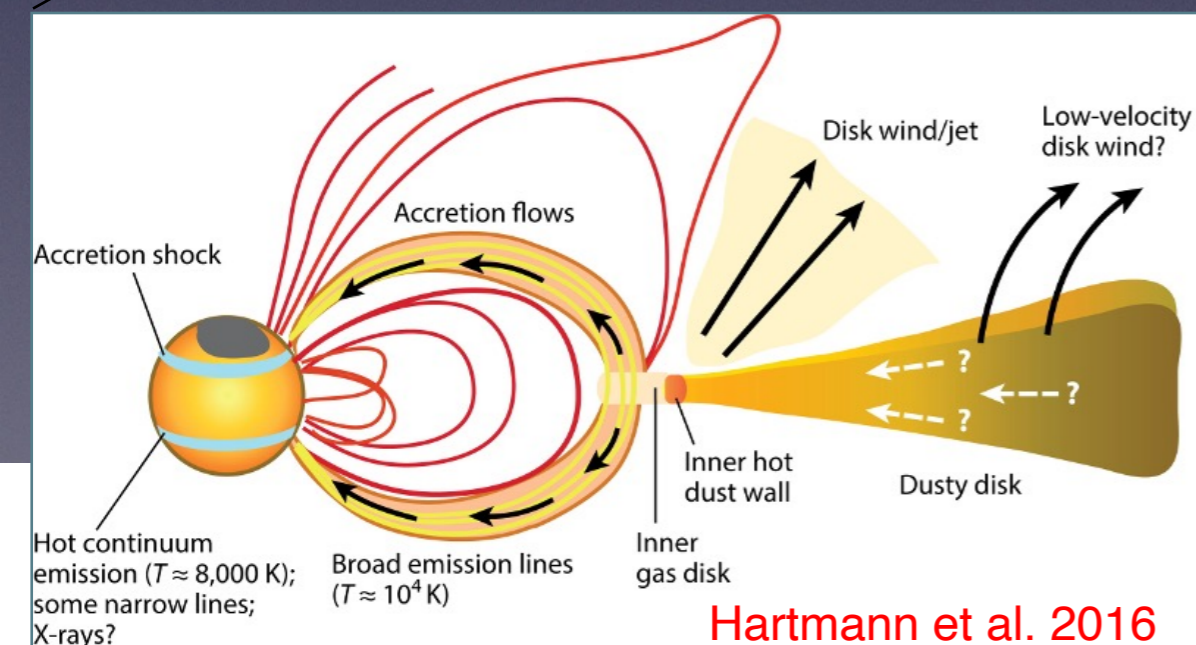
# HD 163296 as seen by ALMA



- Extent of the CO disk is much larger than that of the mm-grains disk
- Qualitative behaviour as expected from viscous spreading and migration of the larger grains



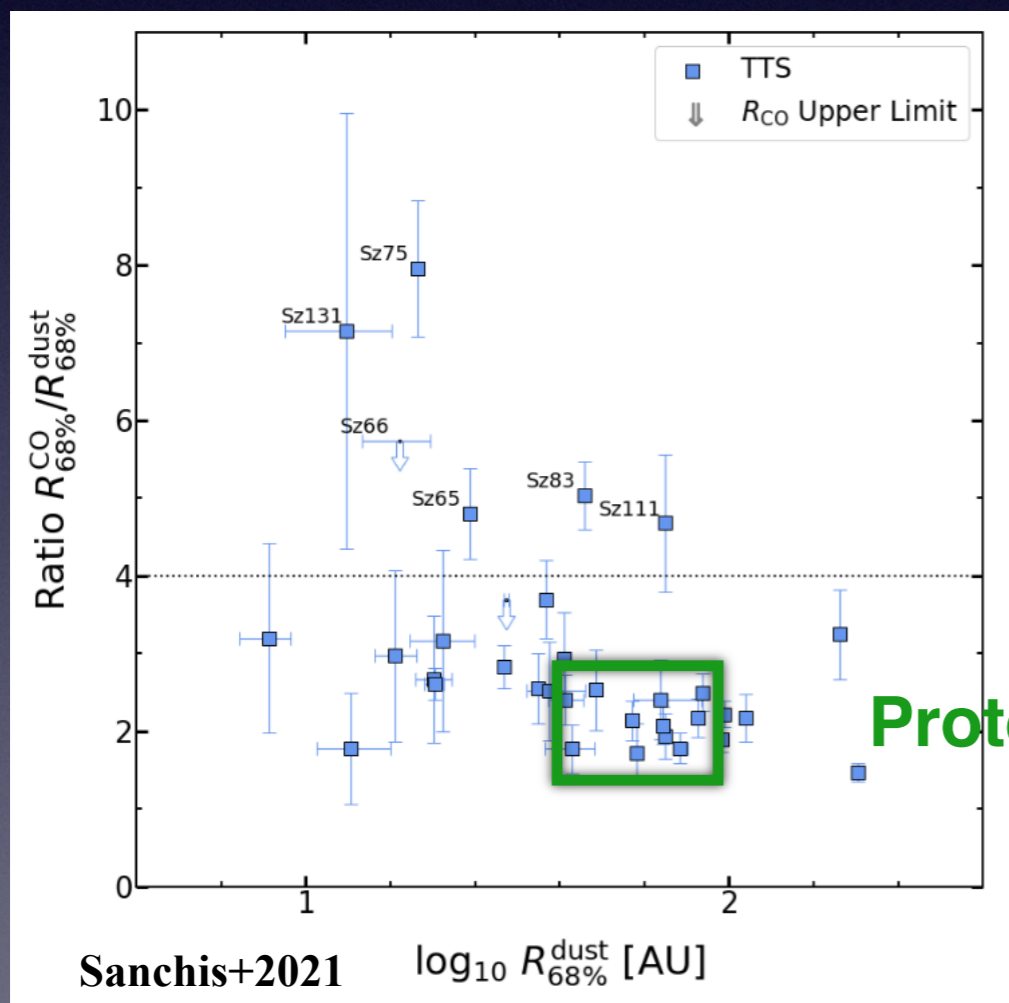
Testi et al. 2014/15



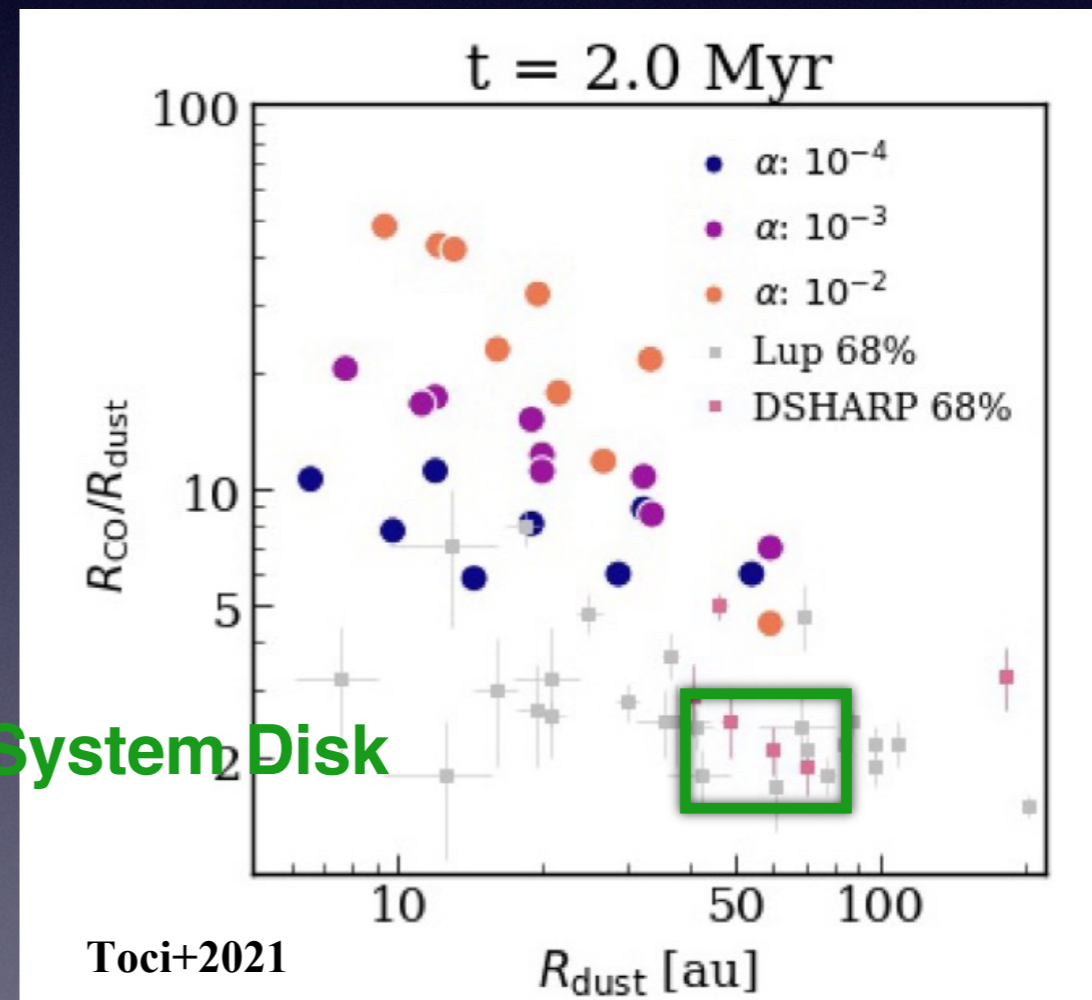


# Gas and dust

- Continuum vs. Gas radii show surprisingly tight correlation
- This is surprising and needs to be better understood

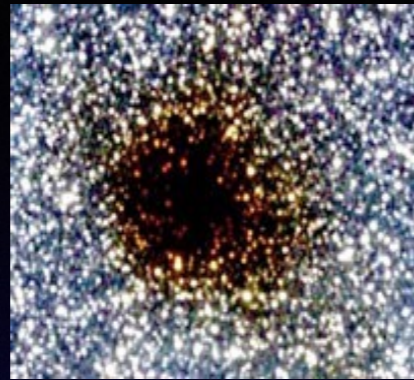
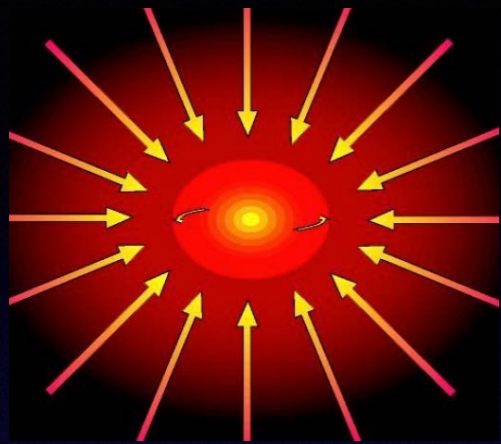


- $R_{CO} \sim 2 R_{dust}$

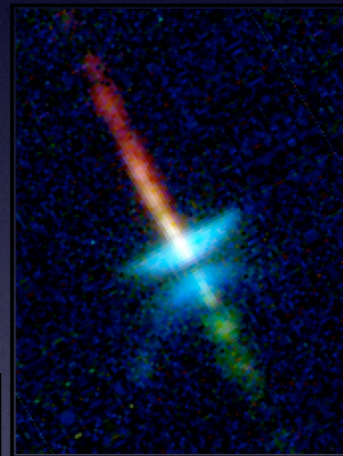
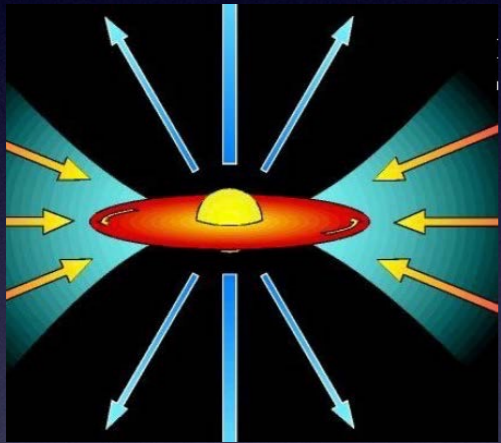


- Not consistent with steady viscous evolution

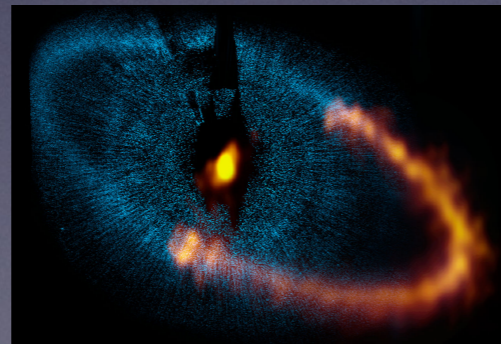
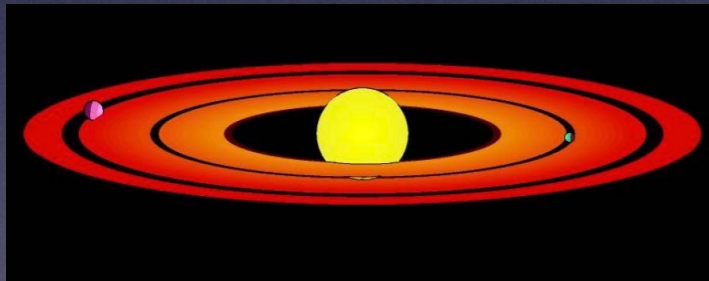
# From Cores to Planetary Systems



Core



Disk



Debris Disk

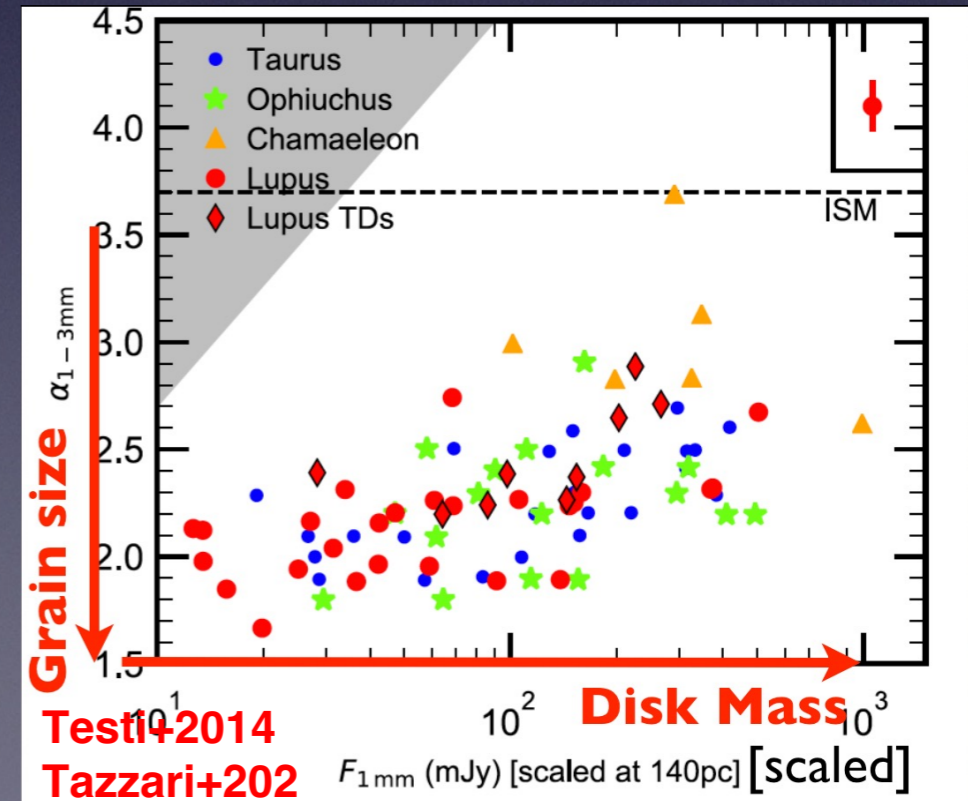


Grain growth

Very difficult to grow beyond 10-100  $\mu\text{m}$   
(Ossenkopf & Henning 1994; Ormel et al. 2009)

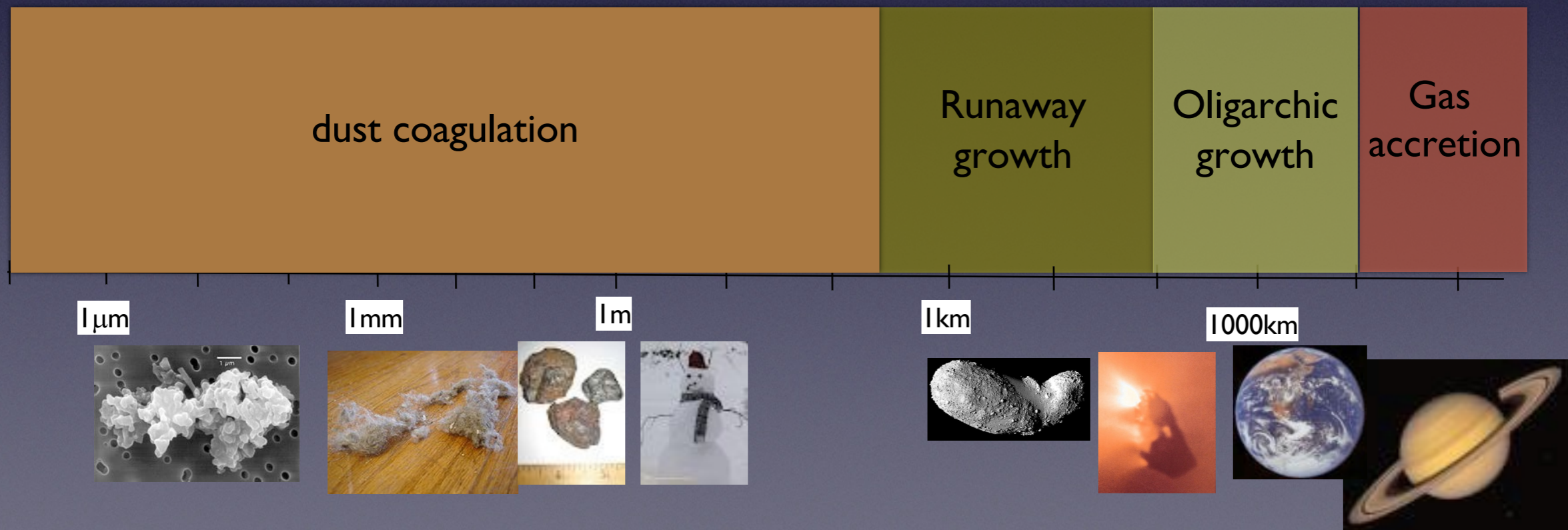
Evidence for growth to micron-size grains  
(Pagani et al. 2010)

Observational evidence for large grains  
(Beckwith & Sargent 1991)  
(Testi et al. 2003, Natta et al. 2007, Testi et al. 2014)



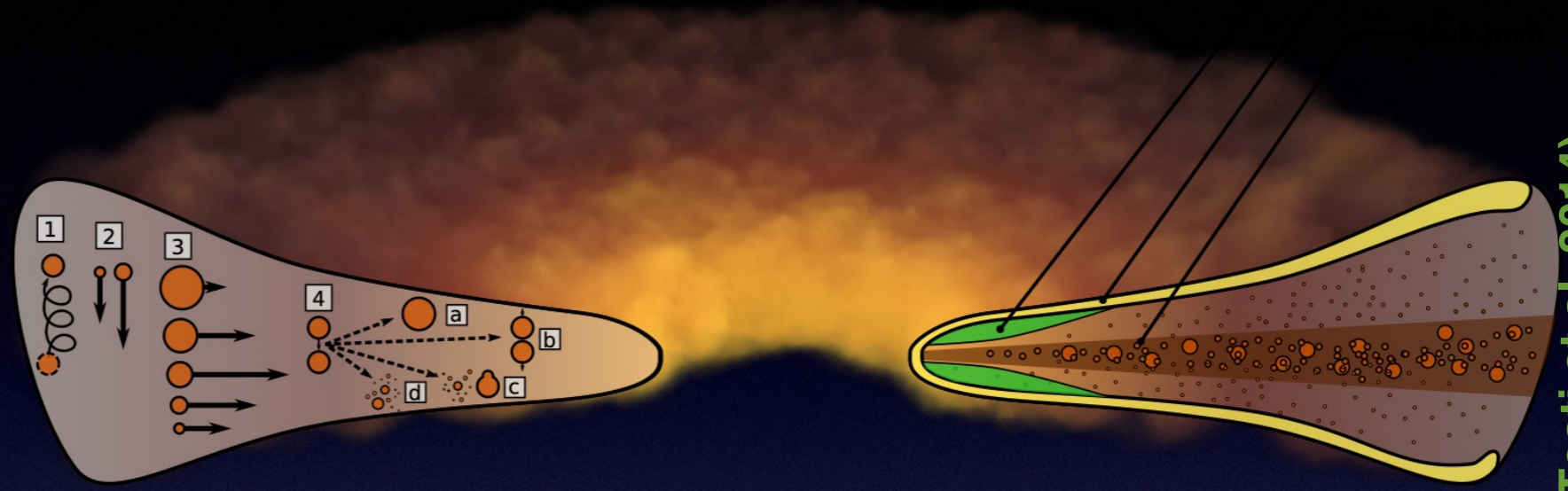
# Dust evolution

- The core-accretion scenario
  - Dust growth and planetesimals formation
  - Formation of rocky cores
  - Gas accretion from disk



# Dust evolution: grain growth processes

(Testi et al. 2014)



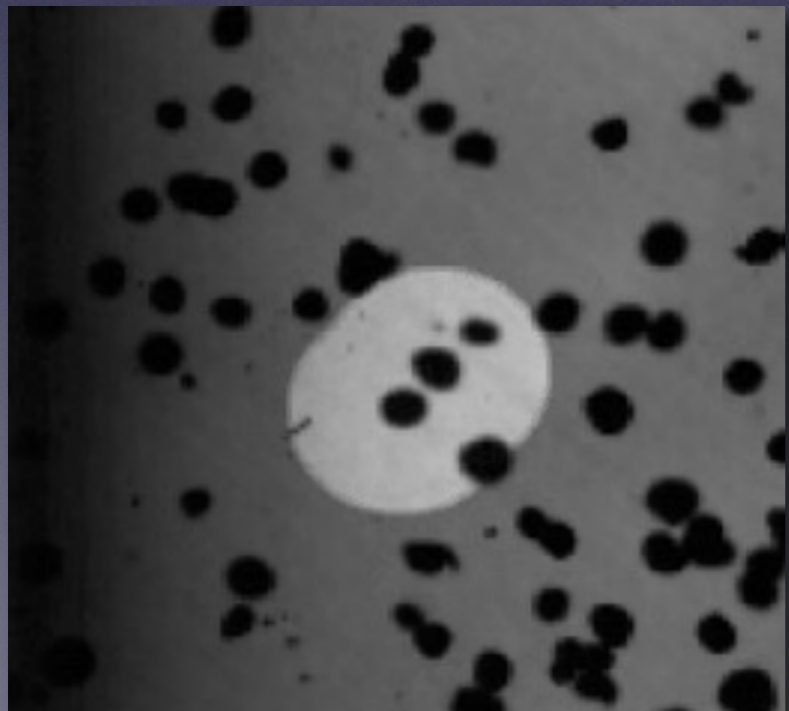
- 1 Turbulent Mixing (radial or vertical)
- 2 Vertical Settling
- 3 Radial Drift



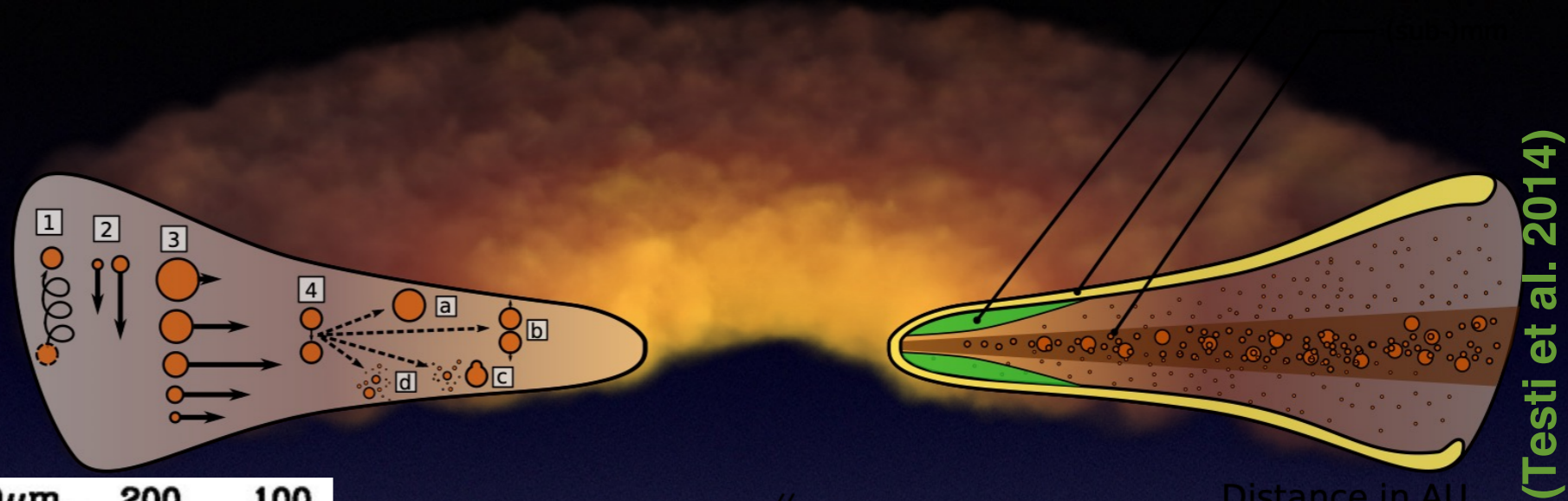
Photon  
FASTCAM S43 mode...  
1024 X 1024  
-00:00:00.491  
1/3000 sec  
Time: 15.17  
Date: 2011/6/9  
End  
Frame: 491



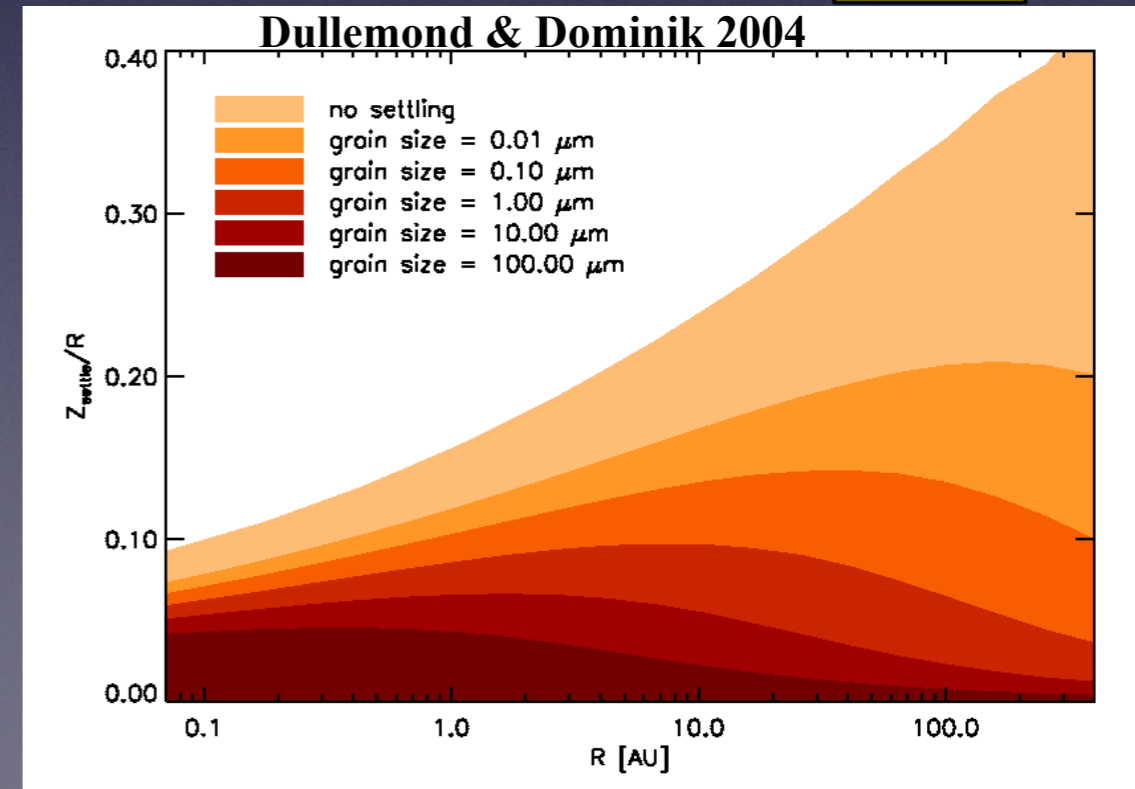
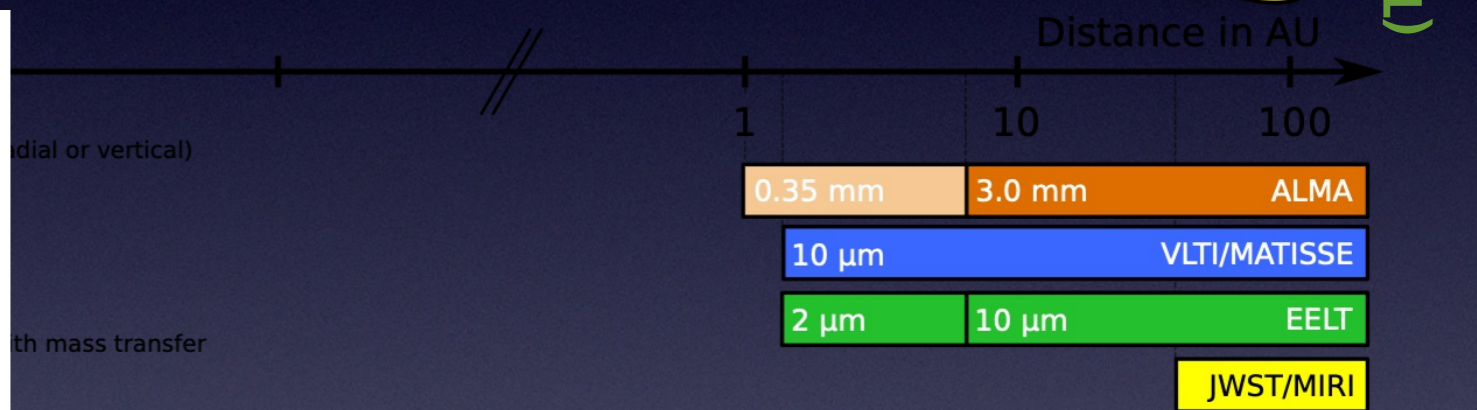
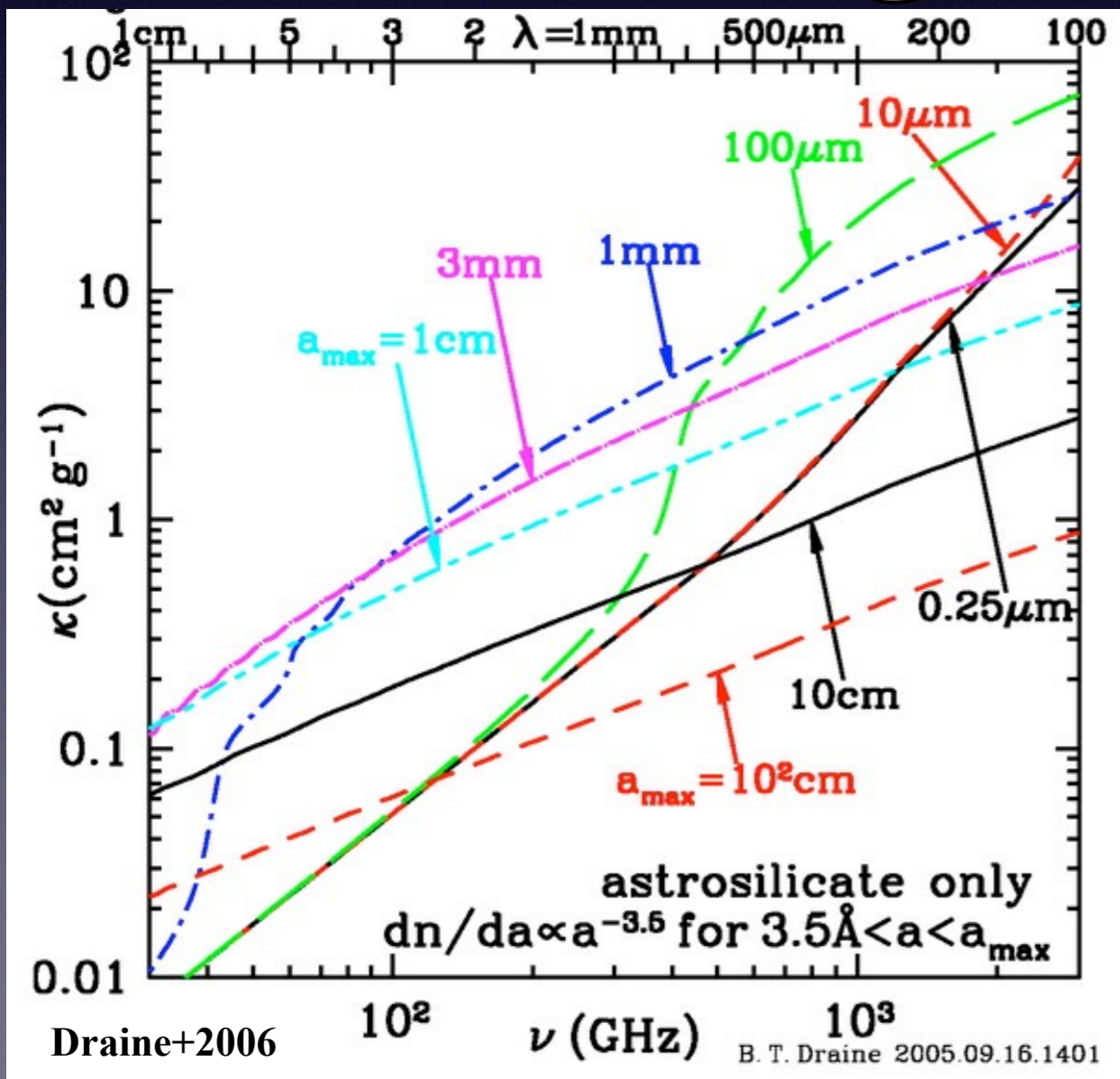
Movies from J. Blum and collaborators:  
Weidling et al. 2012  
Schraepler et a. 2012  
Guettler et al. 2010



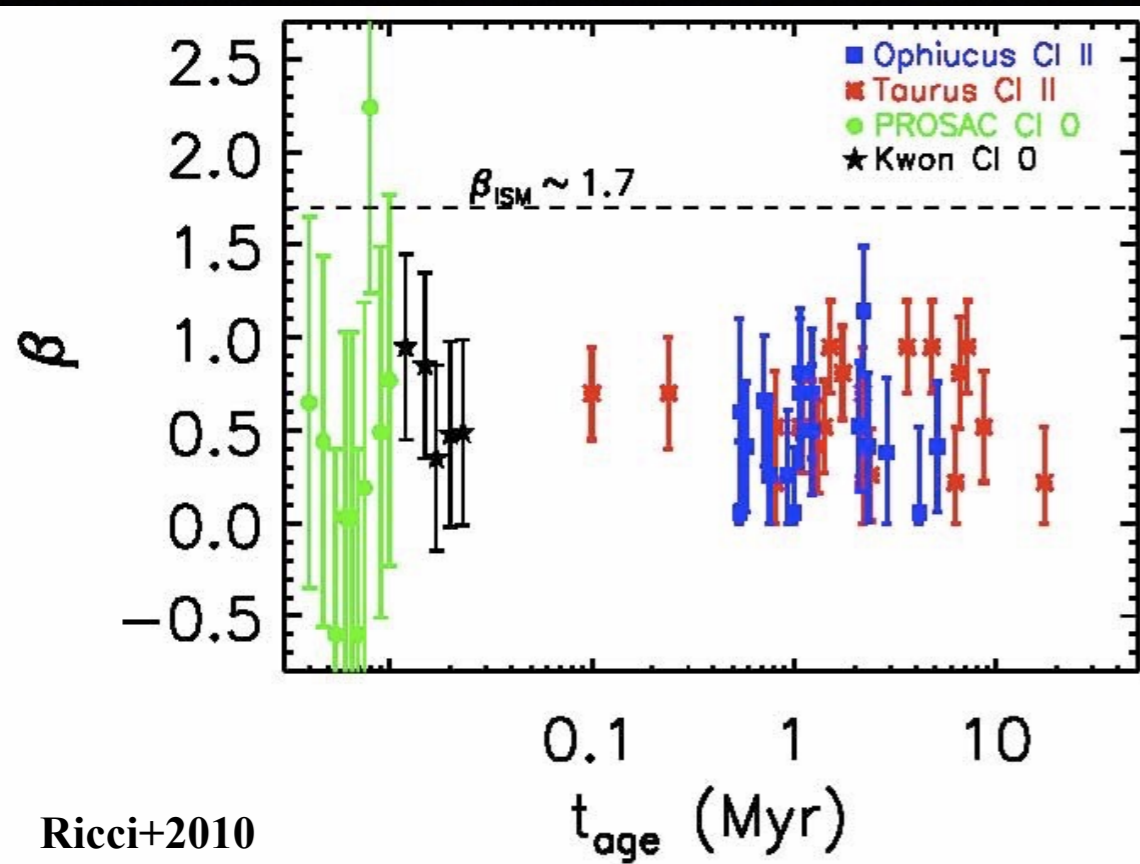
# Dust evolution: grain growth processes



(Testi et al. 2014)

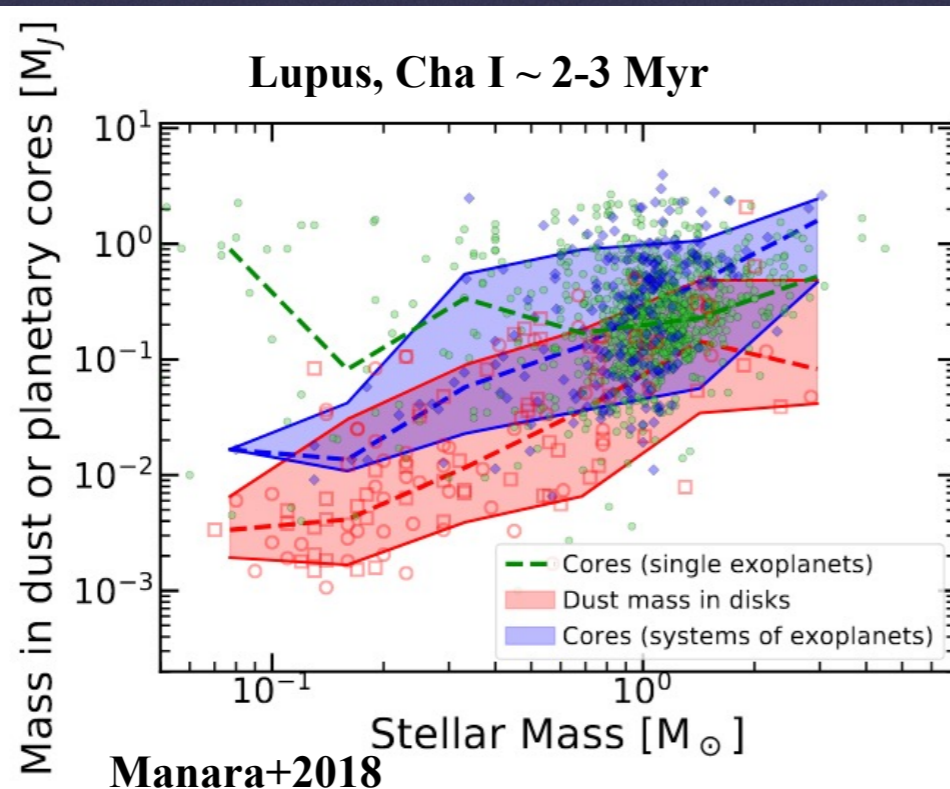


# Annoying alarms

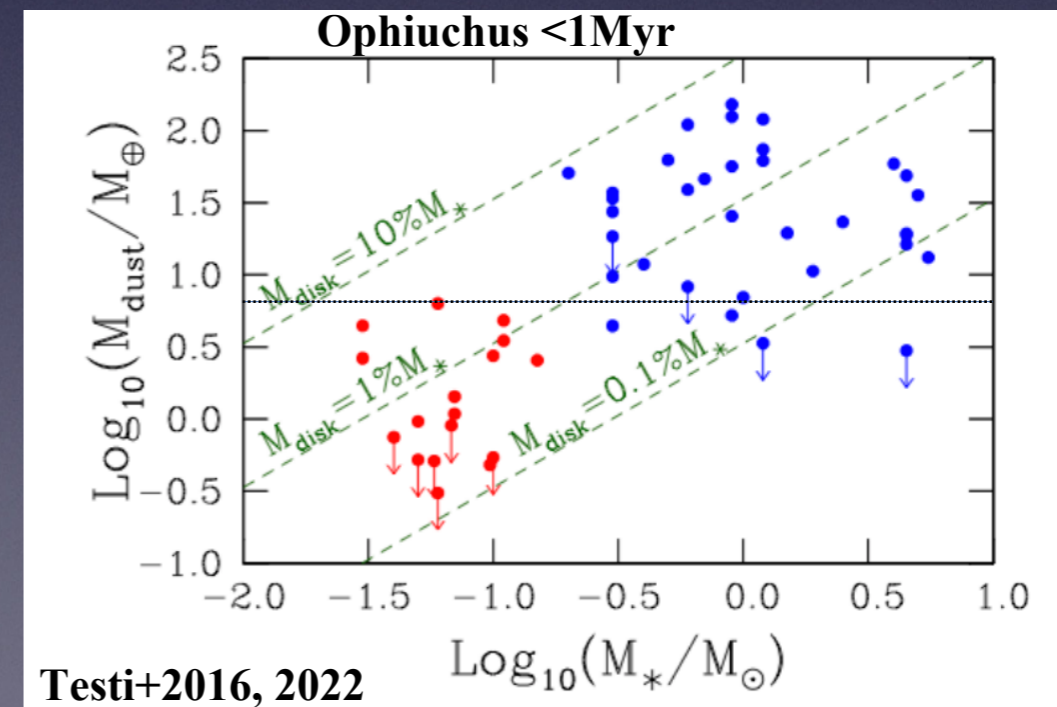


Ricci+2010

- Evidence for dust evolution in young protostars
- No evidence for evolution from small to large dust grains
- Initial surveys revealed a gradual decay (factor  $\sim 4$  in  $\sim 5$  Myr)
- Dust content is relatively low
- Estimates rely on simple assumption on temperature structure and dust opacity
- Already at 1 Myr disks seem to contain too little dust to form planets



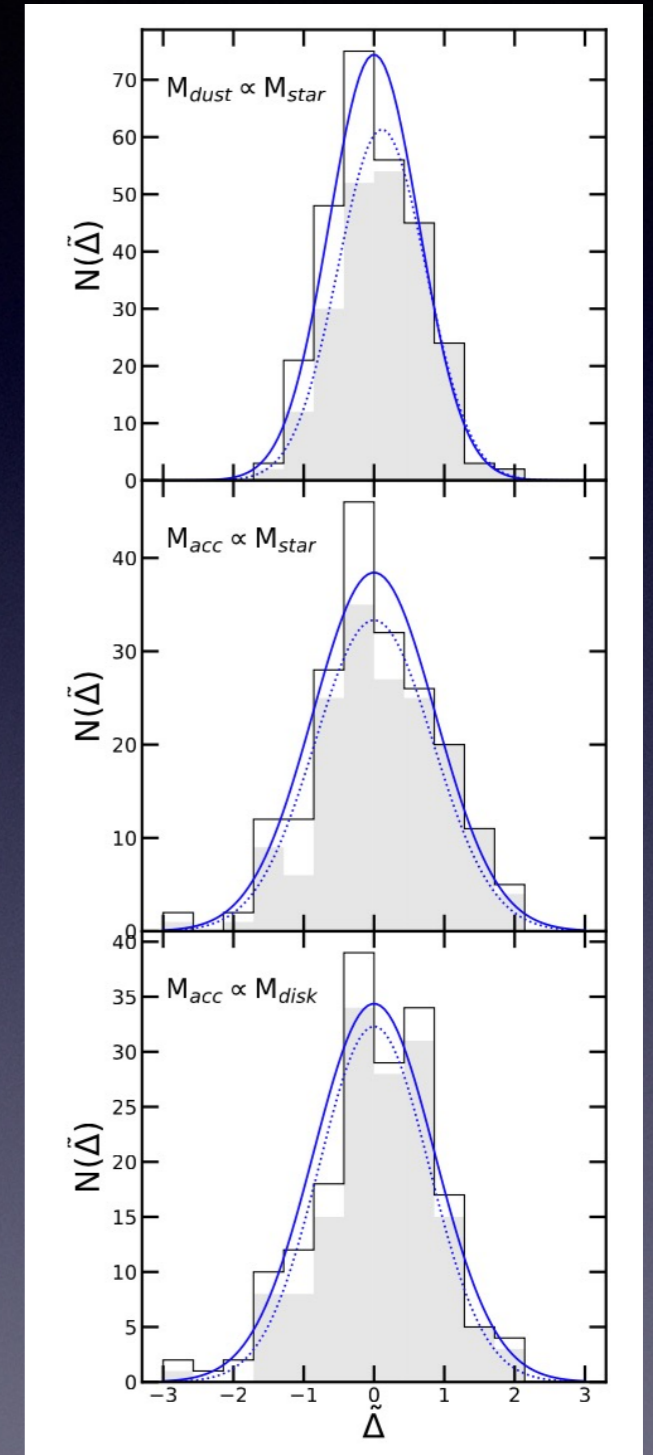
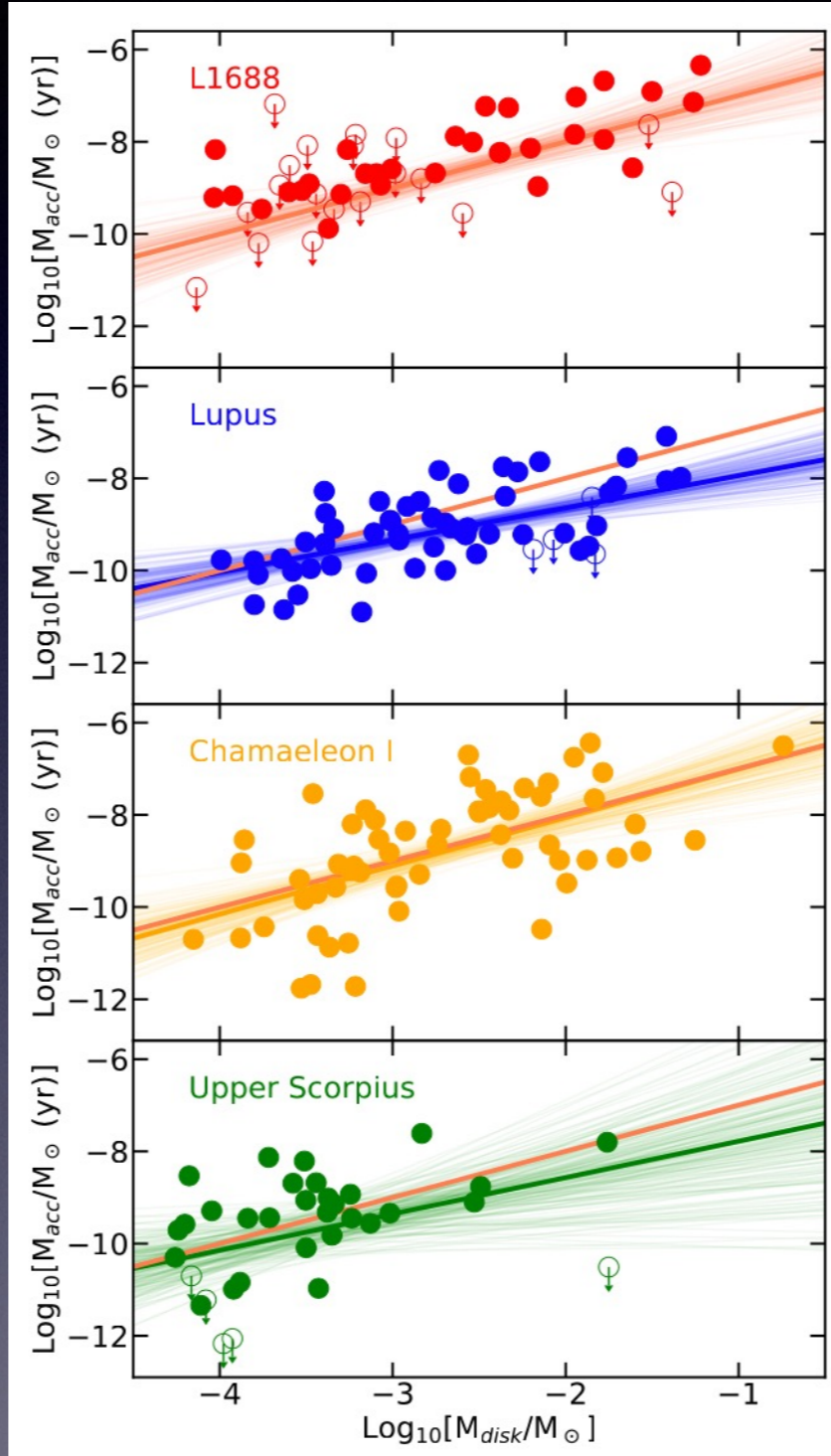
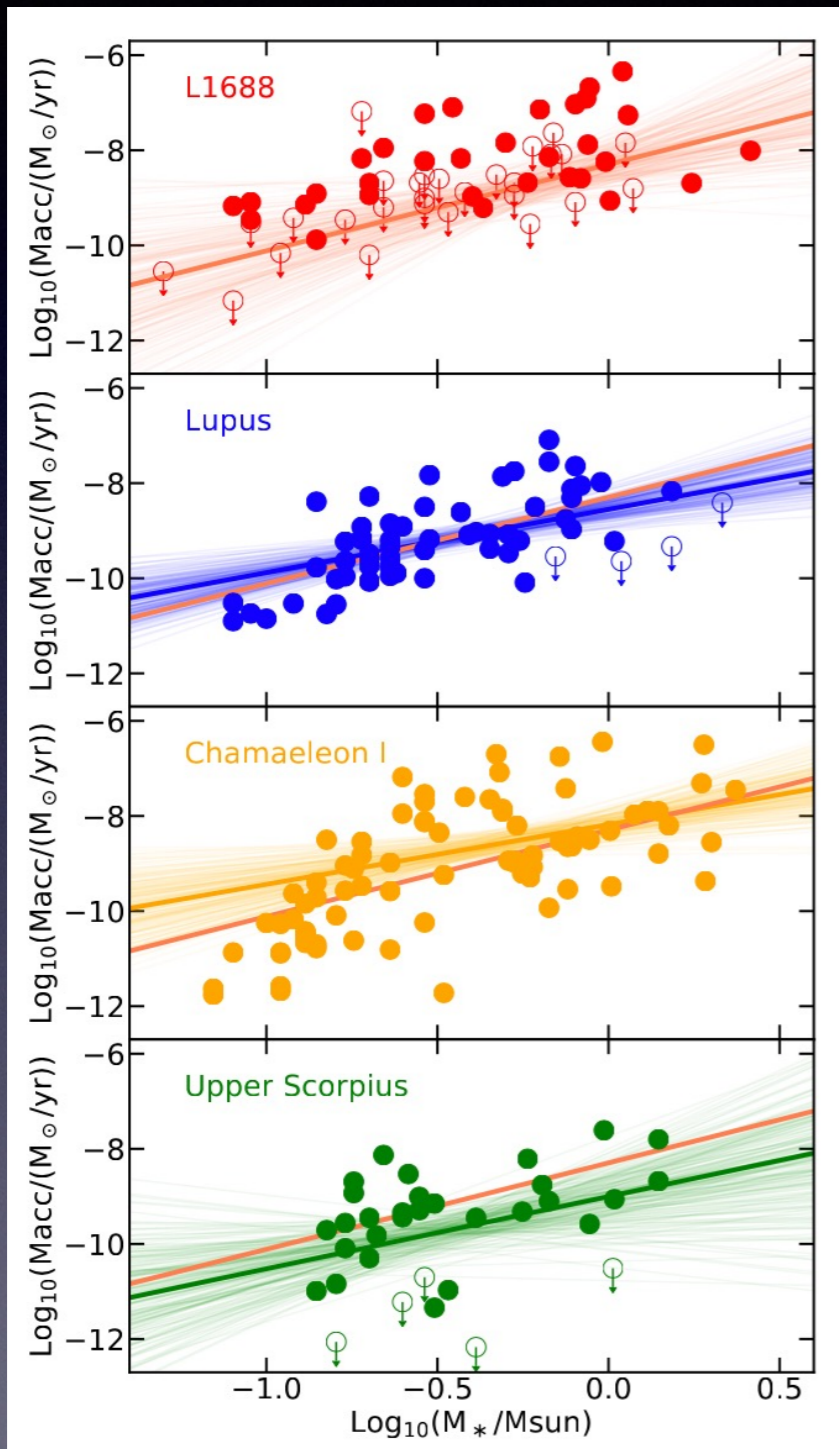
Manara+2018



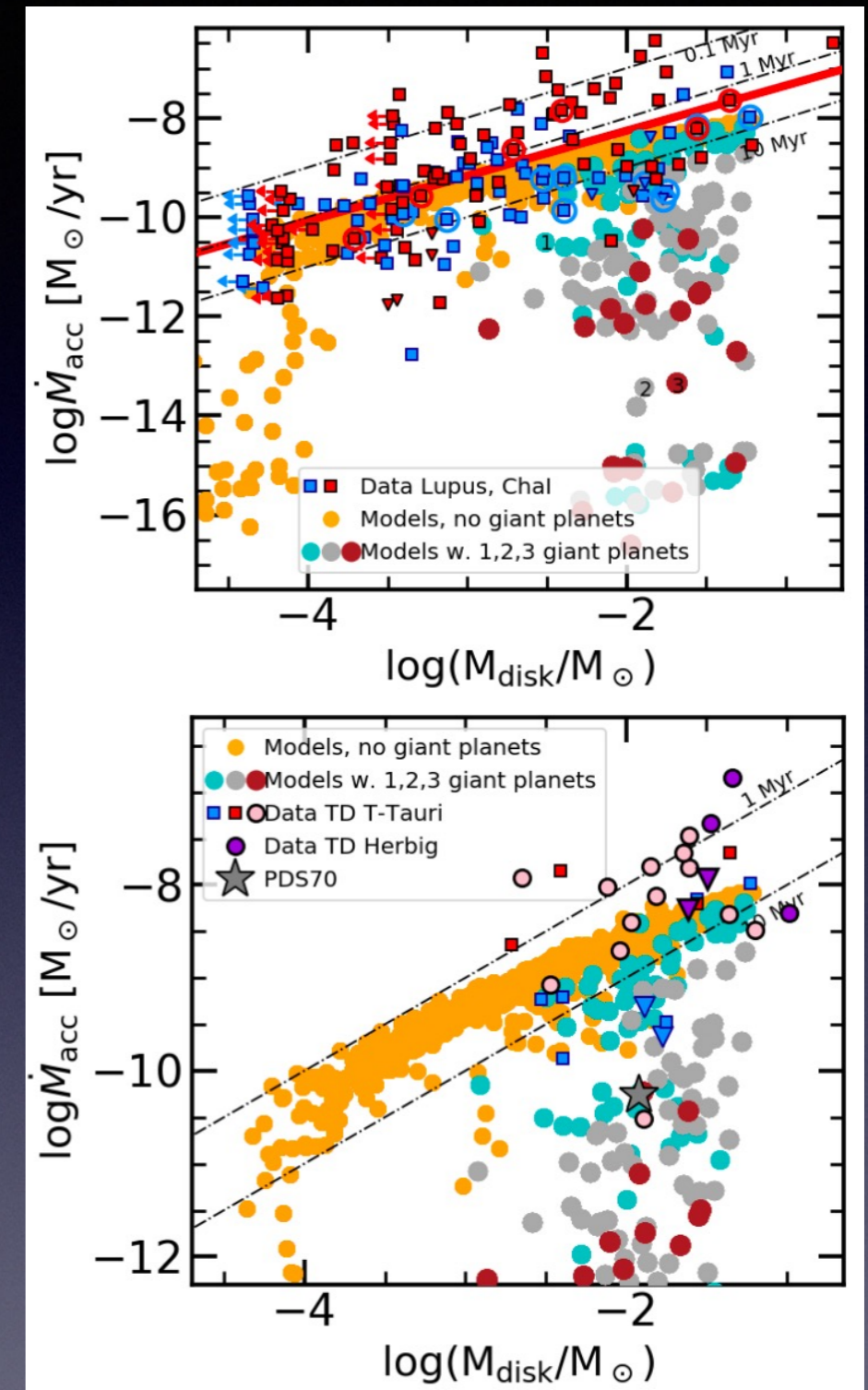
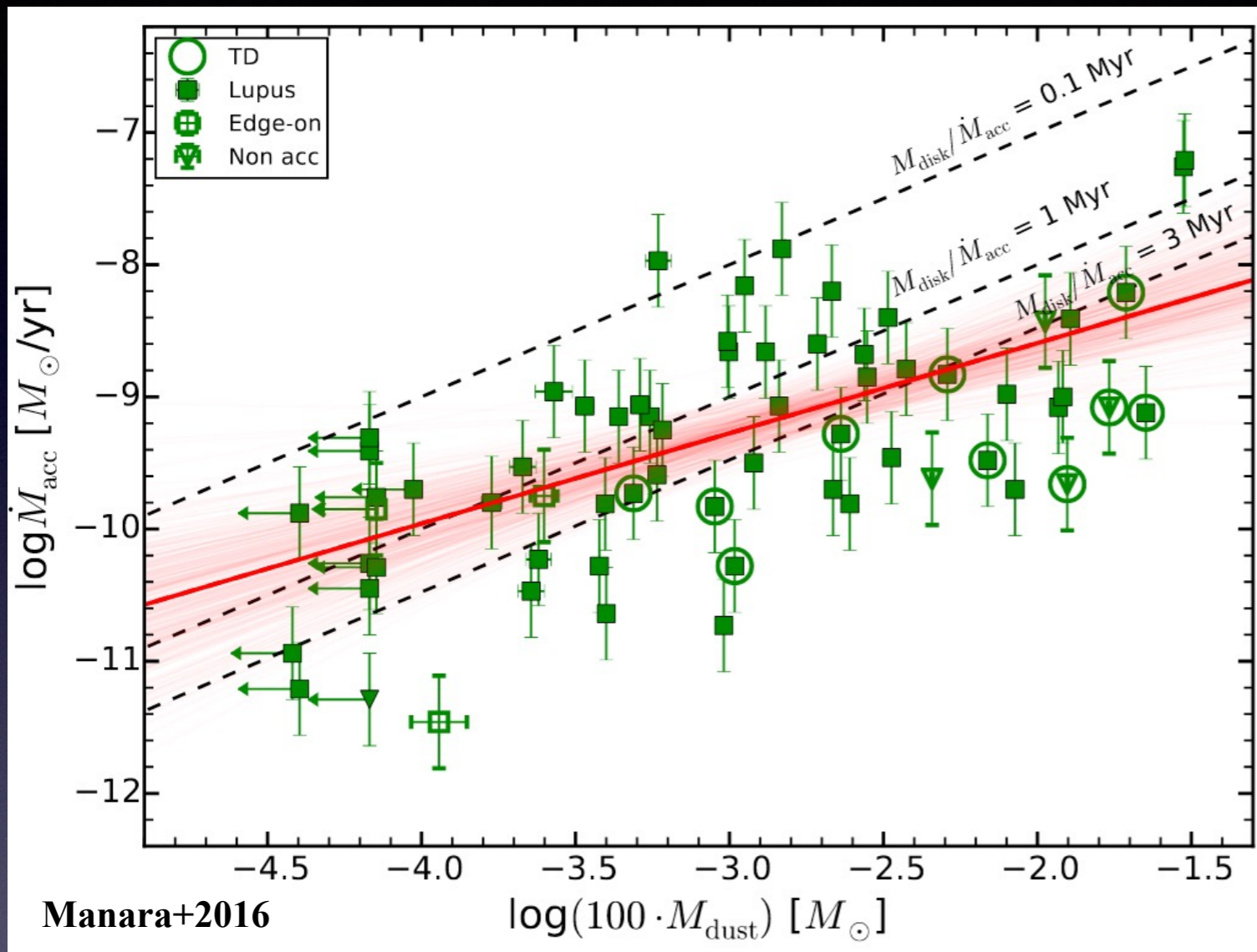
Testi+2016, 2022

# Evolution of disk properties

(Testi et al. 2022; see also Manara+2022)  
Data from ALMA, XShooter, etc.



# Long term disk evolution

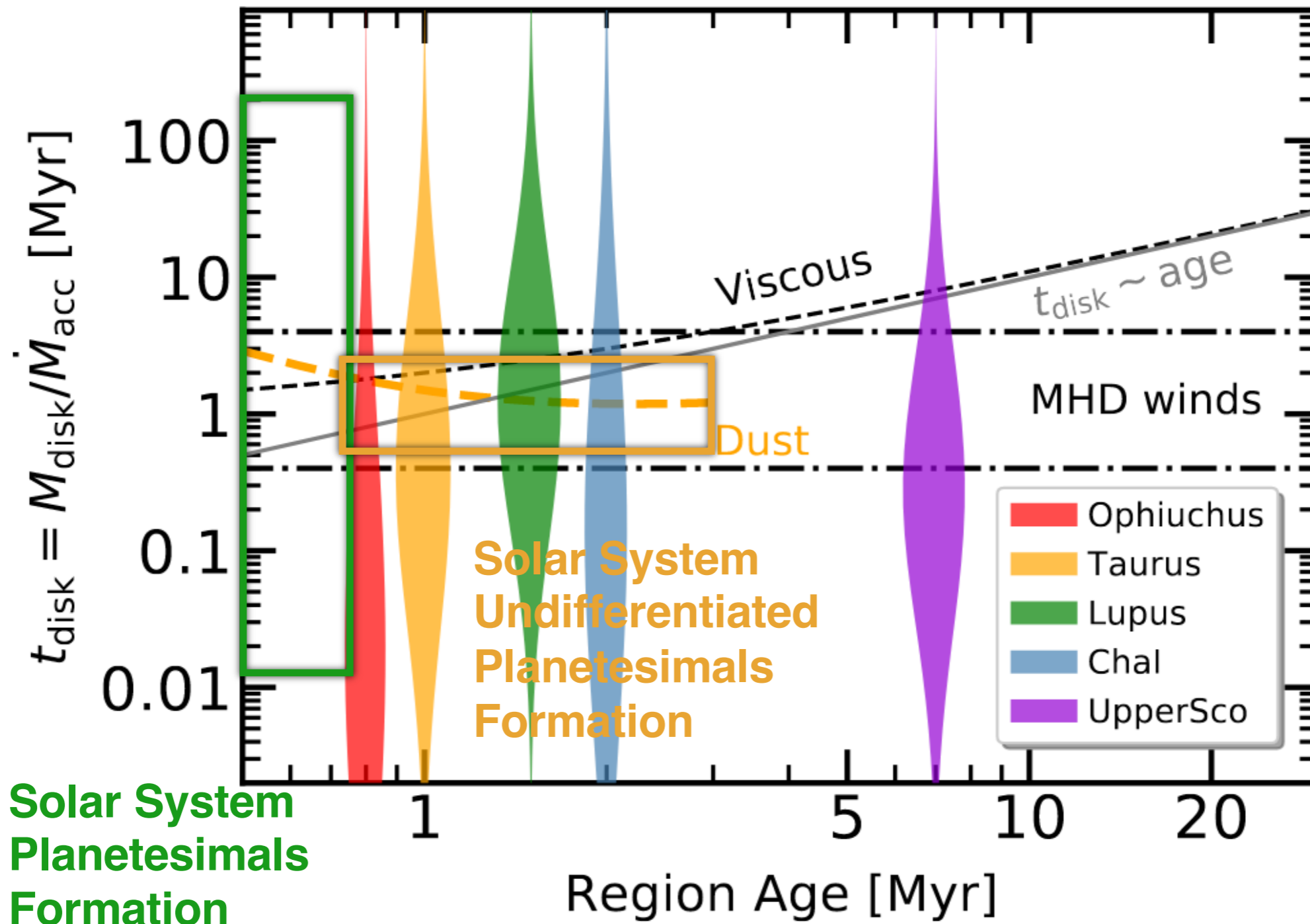


- Almost as predicted by viscous evolution... but not quite!

Manara, Mordasini, Testi, et al. 2019



# Evolution of disk properties

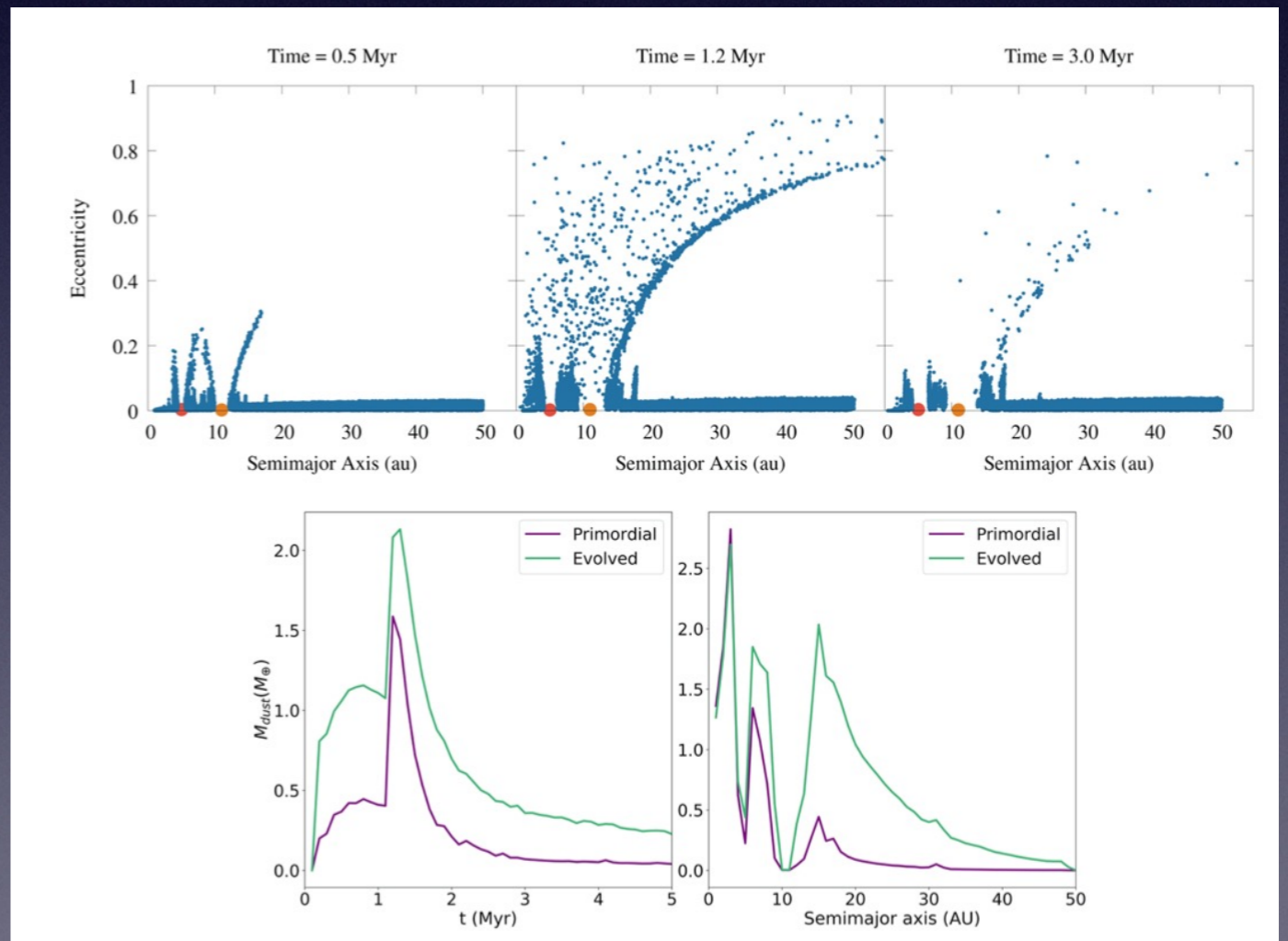
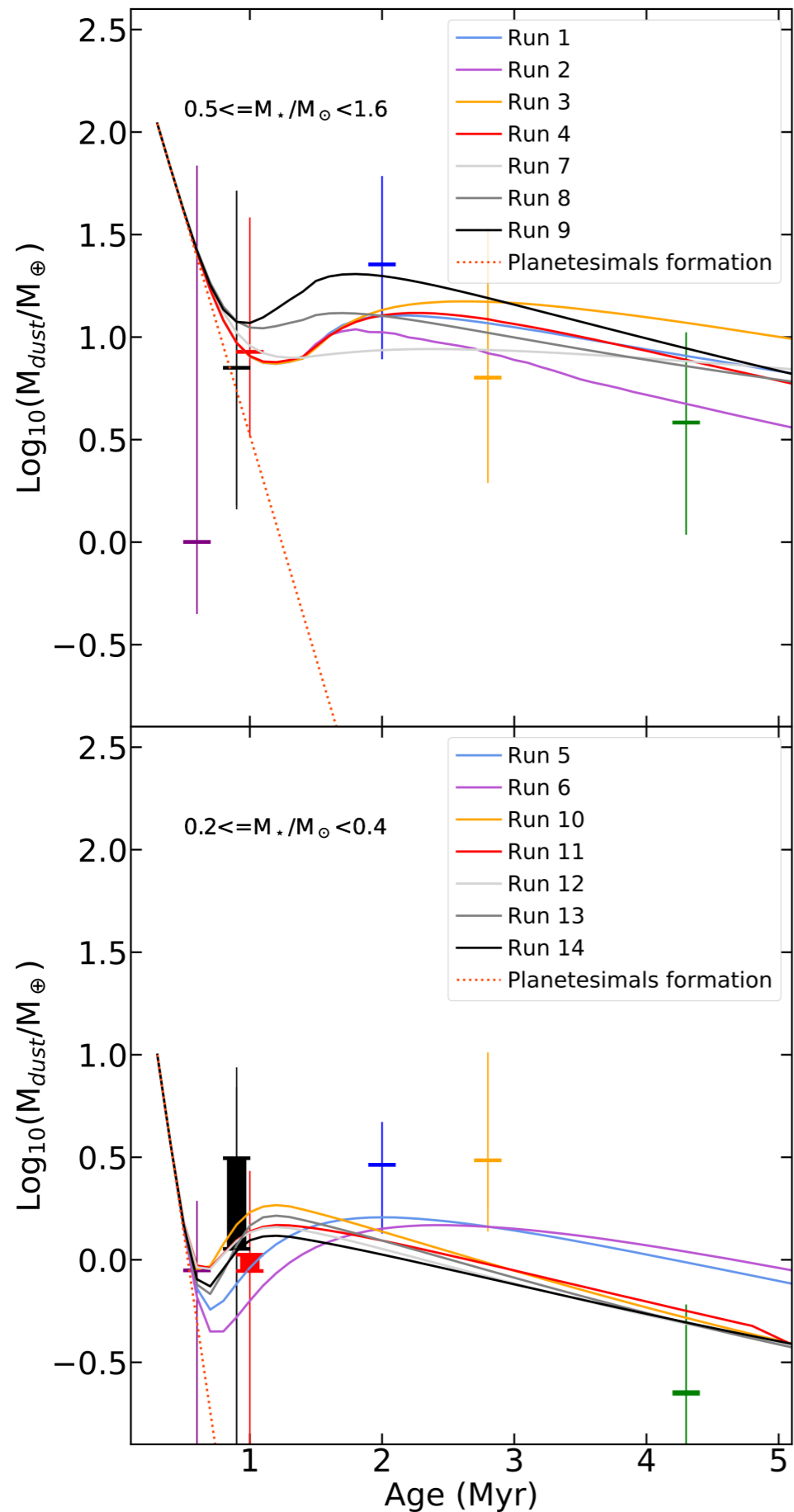


(Manara+2023)

Solar System  
Planetesimals  
Formation

# Planet formation explanations

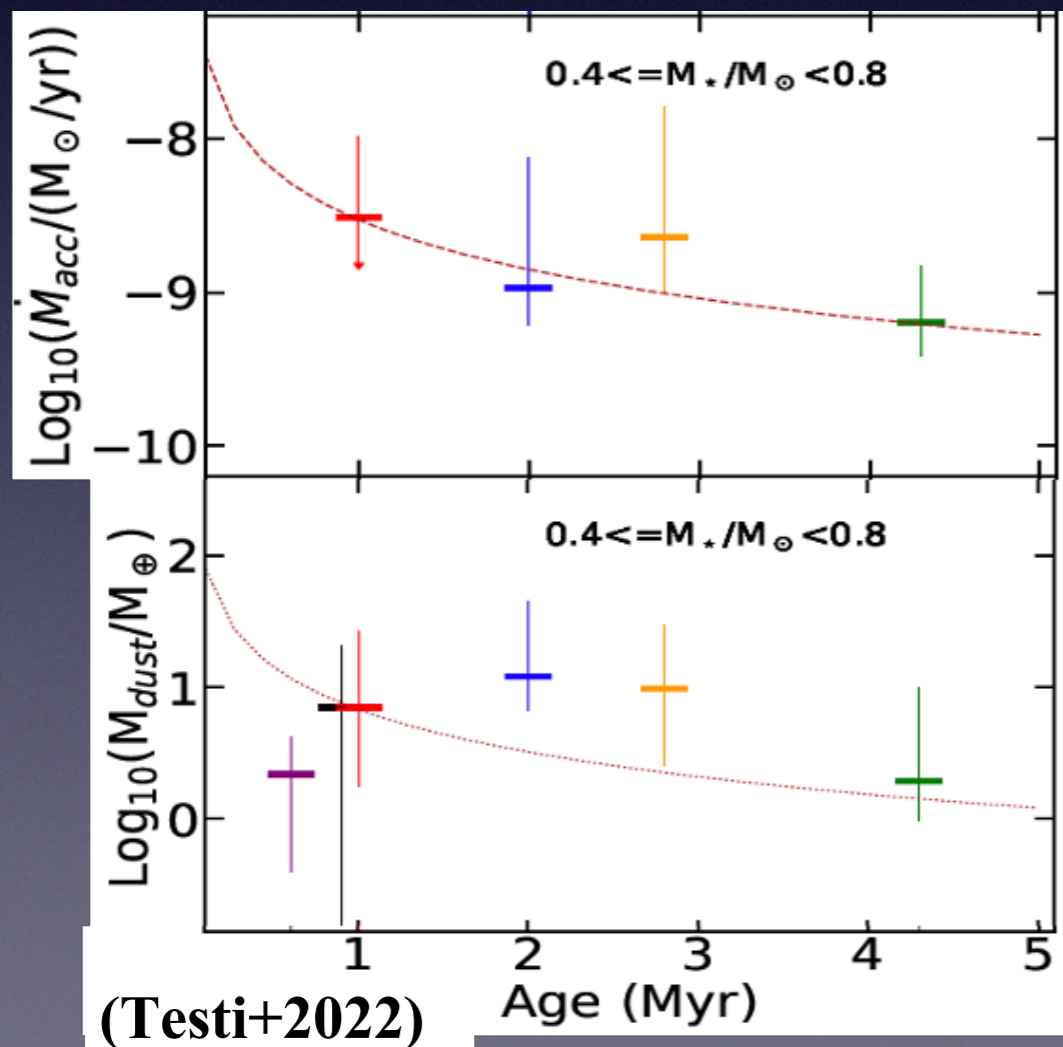
## Planet formation



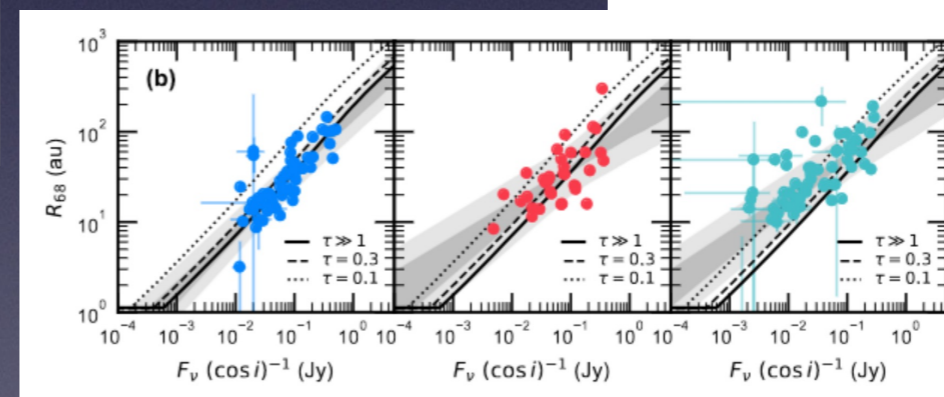
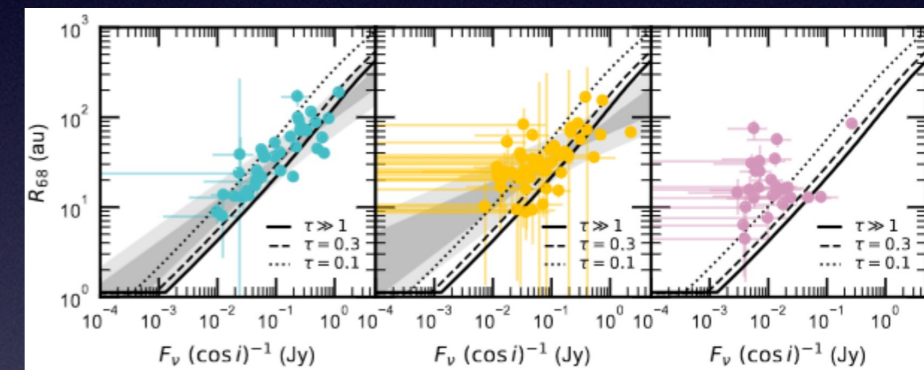
(Turrini+2019, Bernabo+2022)

# Mass deficit explanations

- Early planetesimals and planet formation
- Optical depth effects



0.9mm



(Tazzari+2023)

1.3mm

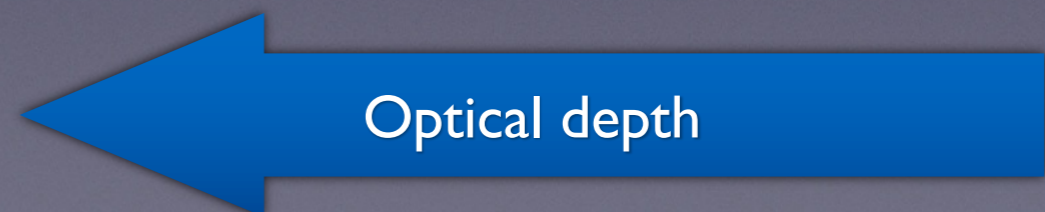
0.5Myr

1Myr

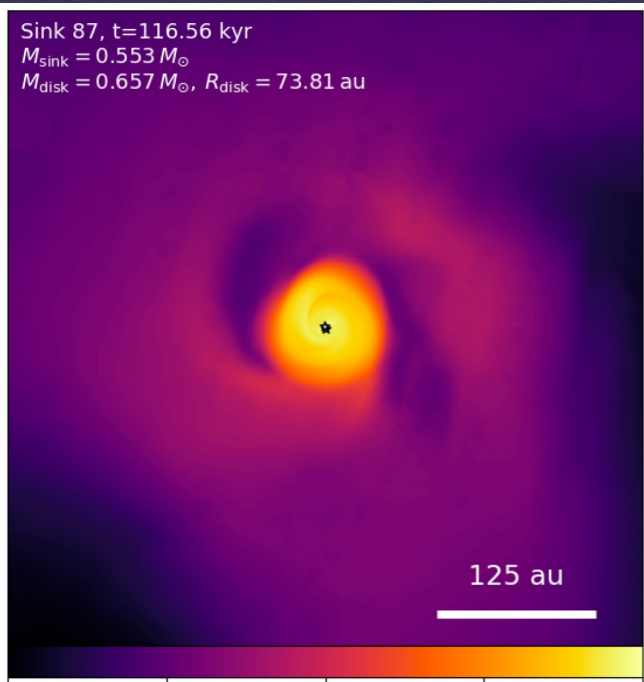
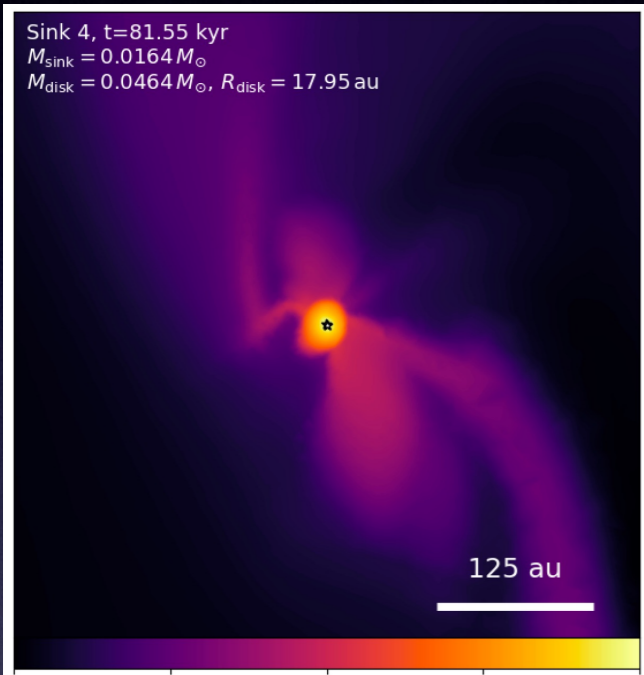
2Myr

3Myr

5-8Myr



# Next generation population synthesis



Initial conditions

→

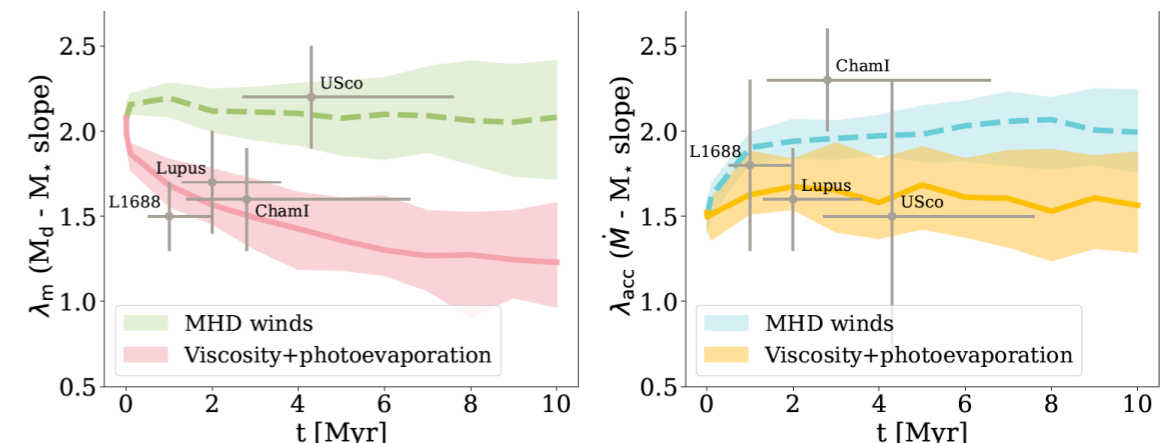
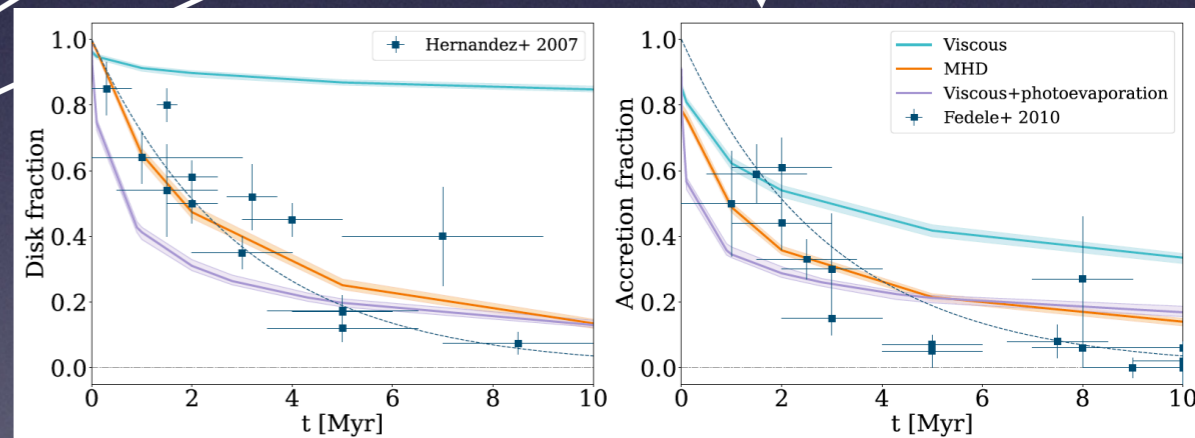
Simplified 1D prescriptions

Population observables



Diskpop  
 Population  
 synthesis of planet  
 forming disks

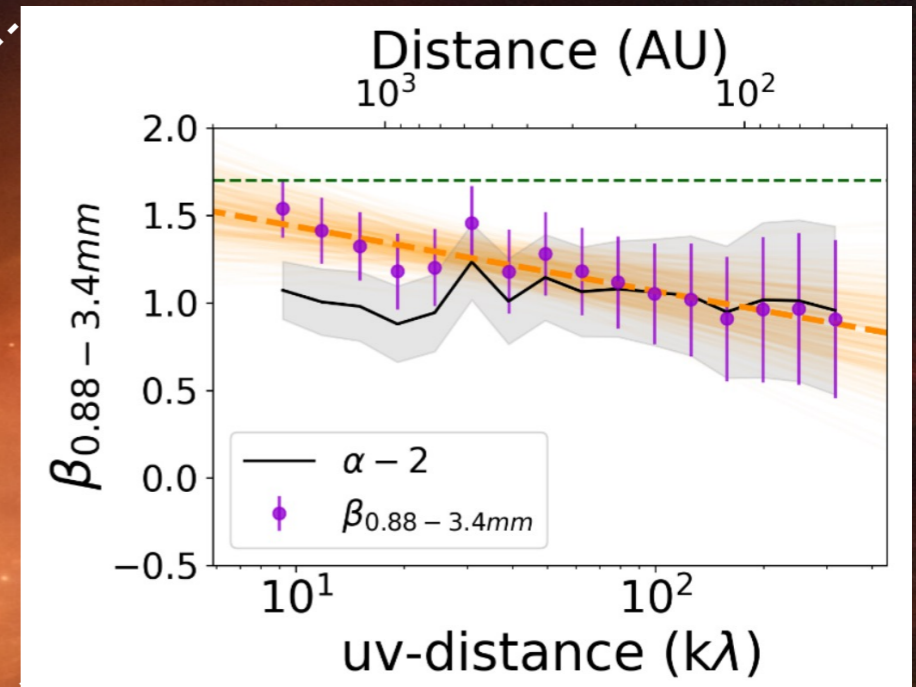
Missing ingredients:  
 Planet formation  
 Chemical evolution



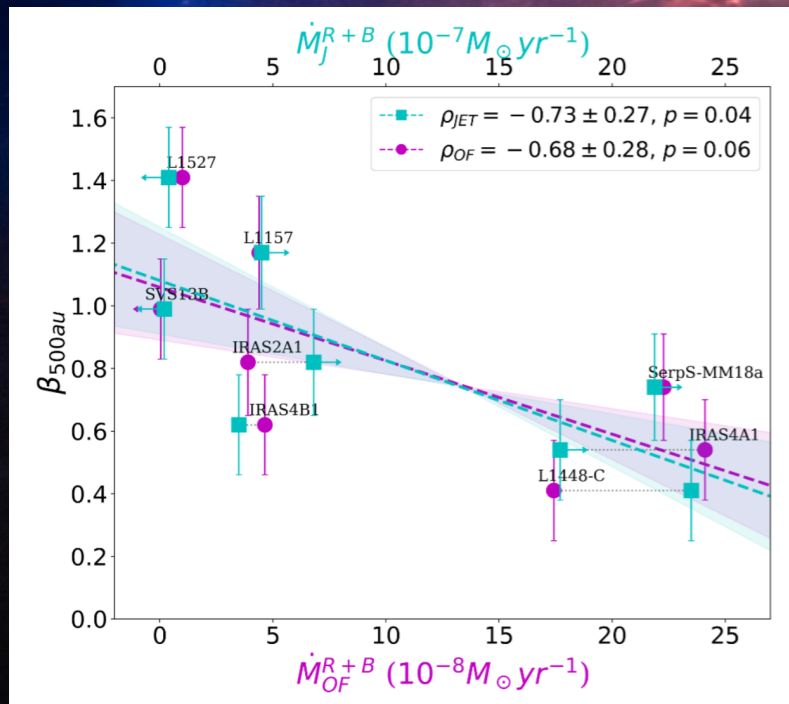
# Are grains growing already in Class 0/I envelopes? Are they transported therein ?



Luca Cacciapuoti



Cacciapuoti, L. et al. 2023a, A&A

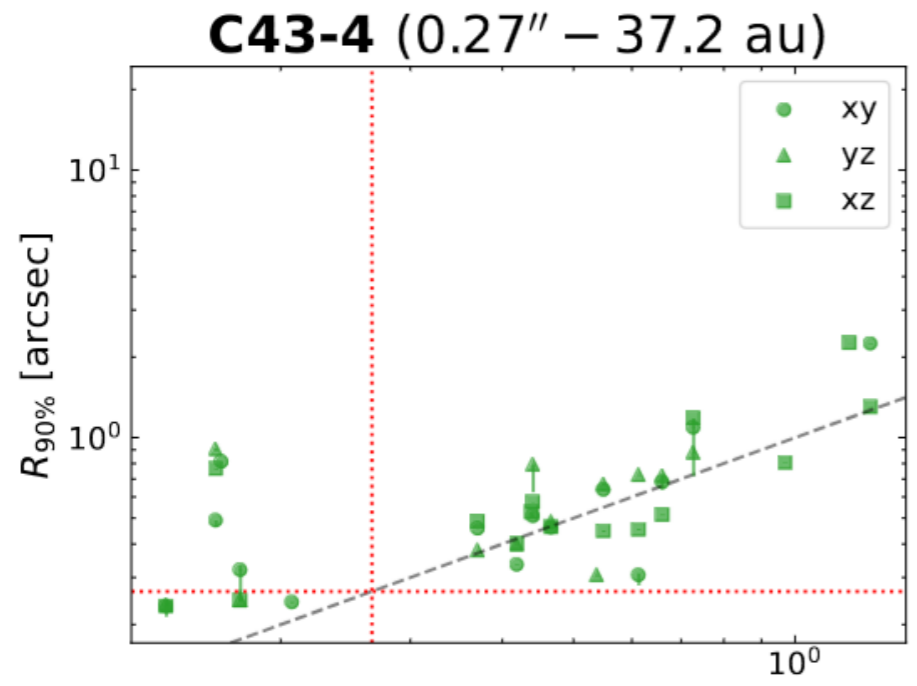


Cacciapuoti, L. et al. subm.

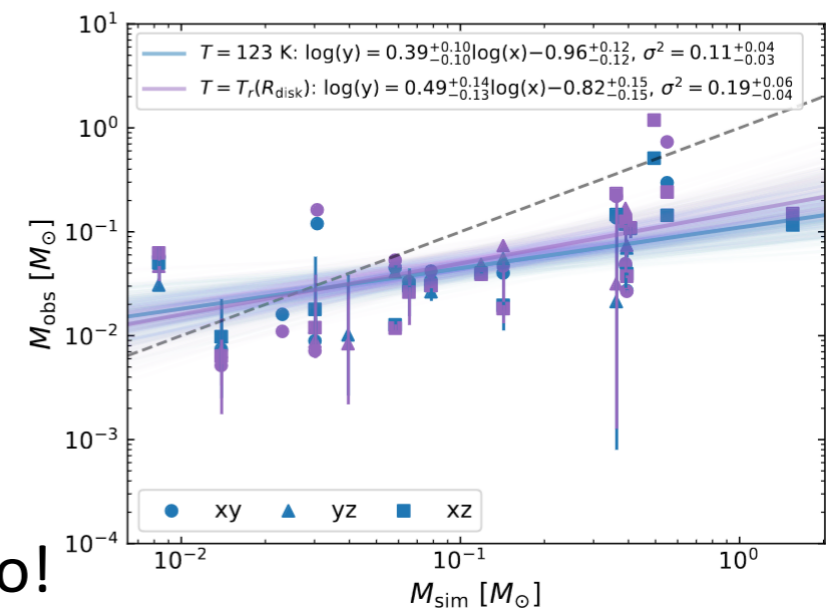
ALMA Band 4 archival data overlaid on  
 JWST NIRC2 view of L1527 IRS, Taurus  
 Credits: NASA, CSA, ESA, STScI

- Key conclusions: comparison not trivial, quick and dirty approach not meaningful to extract the physics
- Importance of going to longer wavelengths

(Ngo et al. 2024)



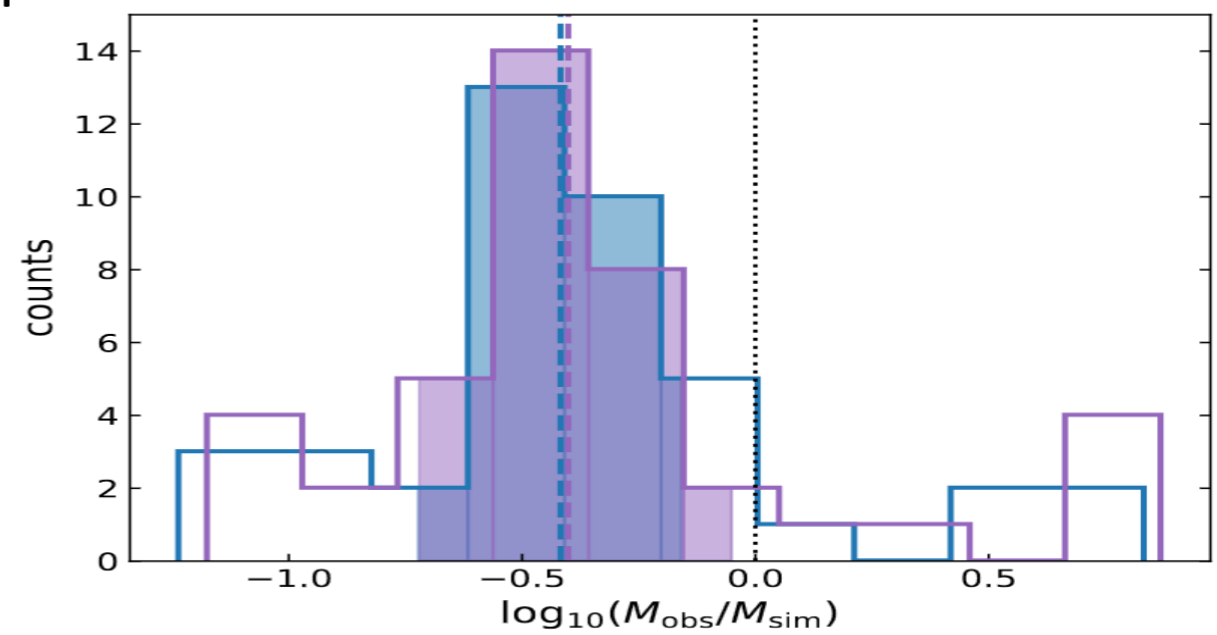
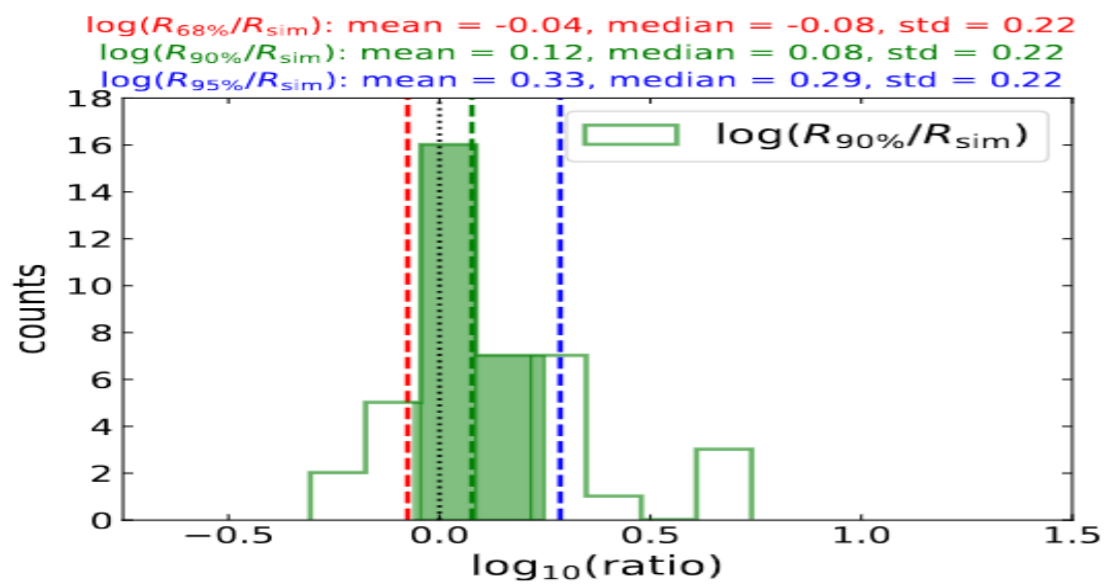
Disk radii - Ok



Disk mass – No!

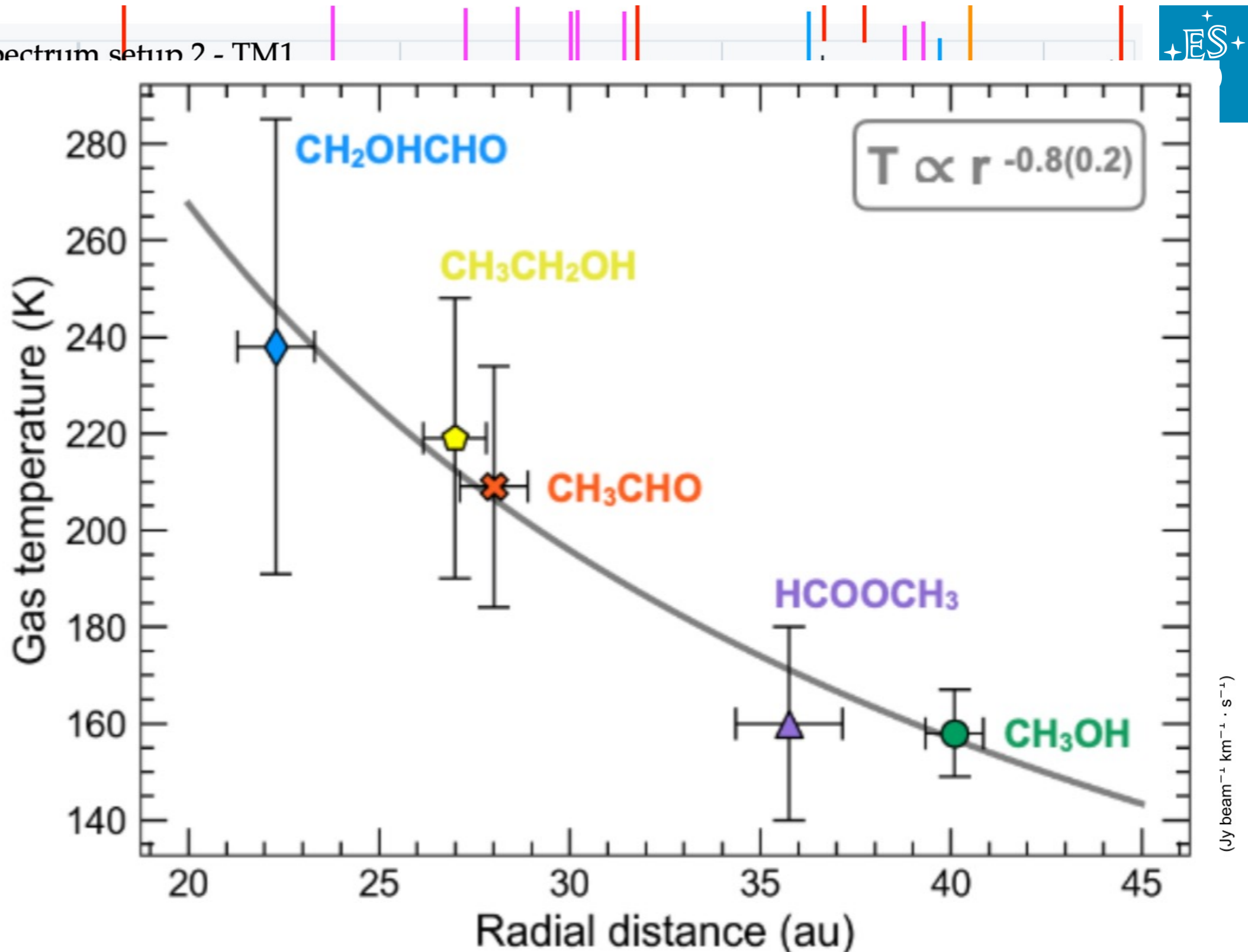
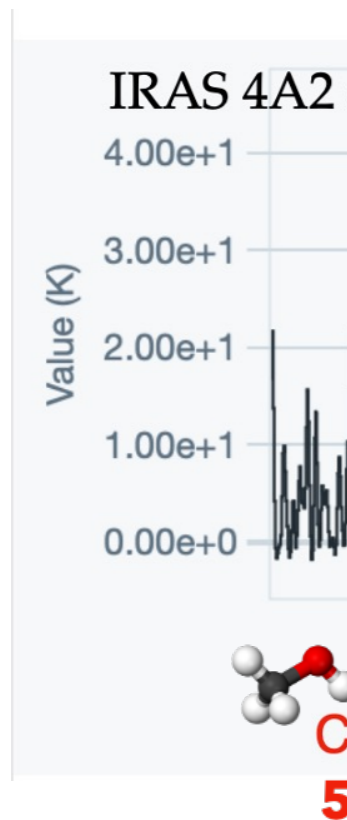
Optical depth!

▭  $\log(M_{\text{obs}}/M_{\text{sim}})$ ,  $T = 123 \text{ K}$ :  
 mean = -0.38, median = -0.42, std = 0.45  
▭  $\log(M_{\text{obs}}/M_{\text{sim}})$ ,  $T = T_r(R_{\text{disk}})$ :  
 mean = -0.35, median = -0.40, std = 0.48



# iCOMs: interstellar Complex Organic Molecules

## Molecular lines identification in IRAS 4A2 spectrum



### Estimated

- Methanol
- Acetaldehyde
- Methyl formate
- Formamide
- Glycolaldehyde