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The First Stars: Formation, Properties, and Impact

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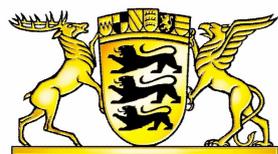


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The First Stars: Formation, Properties, and Impact

some theory
Pop III stars
Pop II stars
supermassive stars
constraints

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Annual Review of Astronomy and Astrophysics
**The First Stars: Formation,
Properties, and Impact**

Ralf S. Klessen^{1,2} and Simon C.O. Glover¹

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Keywords

cosmology, first and second stellar population, galactic archeology, high-redshift Universe, Population III and II, star formation

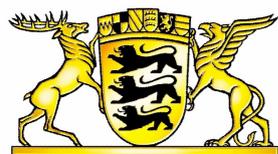
Abstract

The first generation of stars, often called Population III (or Pop III), form from metal-free primordial gas at redshifts $z \sim 30$ and below. They dominate the cosmic star-formation history until $z \sim 15$ – 20 , at which point the formation of metal-enriched Population II stars takes over. We review current theoretical models for the formation, properties, and impact of Pop III stars and discuss existing and future observational constraints. Key takeaways from this review include the following:

- Primordial gas is highly susceptible to fragmentation and Pop III stars form as members of small clusters with a logarithmically flat mass function.
- Feedback from massive Pop III stars plays a central role in regulating subsequent star formation, but major uncertainties remain regarding its immediate impact.



some theory



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cosmic timeline



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cover onset of primordial star formation to early reionization

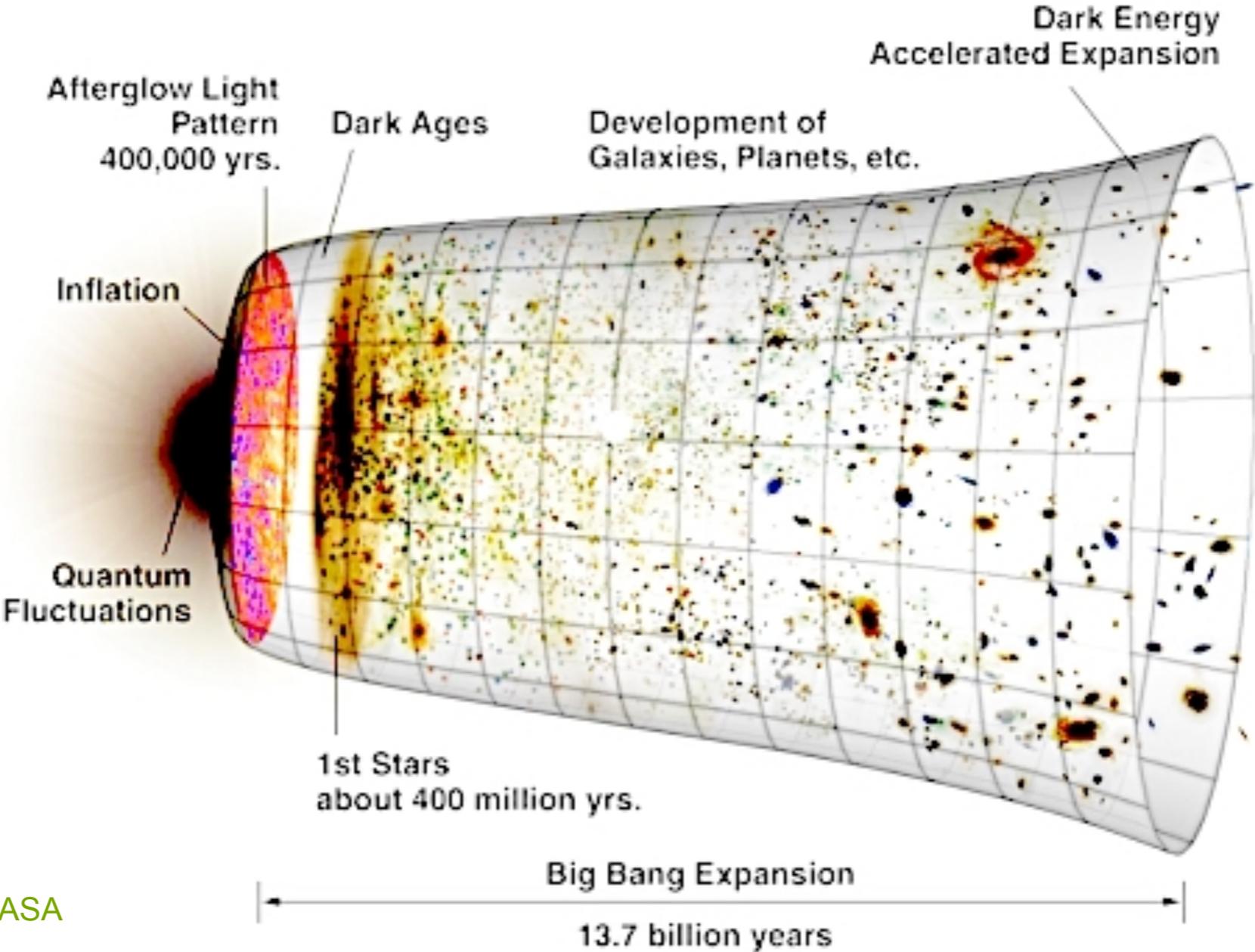


image credit: NASA

some motivation

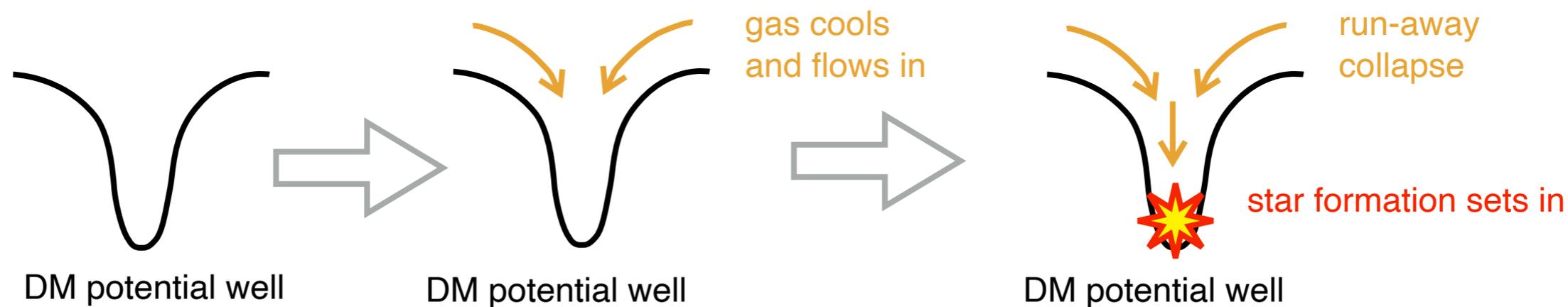
criteria for onset of star formation



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criteria for primordial star formation

- DM halos need to decouple from cosmic expansion and start to contract
- gas needs to decouple and go into run-away collapse
 - > **Jeans criterion:** $\tau_{\text{grav}} < \tau_{\text{sound}}$
- in addition, gas needs to cool away compression heat
 - > **Rees-Ostriker criterion:** $\tau_{\text{cool}} < \tau_{\text{dyn}}$
- both depend on thermodynamic response of the gas
 - > competition between heating and cooling processes
 - > importance of chemistry
- collapse needs to proceed to stellar densities



critical halo mass for star formation 1



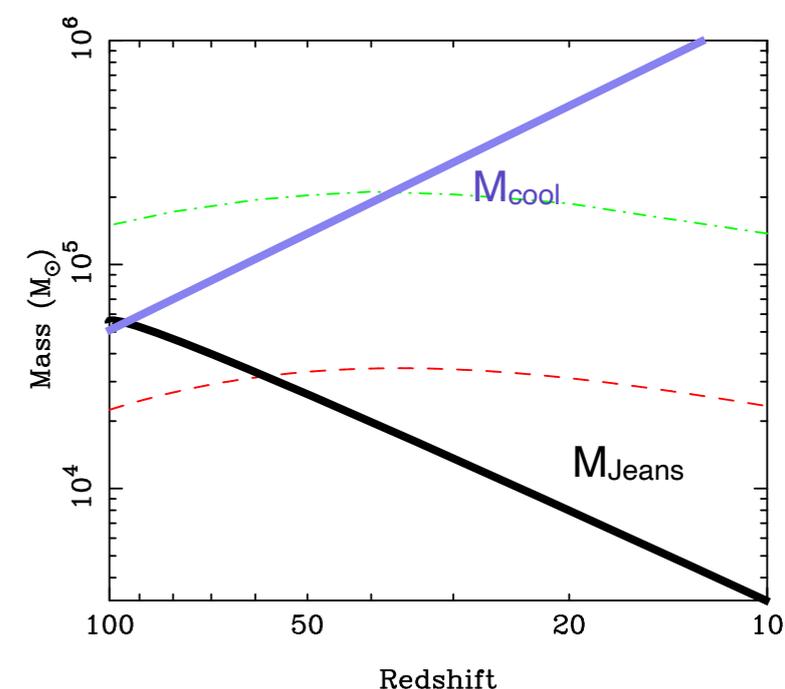
criteria for collapse and star formation

- look at competition between gravity (density ρ) and gas pressure (sound speed c_s or temperature T): **Jeans mass**
- critical mass:

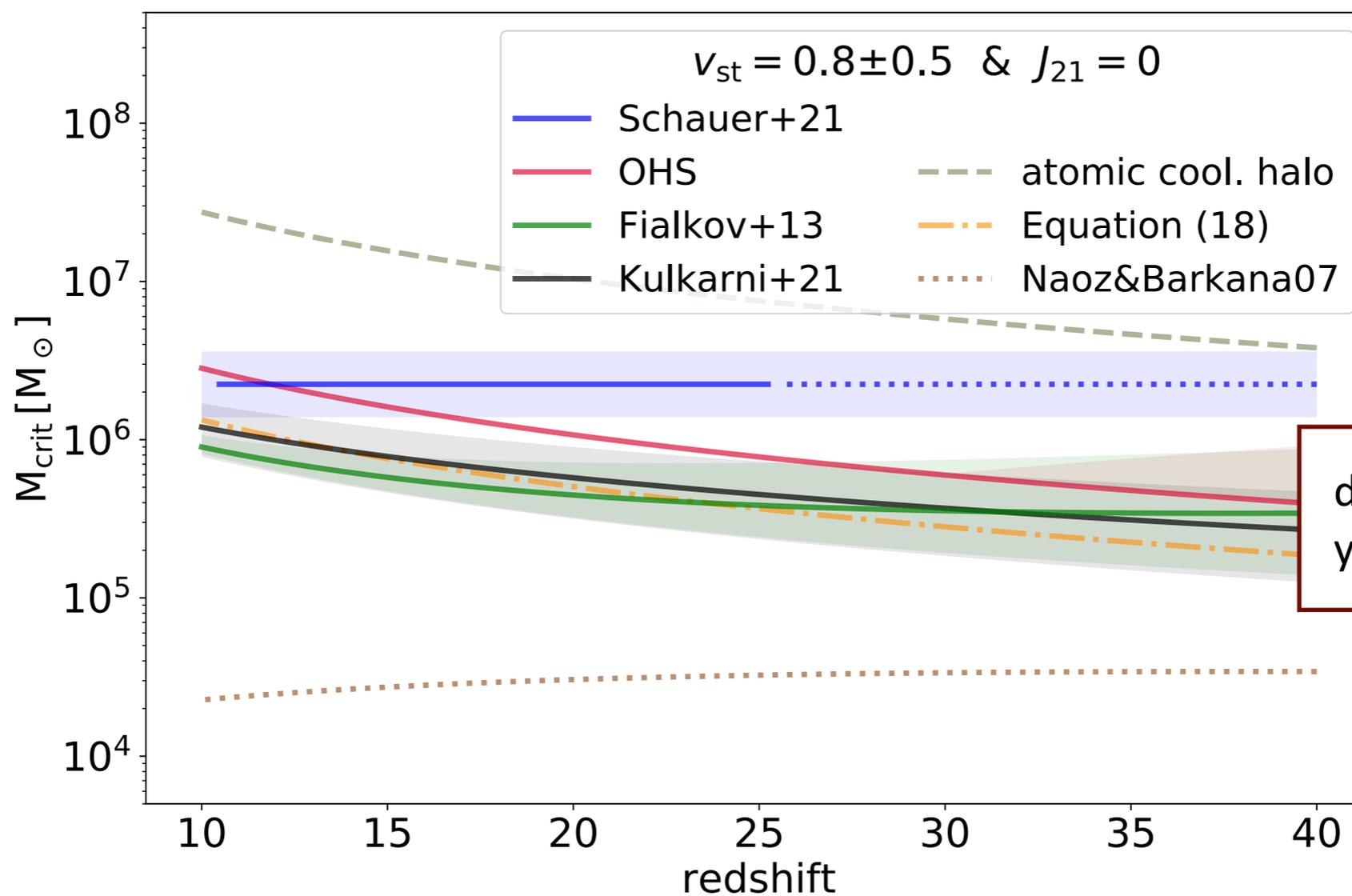
$$M_J = \frac{\pi^{5/2}}{6} \left(\frac{1}{G} \right)^{3/2} \rho^{-1/2} c_s^3 = \frac{\pi^{5/2}}{6} \left(\frac{k}{G} \right)^{3/2} \left(\frac{1}{\mu m_H} \right)^2 n^{-1/2} T^{3/2}$$

- can be extended by considering effective sound speed $c_{s,\text{eff}}^2 = c_s^2 + \sigma^2$ with $\sigma = \sigma_{\text{turb}}$ or $\sigma = v_{\text{Alfven}}$
- in standard LCDM a low redshift this translates to

$$M_J \approx 5 \times 10^3 M_\odot \left(\frac{\Omega_m h^2}{0.14} \right)^{-1/2} \left(\frac{\Omega_b h^2}{0.022} \right)^{-3/5} \left(\frac{z+1}{10} \right)^{3/2}$$

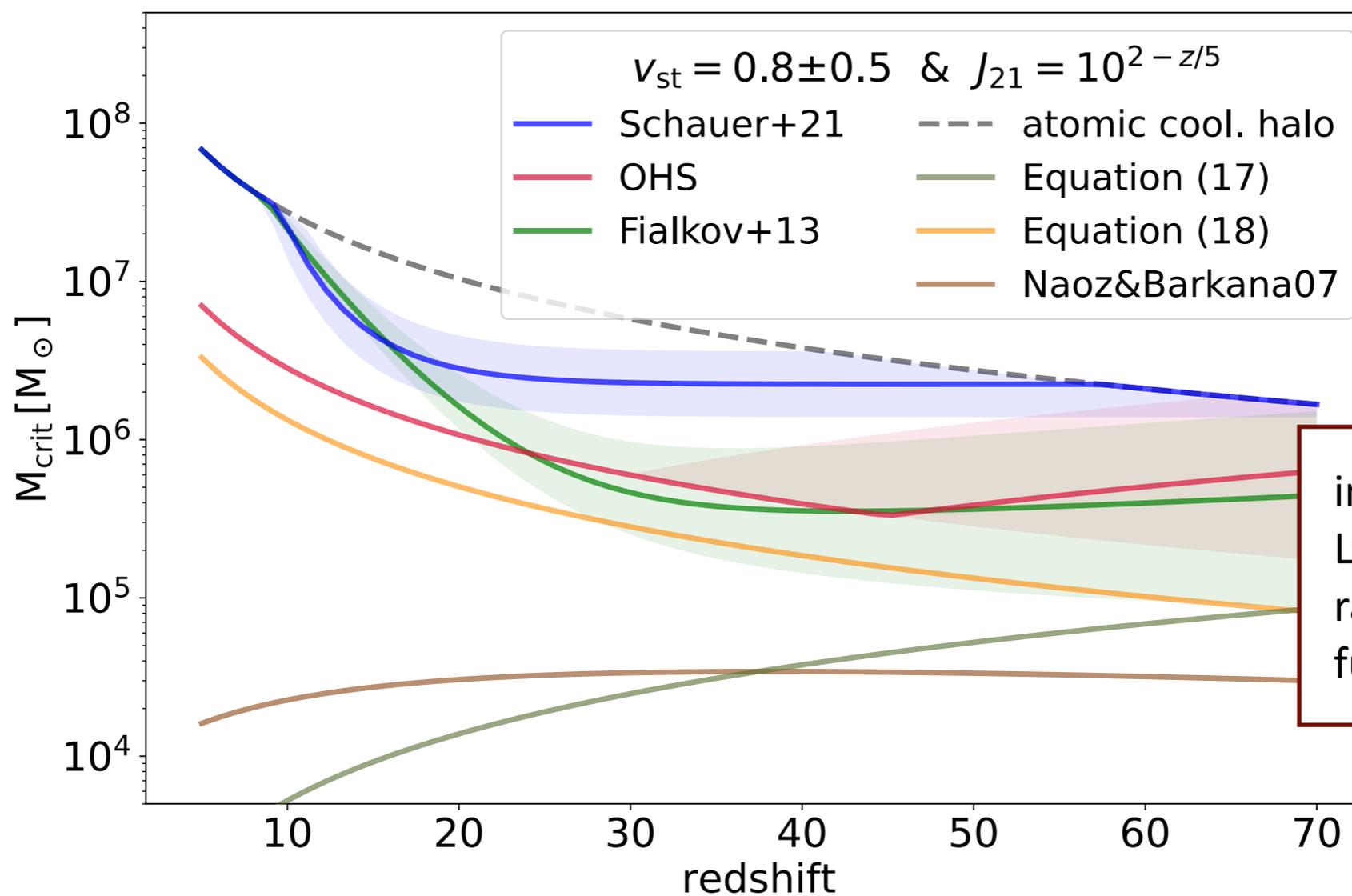


critical halo mass for star formation 1



different models
yield different M_{crit}

critical halo mass for star formation 1



including cosmic Lyman-Werner radiation adds further complexity

critical halo mass for star formation 2



criteria for collapse and star formation

- this is not sufficient, gas also needs to cool away excess heat: **cooling mass**
- efficient cooling requires molecular hydrogen; with H₂ we reach T ~ 500 K and with HD down to T ~ 100 K (but typically not important)

- H₂ typically needs free electrons as catalyst:



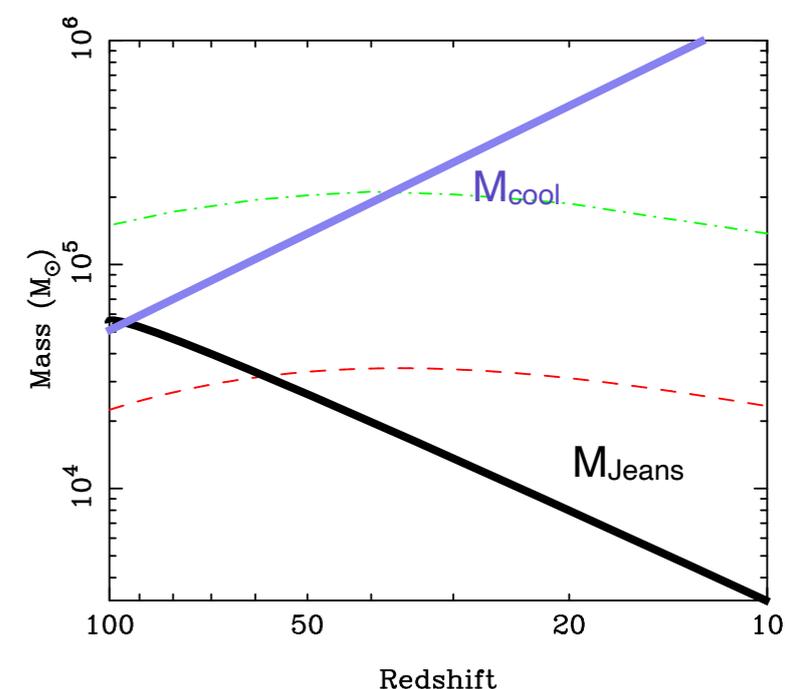
- less important: $\text{H} + \text{H}^+ \rightarrow \text{H}_2^+ + \gamma$ and $\text{H}_2^+ + \text{H} \rightarrow \text{H}_2 + \text{H}^+$

- and at high densities ($n \lesssim 10^9 \text{cm}^{-3}$) via the 3-body path:



- as result:

$$M_{\text{cool}} \approx 6 \times 10^5 M_{\odot} h^{-1} \Omega_{\text{m}}^{-1/2} \left(\frac{\mu}{1.22} \right)^{-3/2} \left(\frac{z+1}{10} \right)^{-3/2}$$

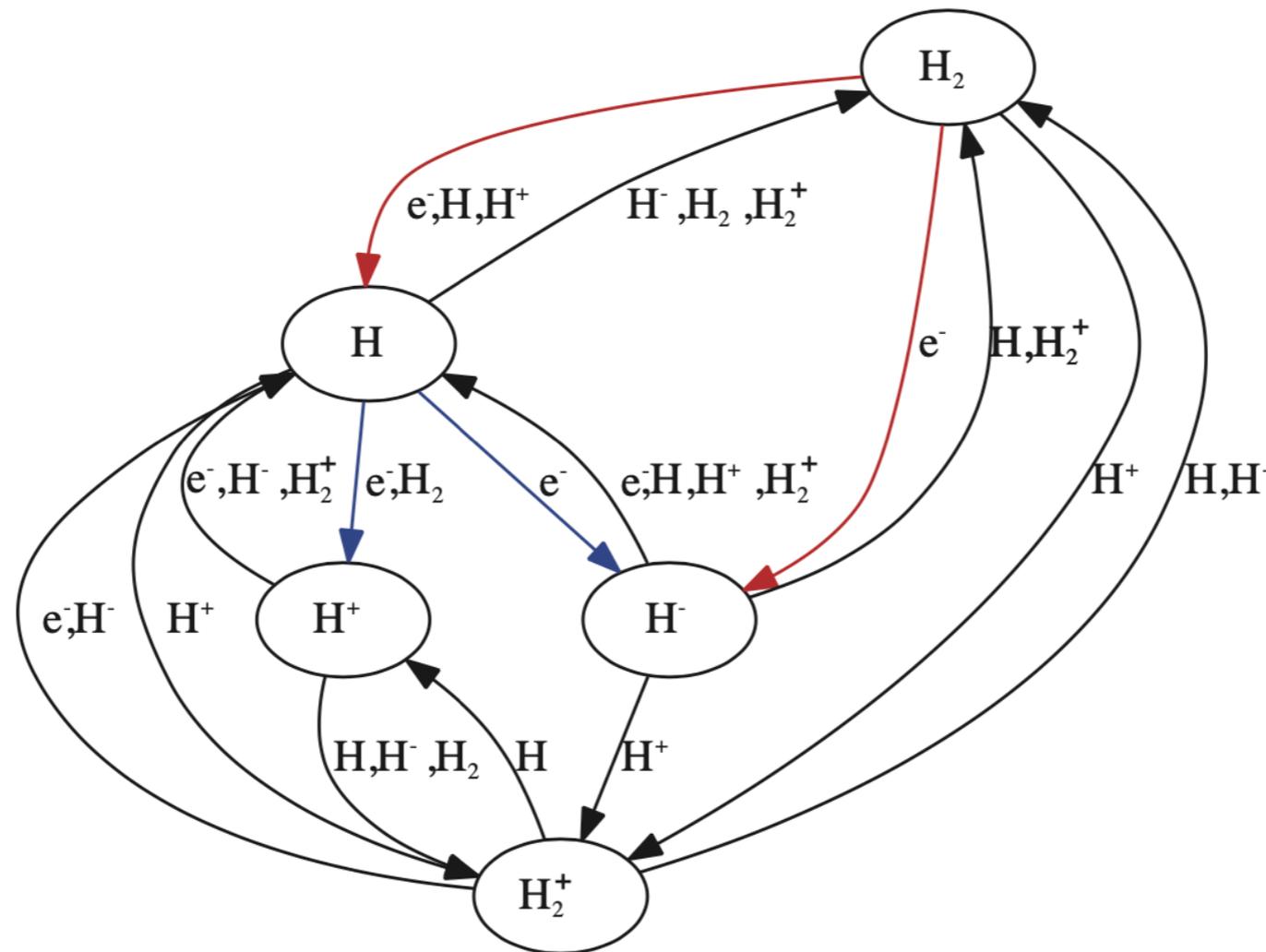


primordial chemistry



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primordial chemistry networks largely focus on H_2 as primary coolants



Bovino & Galli (2019, in Formation of the First Black Holes, eds. Latif M. and Schleicher D.R.G), using KROME, see Grassi et al. (2014, MNRAS, 439, 2386)

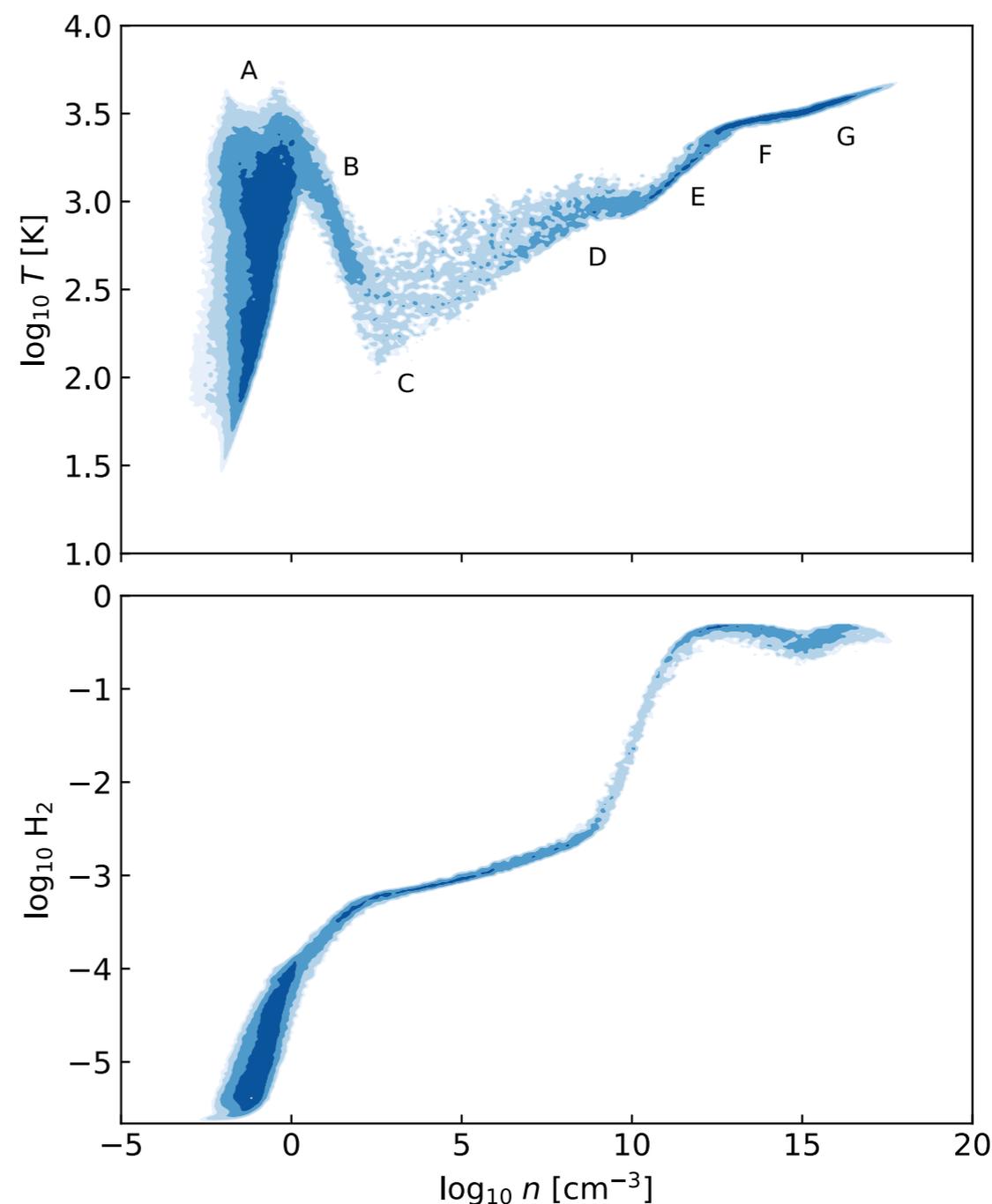
effective equation of state



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effective EOS constitutes a relation between temperature and density

- (A) gas flows into potential well and is compressionally heated
- (B) H₂ formation and run-away cooling
- (C) gas accumulates and collapse resumes
- (D) 3-body H₂ formation sets in and gas becomes fully molecular
- (E) gas becomes optically thick and temperature rises further
- (F) collision-induced emission (CIE) becomes important coolant
- (G) at T ~ 2000 K H₂ dissociation sets in



Klessen & Glover (2023, ARAA, 61, 65 -- arXiv.2303.12500)

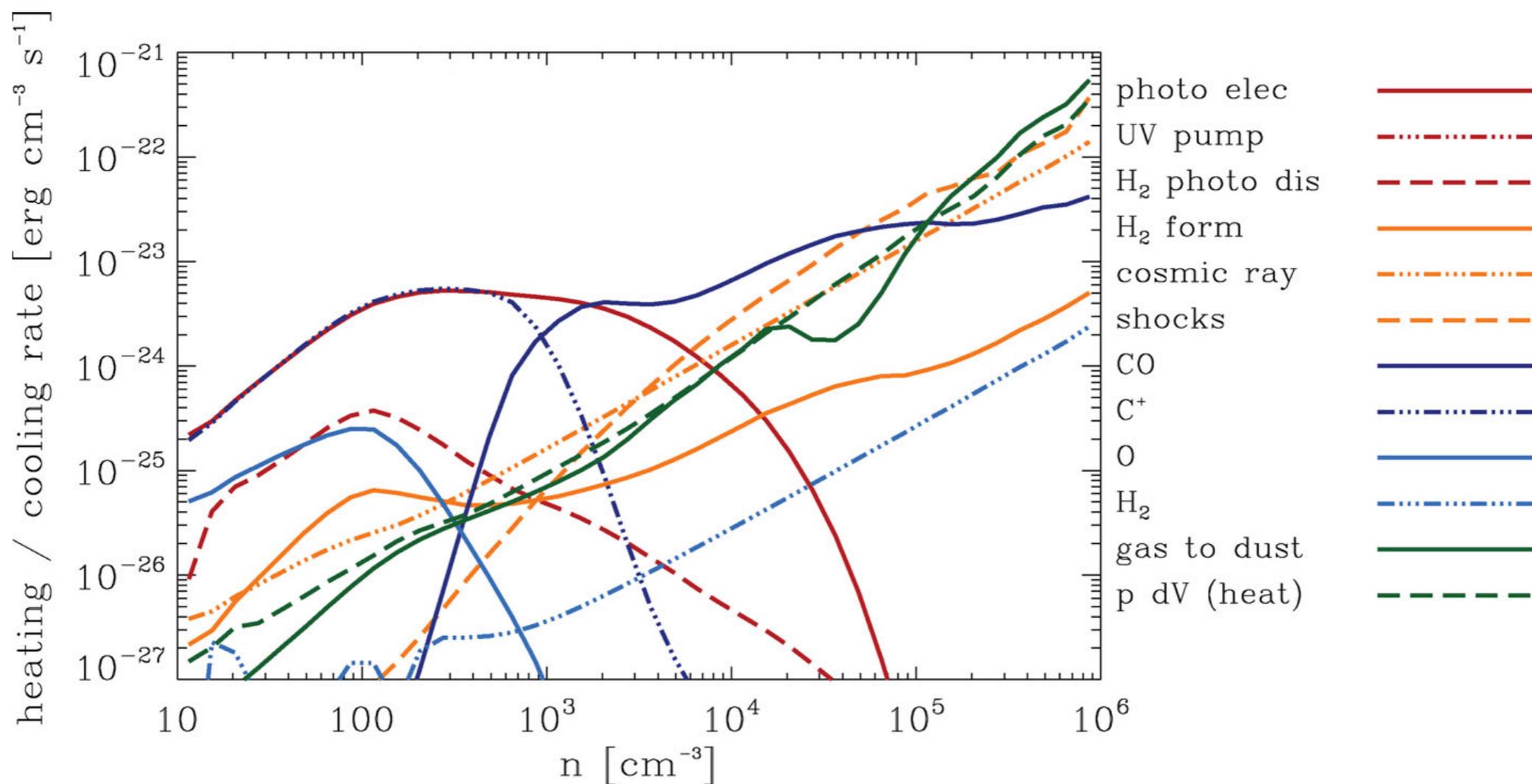
inspired by Yoshida et al. (2006, ApJ, 652, 6)
using data of Lewis Prole and Anna Schauer

heating and cooling processes at $Z \sim Z_{\text{sun}}$



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overview of main heating and cooling processes as function of hydrogen nuclei number density n



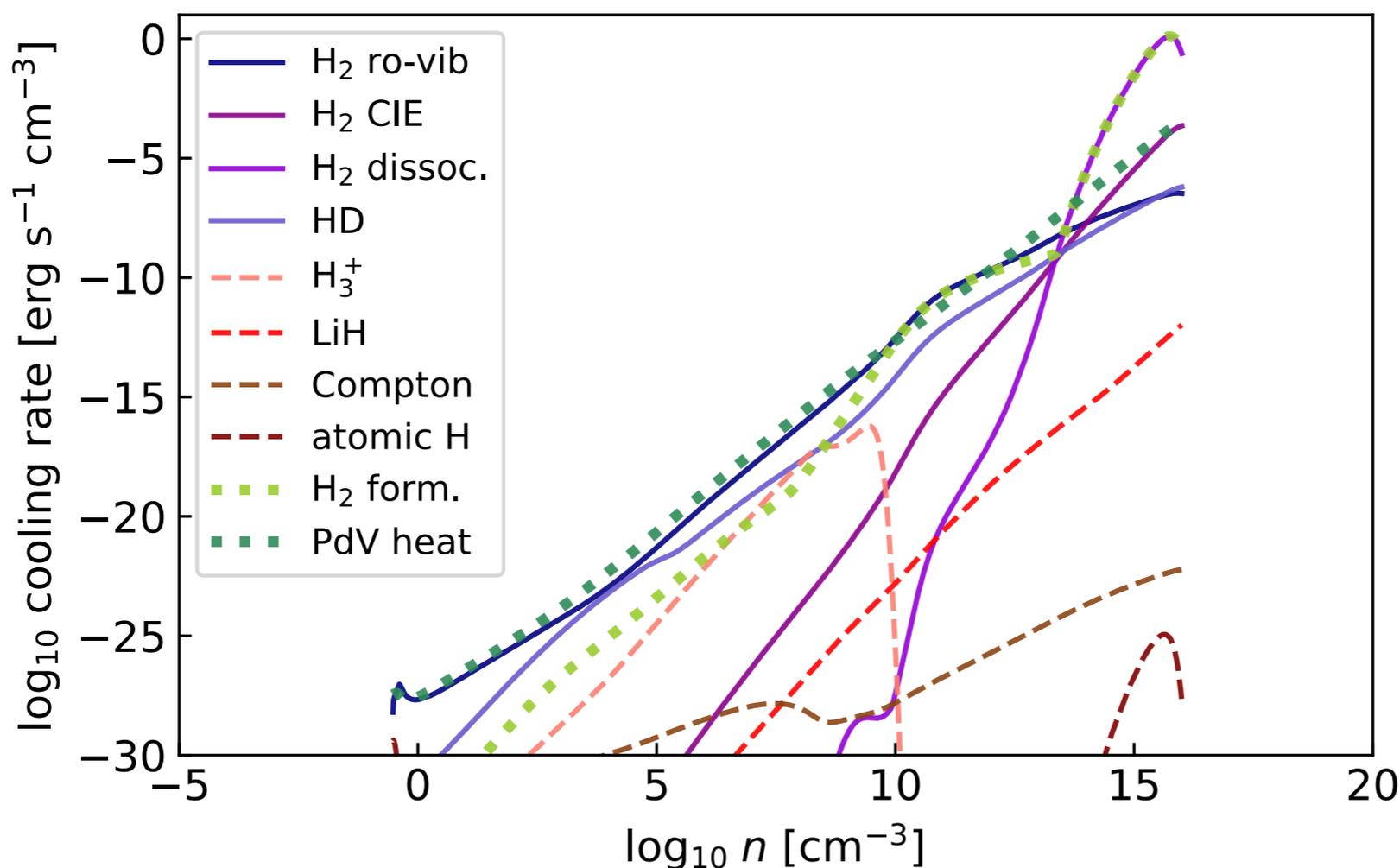
(Klessen, & Glover (2016, SAAS, 43, 85), figure from Glover & Clark (2012, MNRAS, 421, 9)

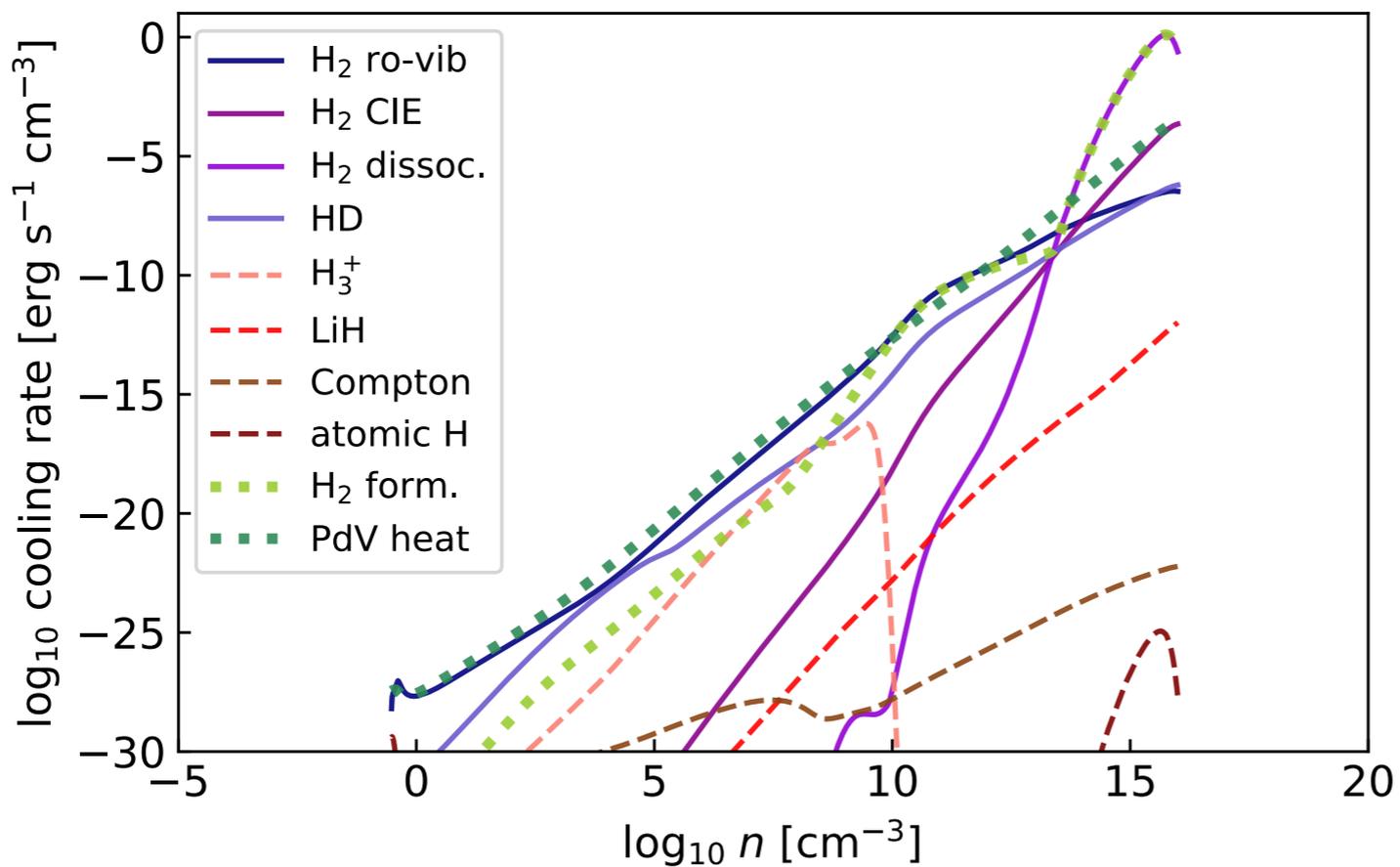
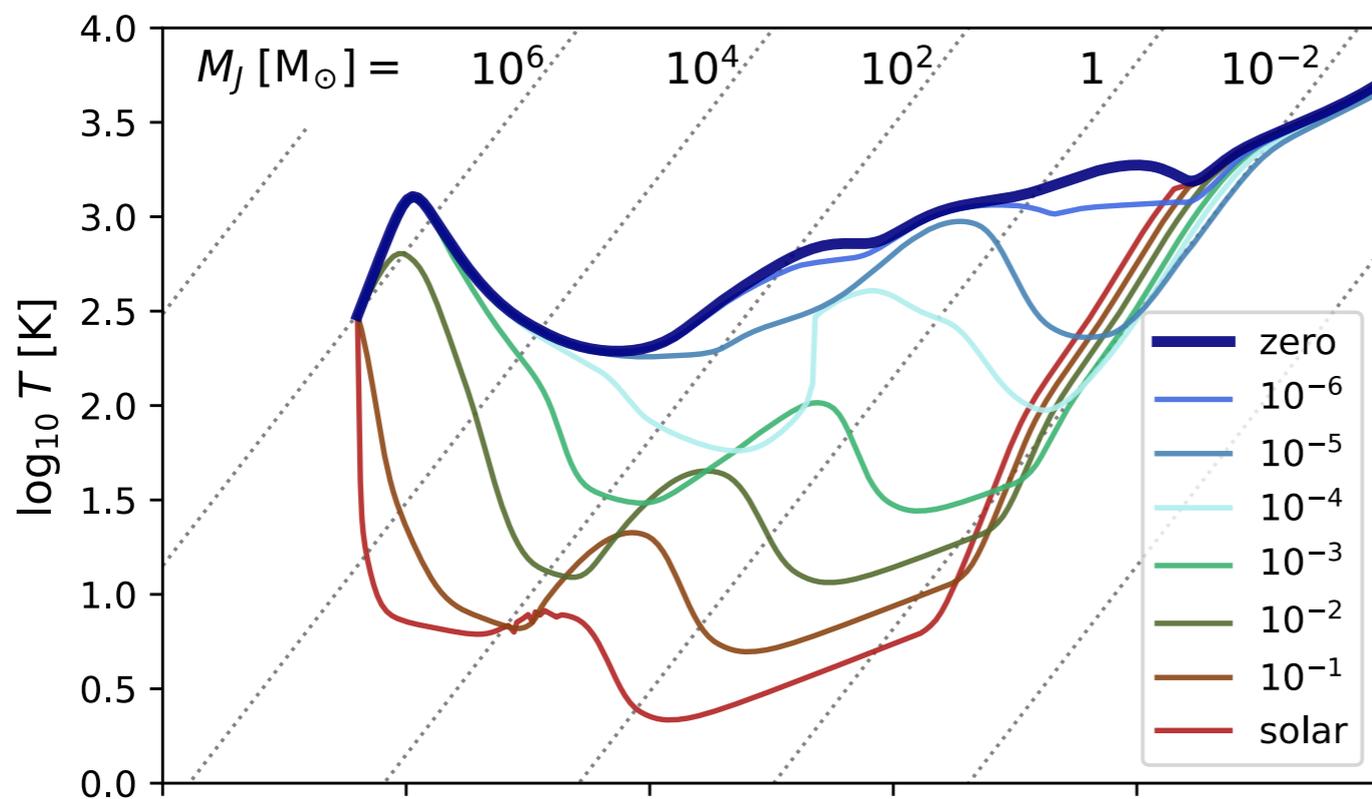
heating and cooling processes at $Z \sim 0$



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overview of main heating and cooling processes as function of hydrogen nuclei number density n





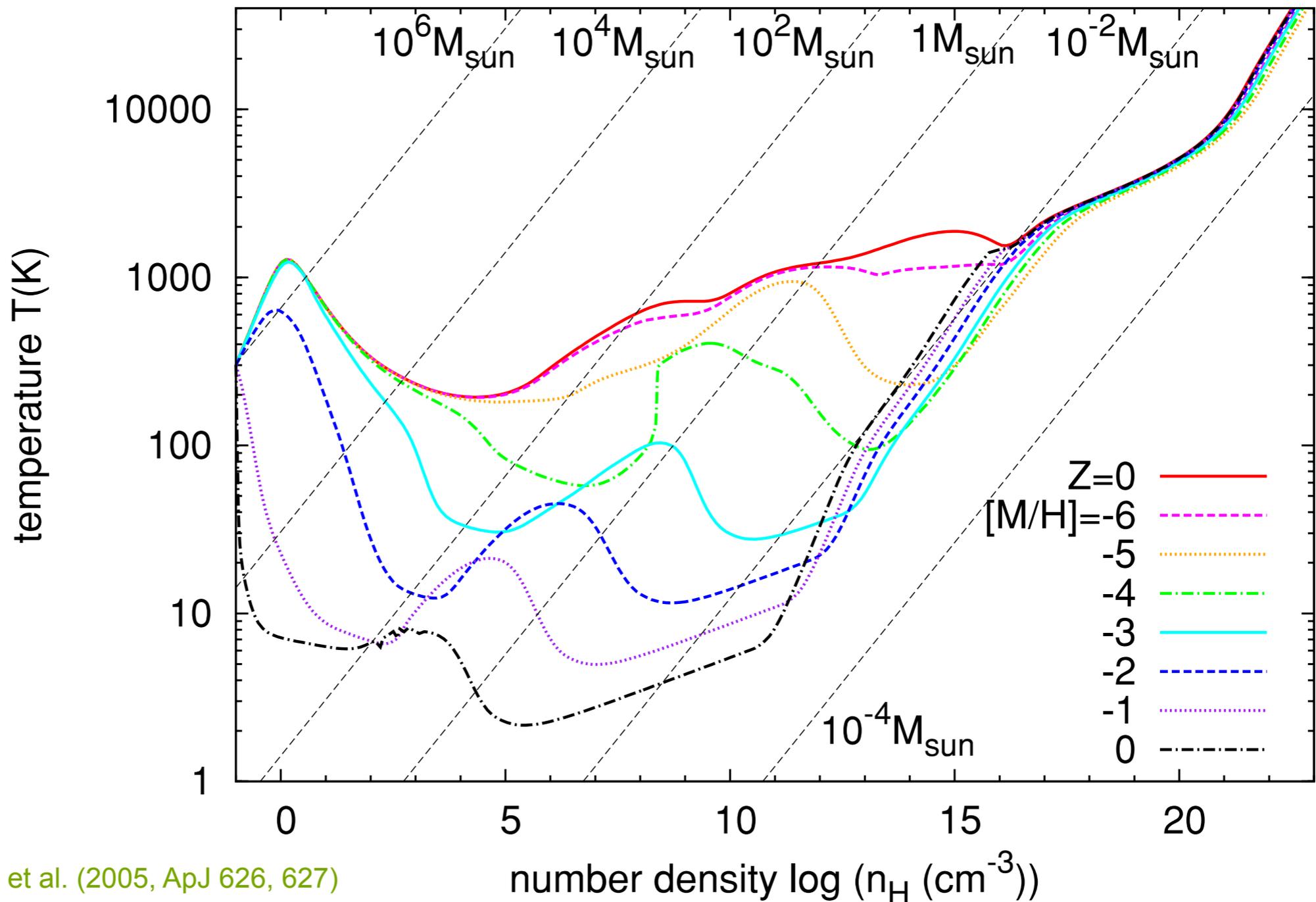
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this can be combined with simple 1D collapse calculations and looking at the density and temperature in the central core

EOS as function of metallicity



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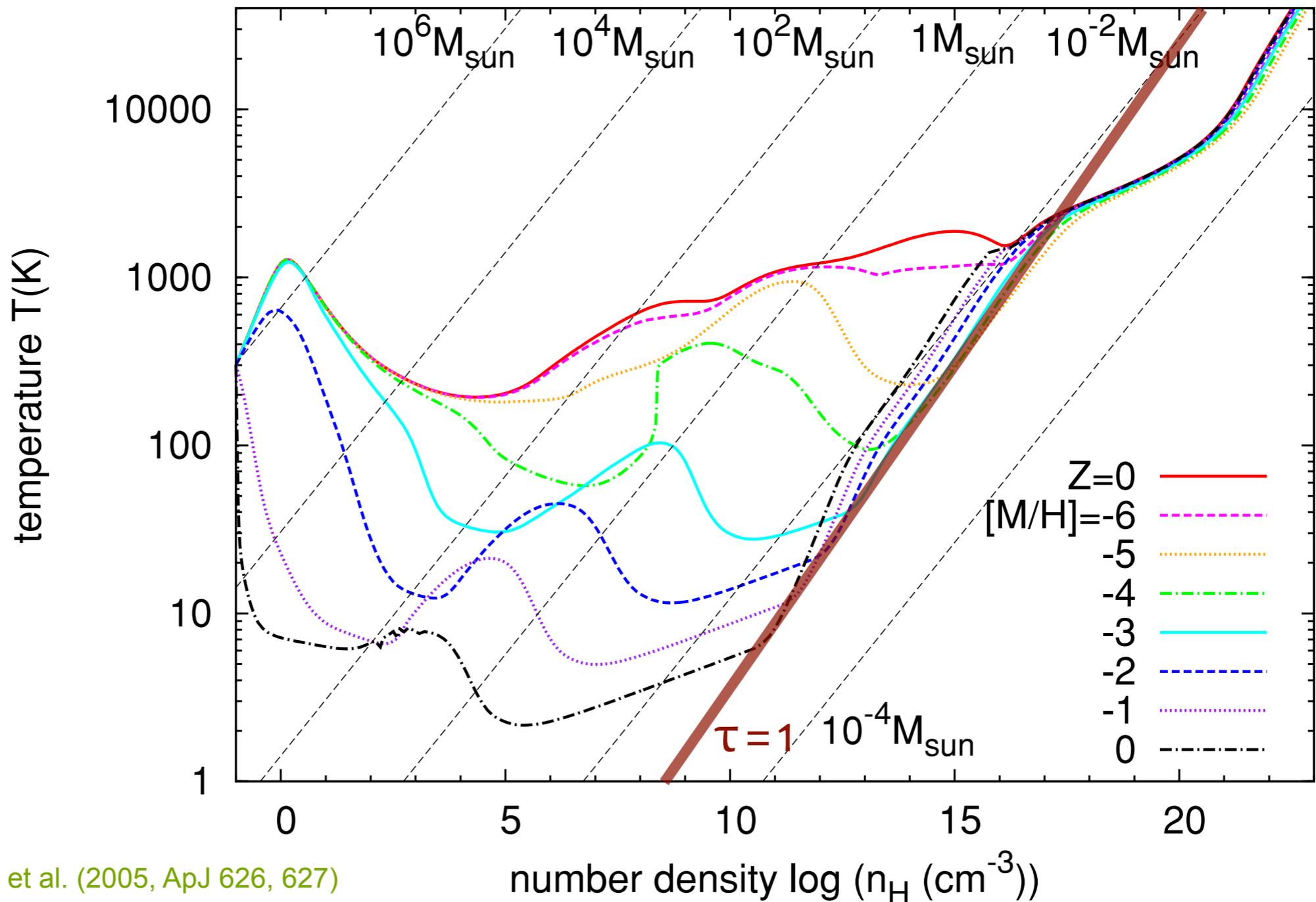


Omukai et al. (2005, ApJ 626, 627)

EOS as function of metallicity



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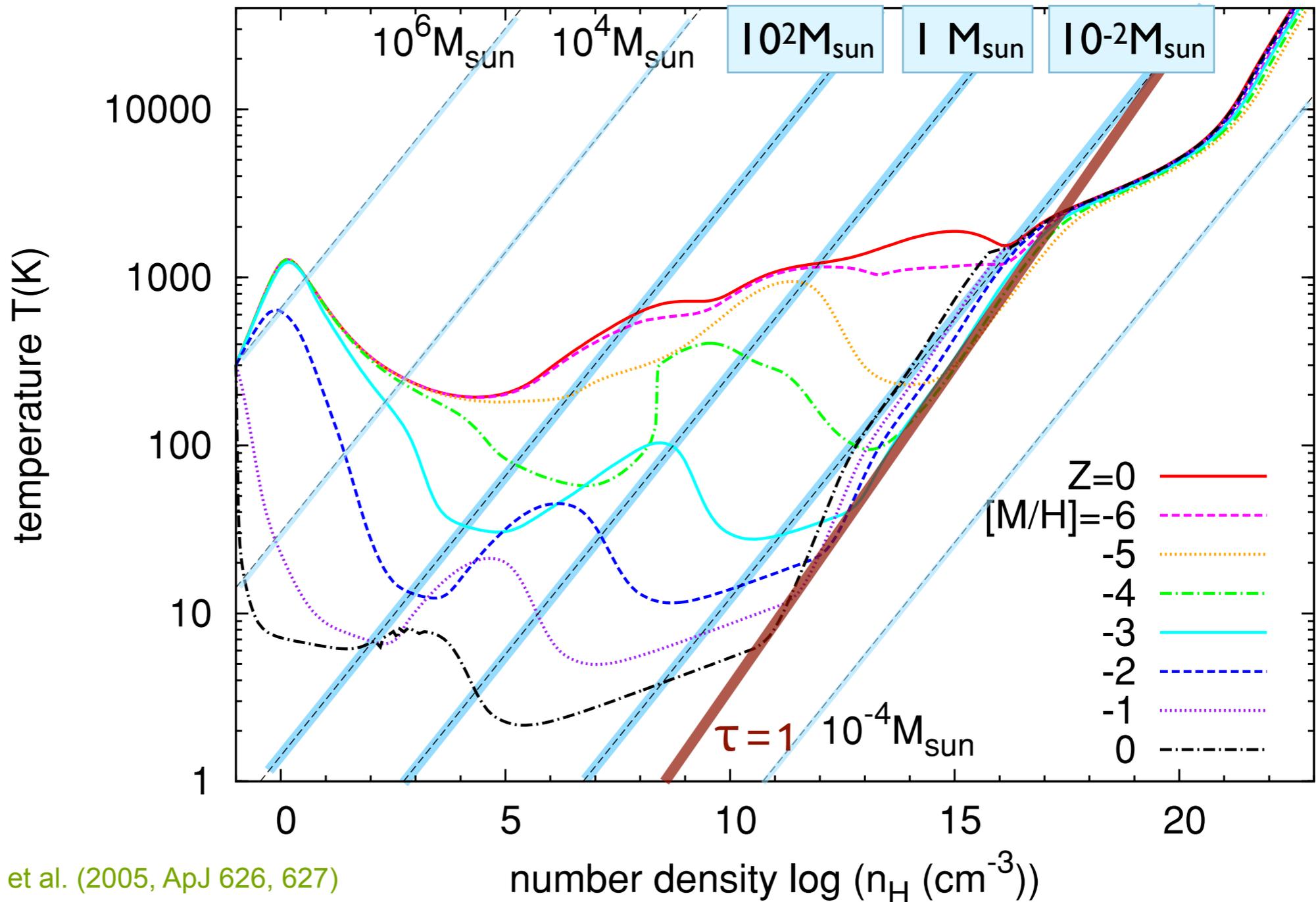


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EOS as function of metallicity



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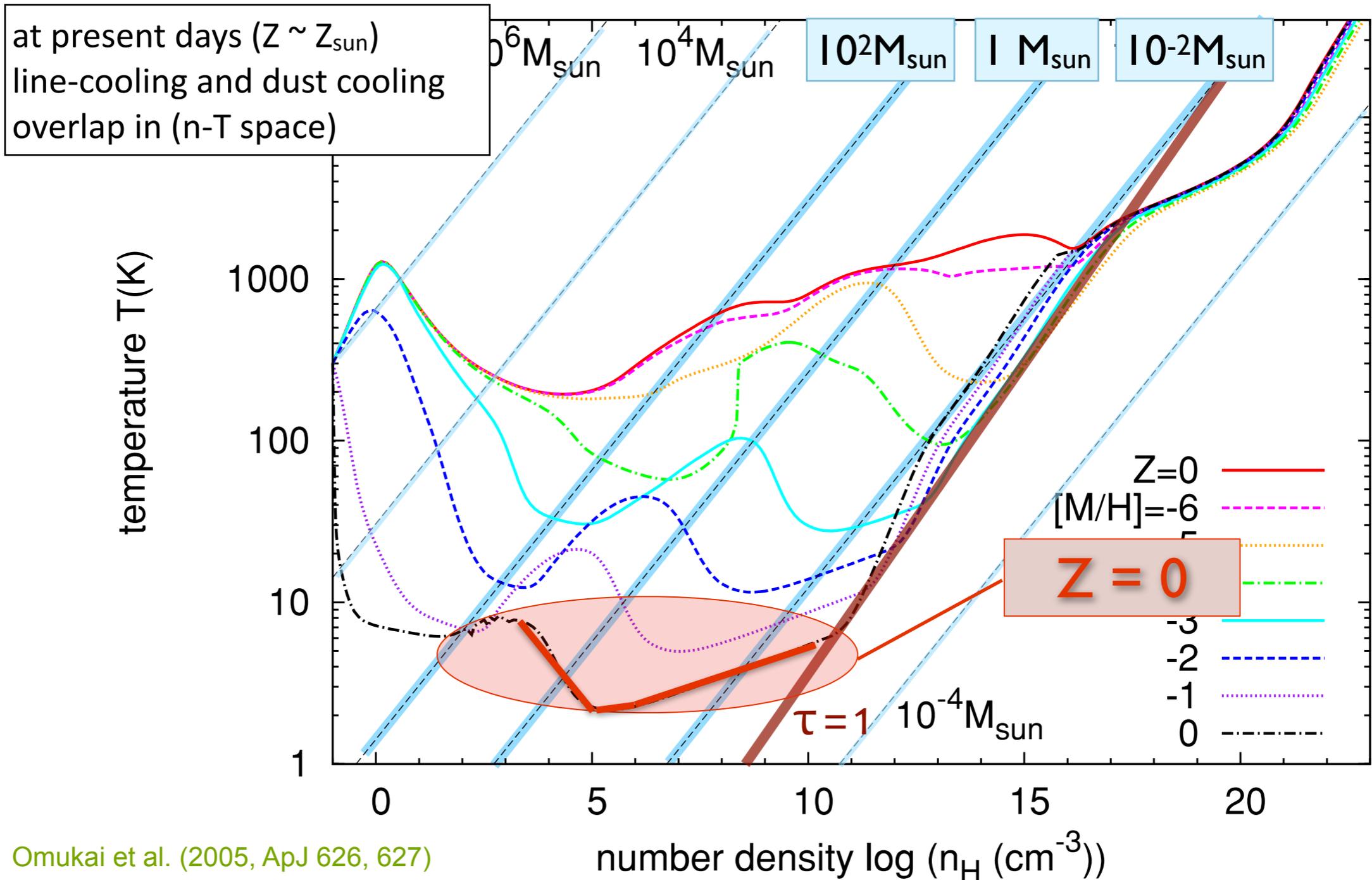


Omukai et al. (2005, ApJ 626, 627)

EOS at present days



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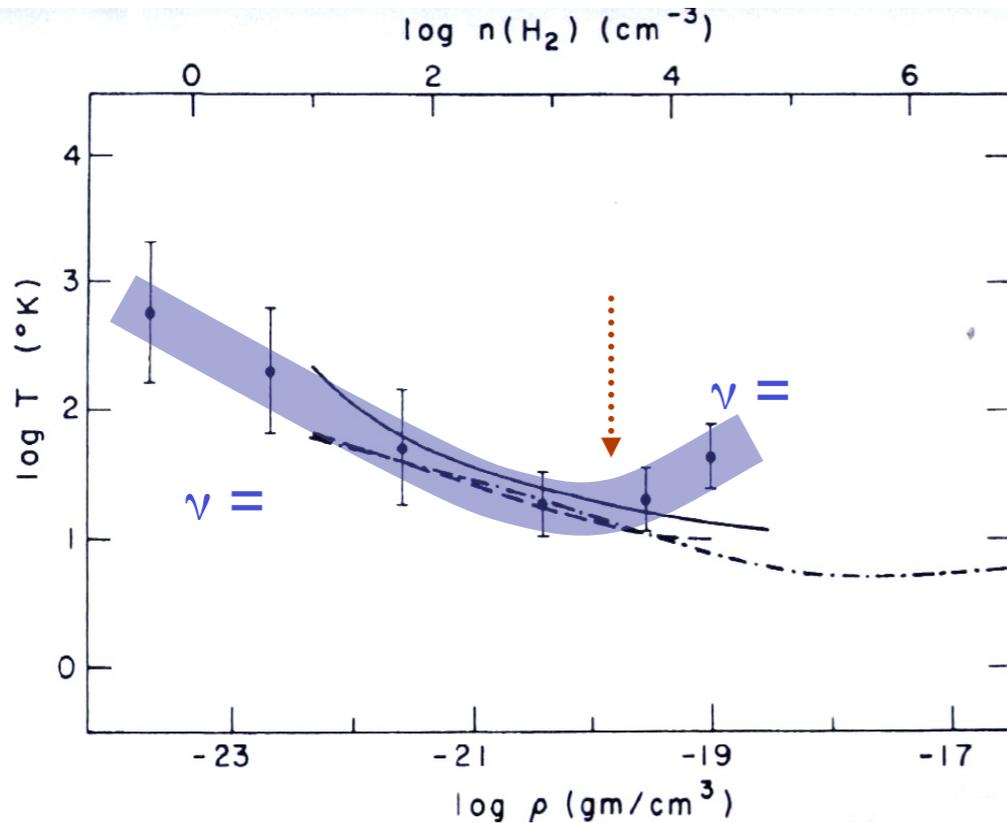
Omukai et al. (2005, ApJ 626, 627)

present-day SF

characteristic mass from 'kink' in EOS

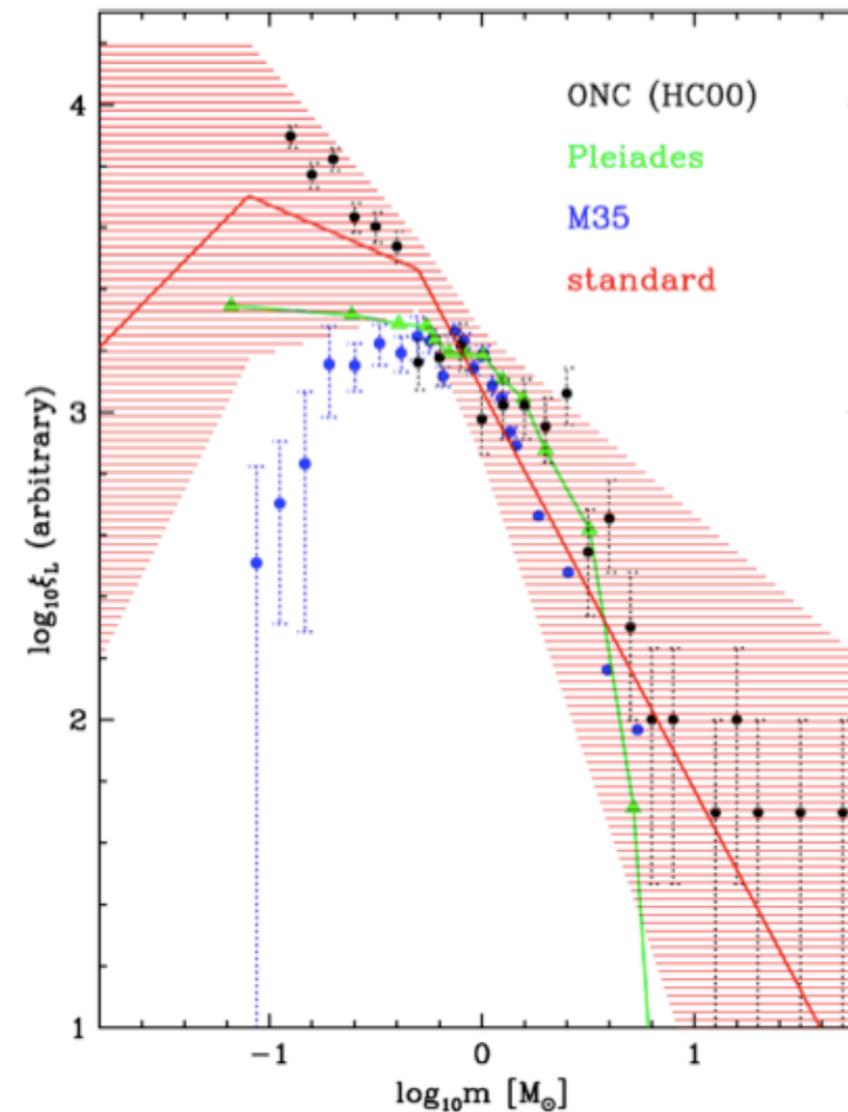


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it has been proposed almost 40 years ago, that this kink sets the characteristic mass of the stellar IMF

Larson (1985, MNRAS, 214, 379),
Larson (2005, MNRAS, 359, 211),

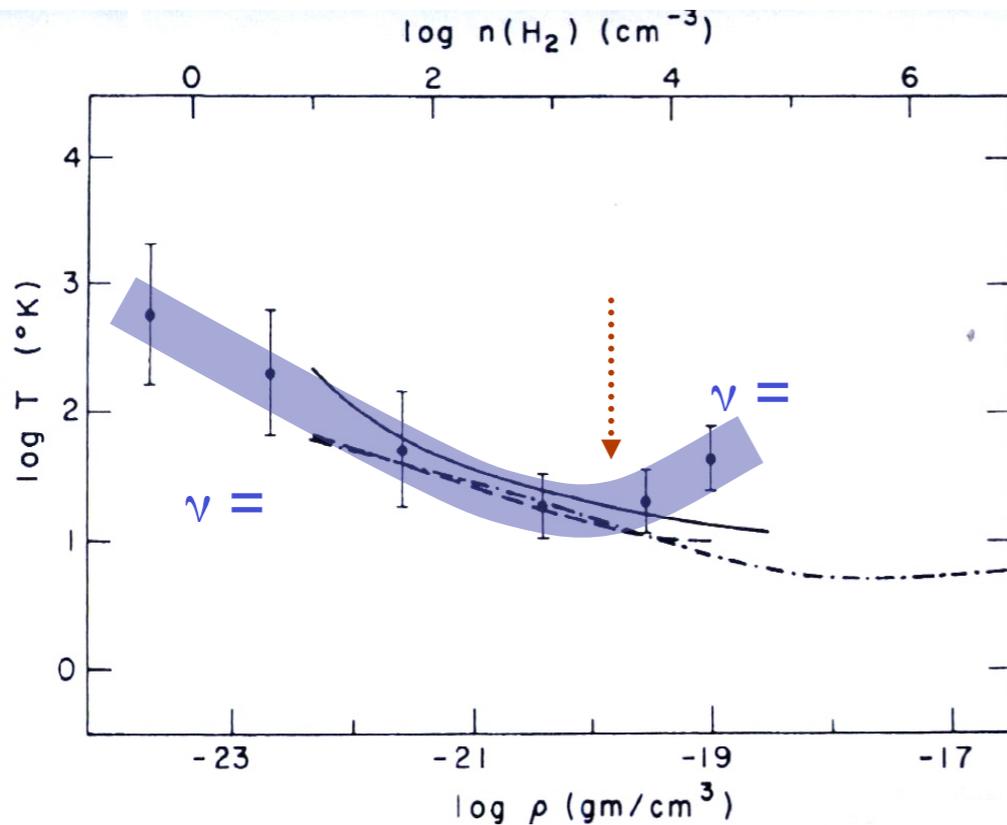


Kroupa (2002, Science, 295, 82)

characteristic mass from 'kink' in EOS

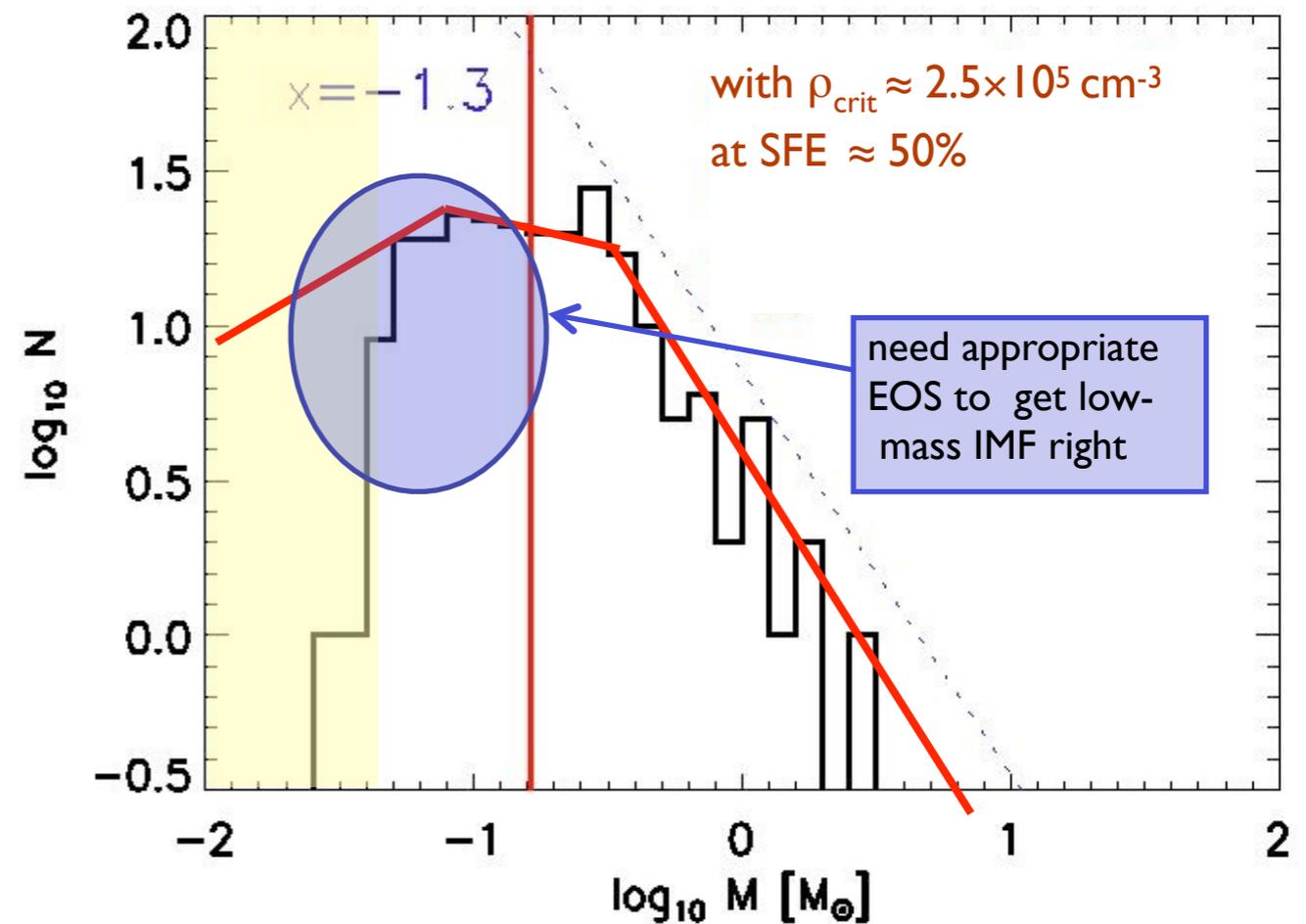


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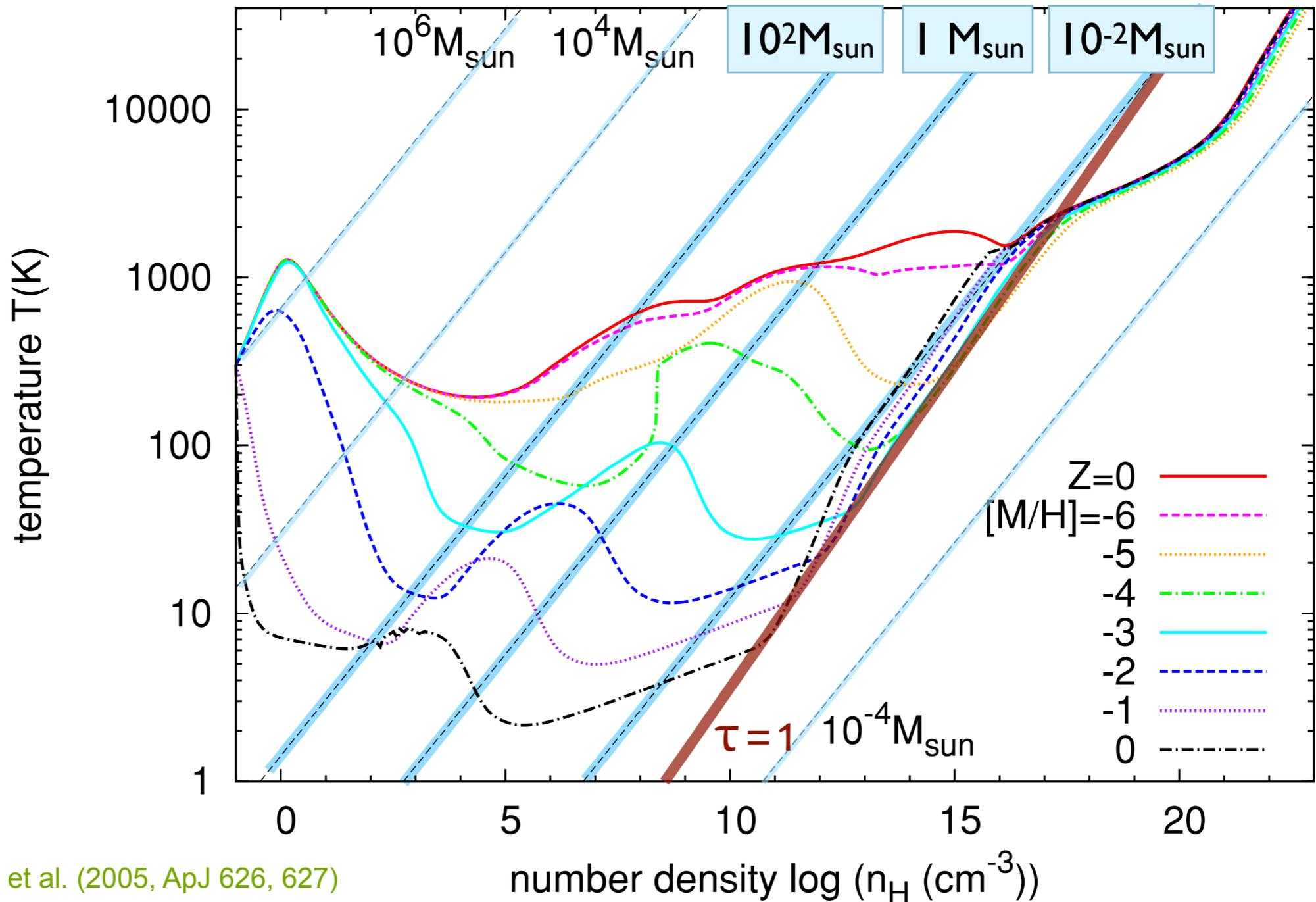
this is supported by numerical simulations

Jappsen et al. (2005, A&A, 435, 611)

EOS as function of metallicity



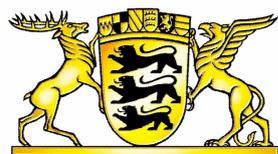
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Omukai et al. (2005, ApJ 626, 627)



Pop III stars



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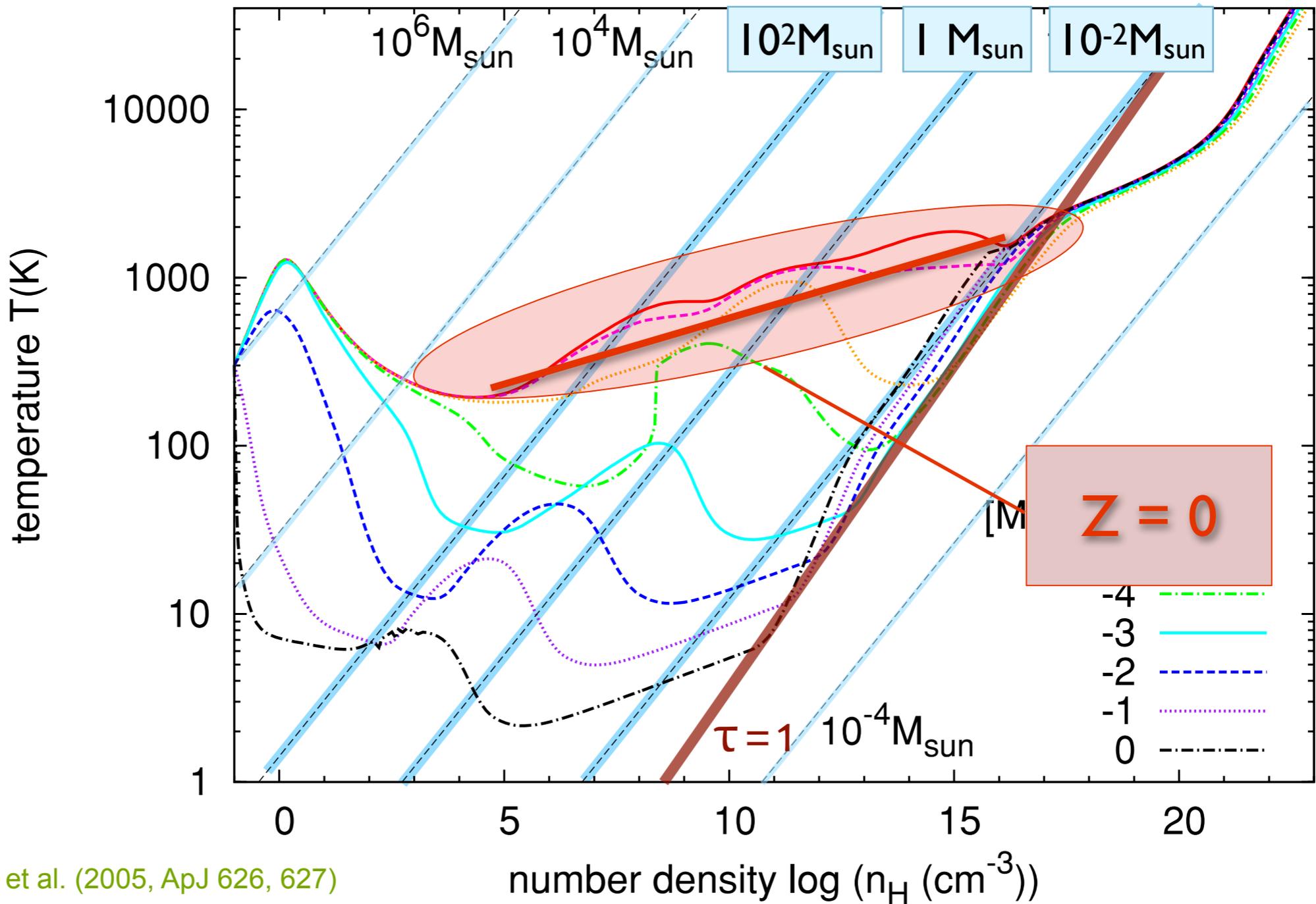


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Pop III stars

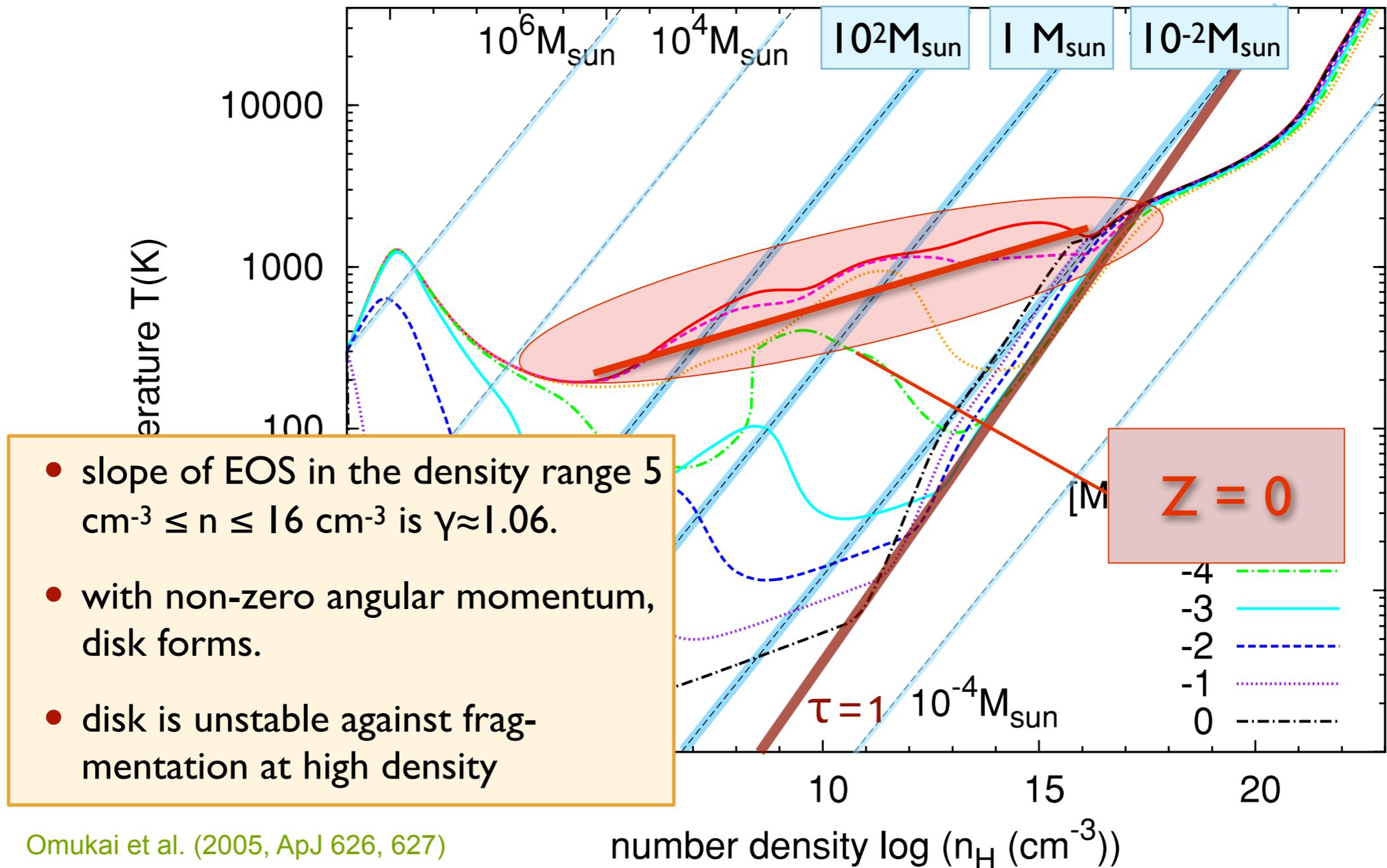


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Omukai et al. (2005, ApJ 626, 627)

Pop III stars



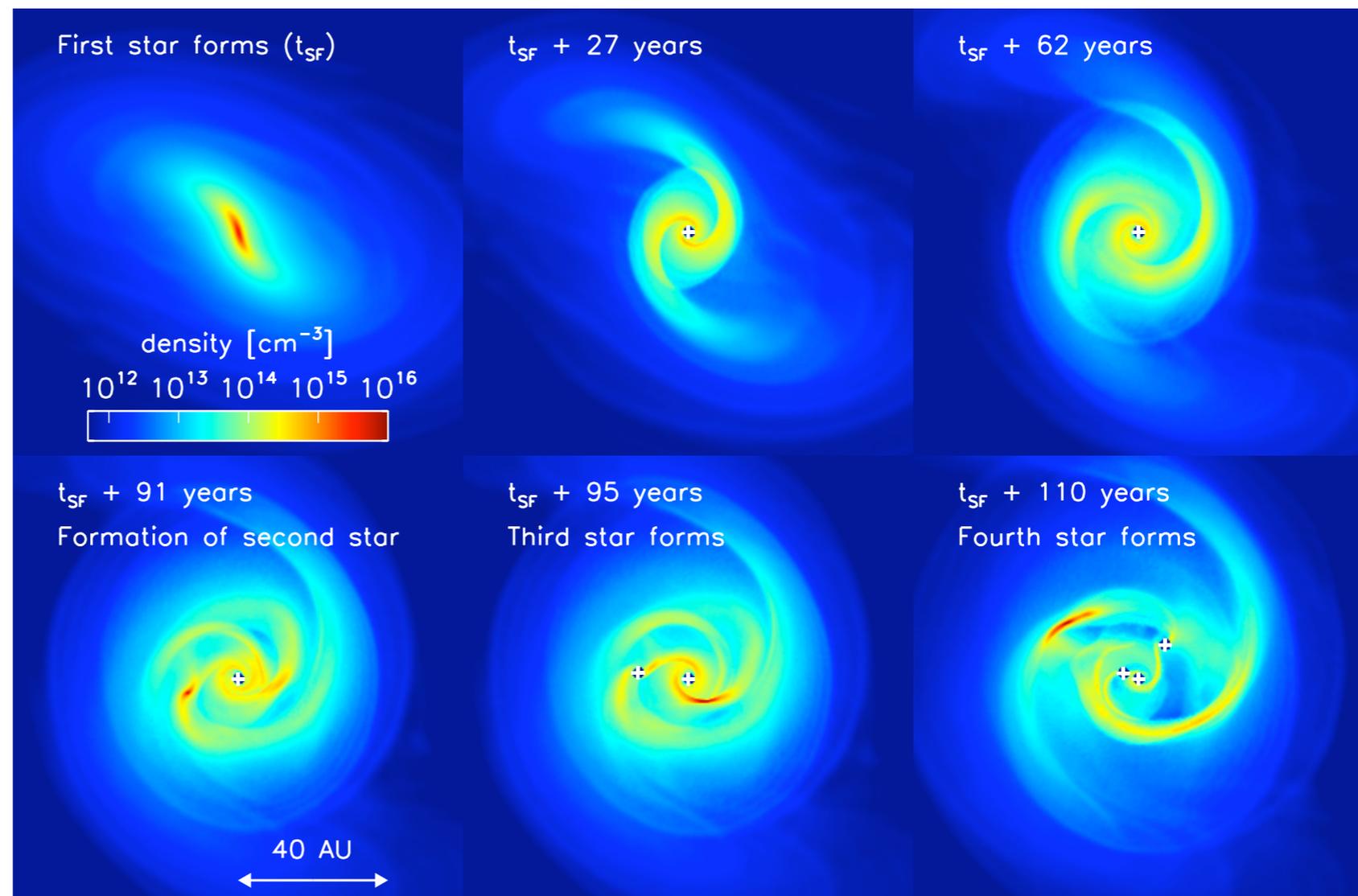
Omukai et al. (2005, ApJ 626, 627)

Pop III stars



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multiple Pop III stars form by disk fragmentation



Clark et al. (2011, Science, 331, 1040)

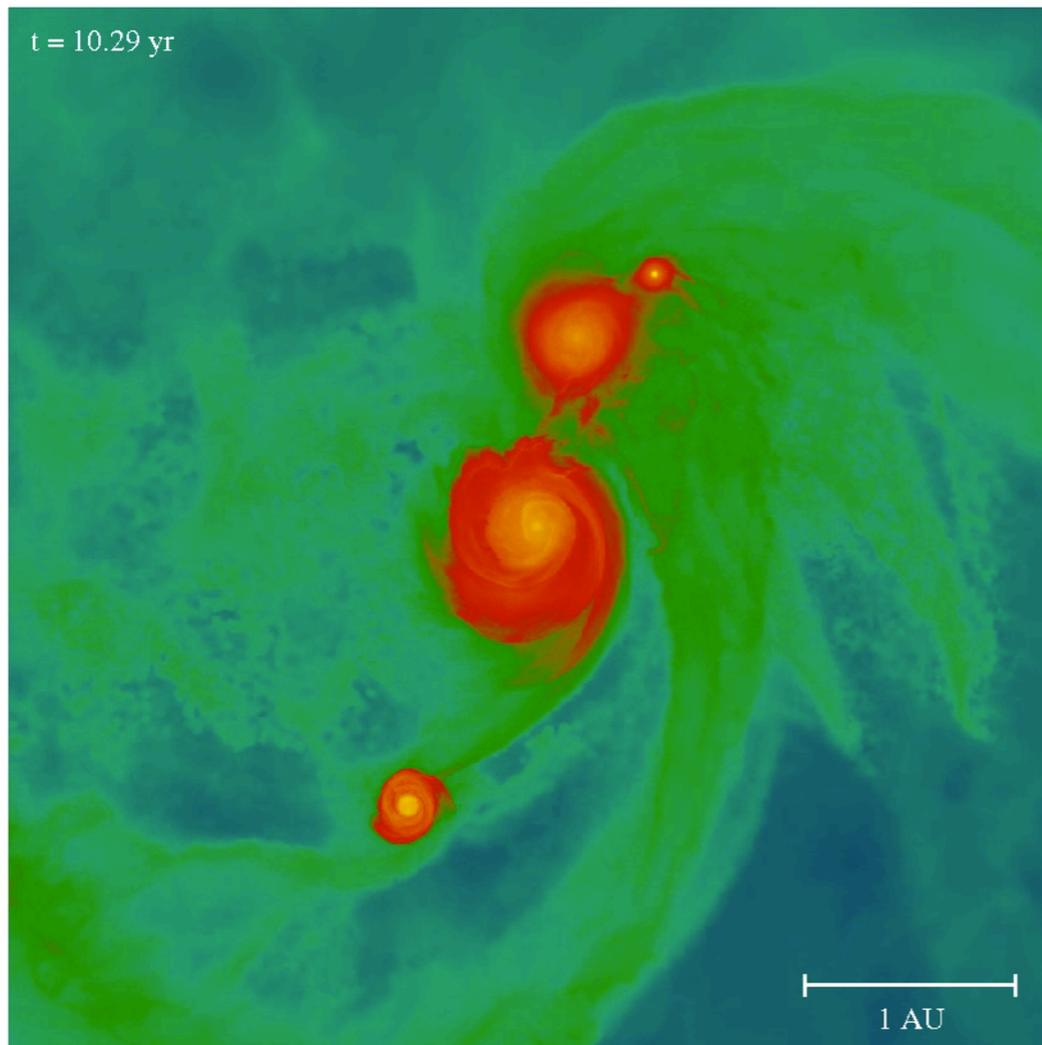
disk fragmentation

Pop III stars

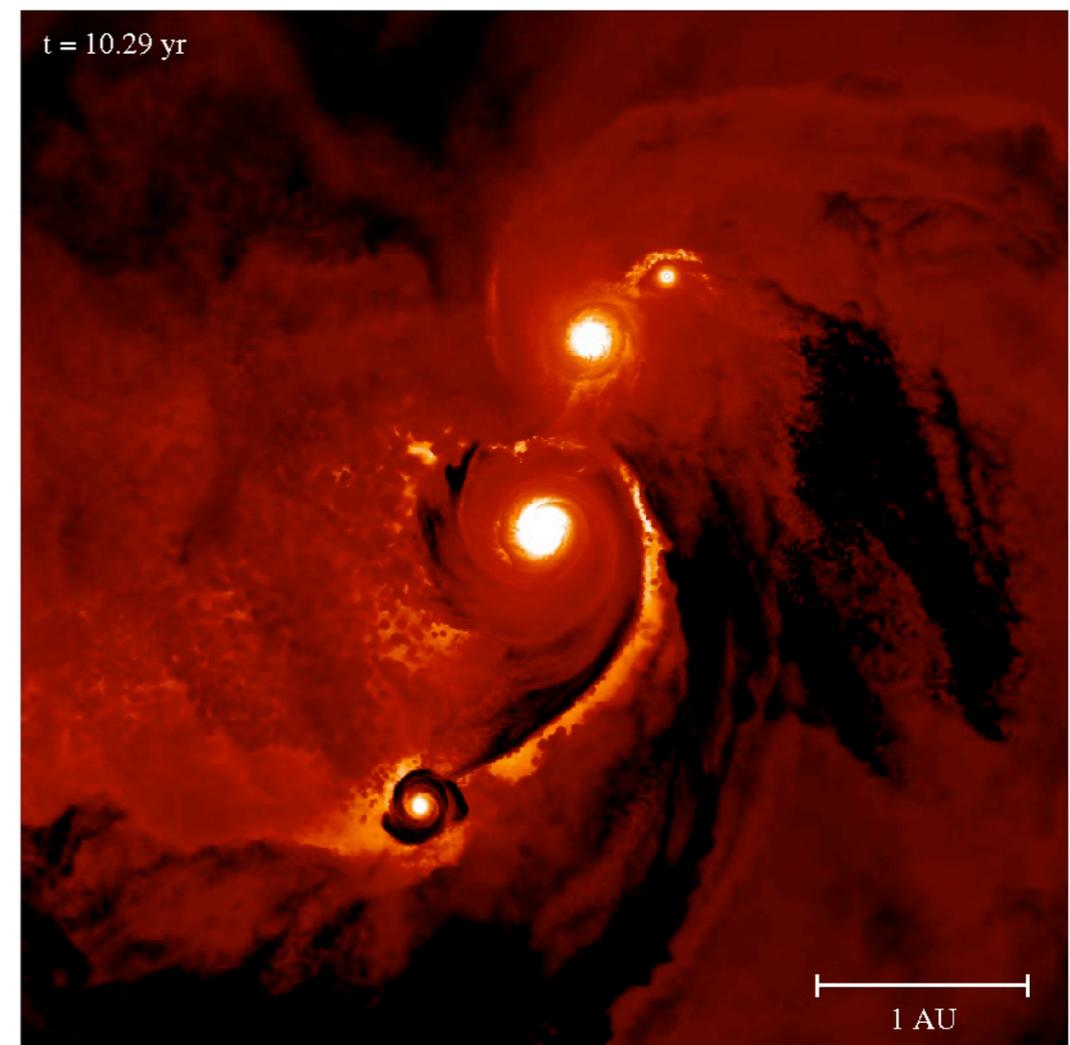


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multiple Pop III stars form by disk fragmentation



density

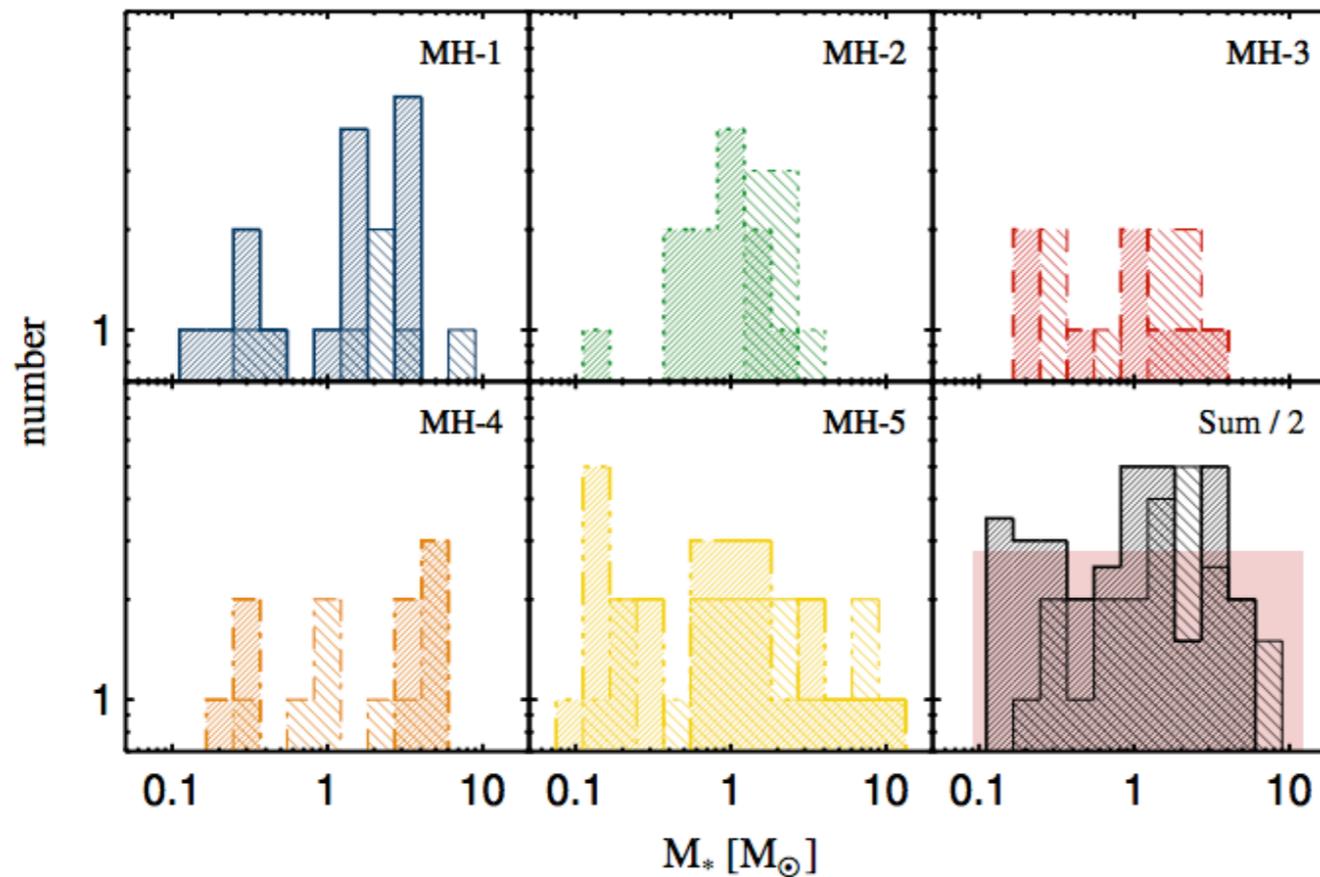


temperatur

IMF of Pop III stars



simulations suggest IMF of metal-free stars is log flat
(with hint for top-heaviness)



we see “flat”
mass spectrum

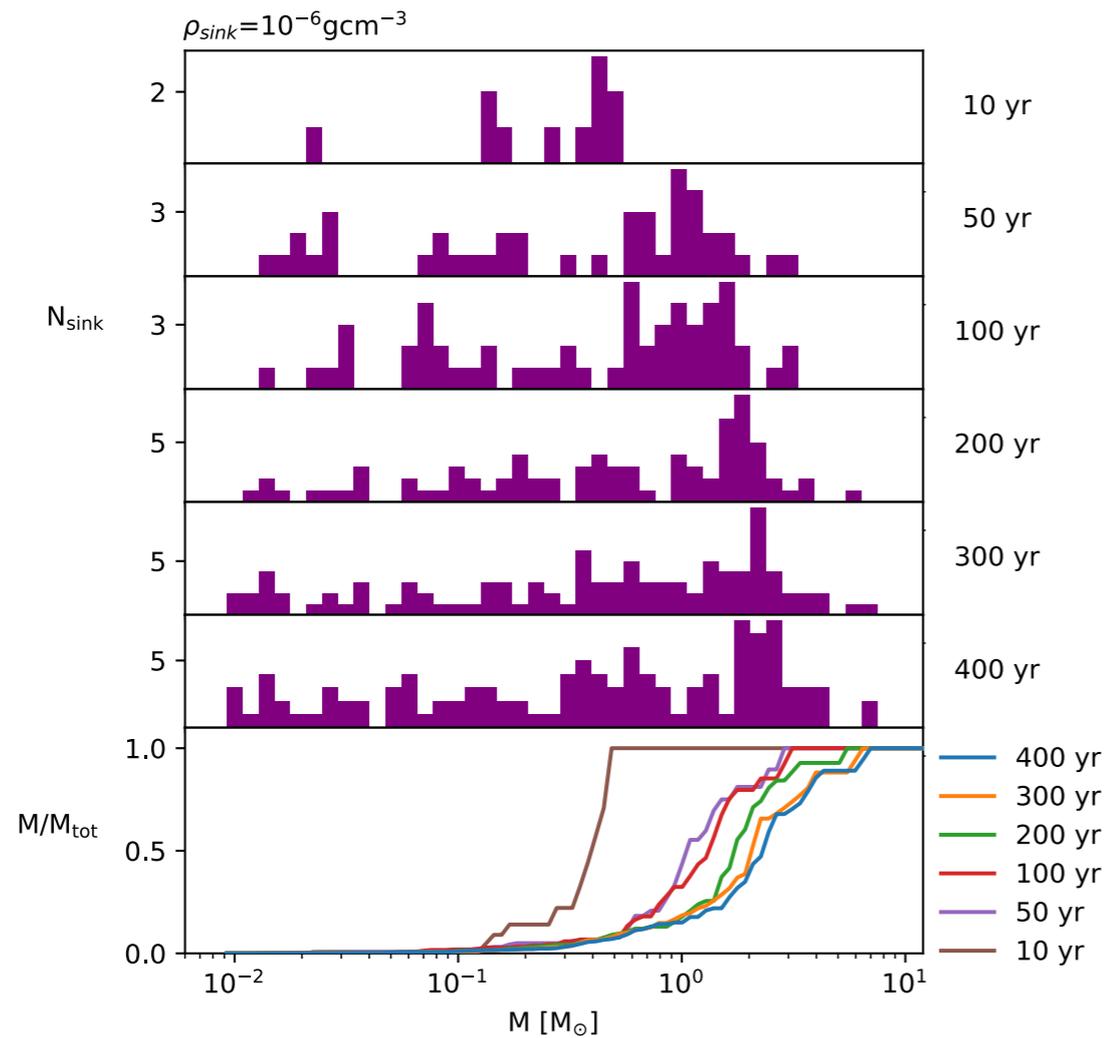
Greif et al. (2011, ApJ, 737, 75), Clark et al. (2011, Science, 331, 1040), Smith et al. (2011, MNRAS, 414, 3633), Dopcke et al. (2013, ApJ, 766, 103), Hirano et al. (2014, ApJ, 781, 60), Tanaka & Omukai (2014, MNRAS, 439, 1884), Nakauchi et al. (2014, MNRAS, 442, 2667), Wollenberg et al. (2020, MNRAS, 494, 1871), Prole et al. (2022, MNRAS, 510, 4019), Prole et al. (2022, MNRAS, 516, 2223), and many more

IMF of Pop III stars



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simulations suggest IMF of metal-free stars is log flat
(with hint for top-heaviness)



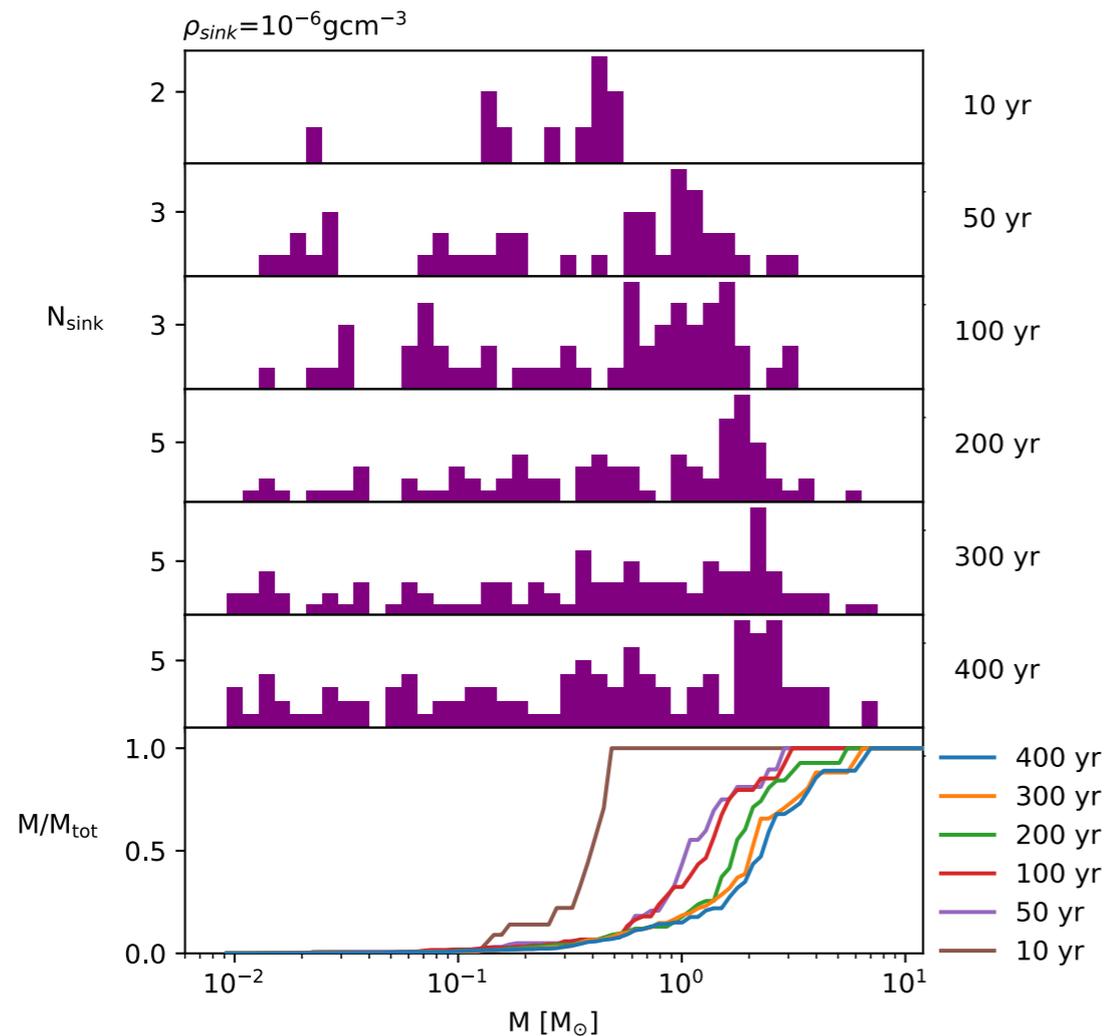
Prole et al. (2022, MNRAS, 510, 4019)

IMF of Pop III stars

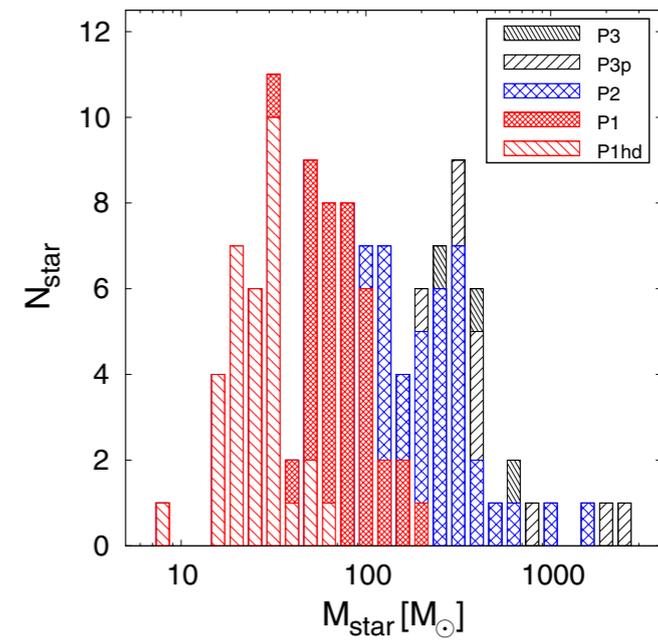


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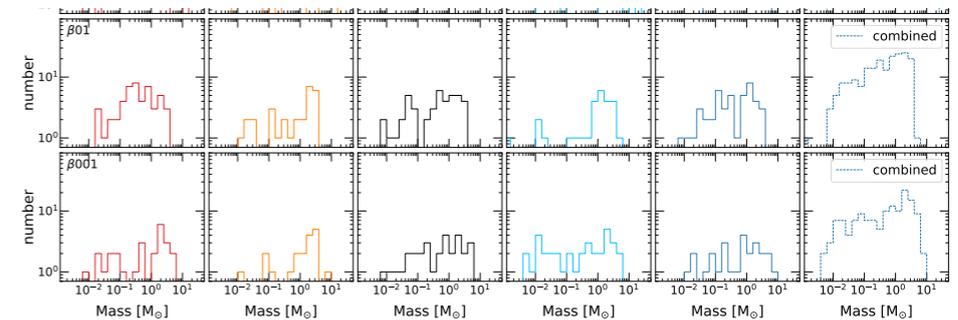
simulations suggest IMF of metal-free stars is log flat (with hint for top-heaviness)



Prole et al. (2022, MNRAS, 510, 4019)



Hirano et al. (2014, ApJ, 781, 60)



Wollenberg et al. (2020, MNRAS, 494, 1871)

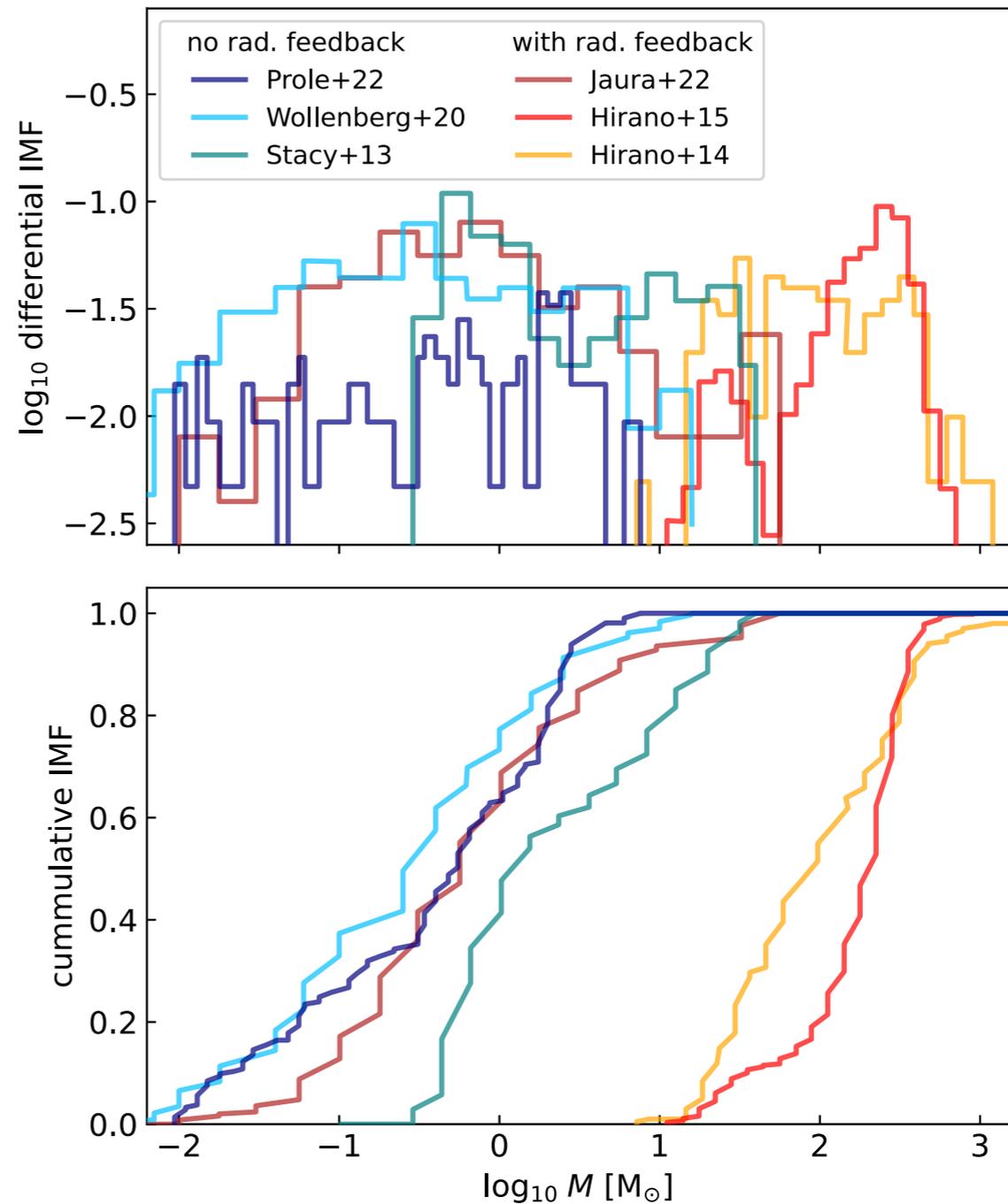
IMF of Pop III stars



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simulations suggest IMF of metal-free stars is log flat (meaning it is top heavy)

BUT: result depends strongly on *numerical resolution*, and on the *physics* involved, and on the way *feedback* is taken into account.

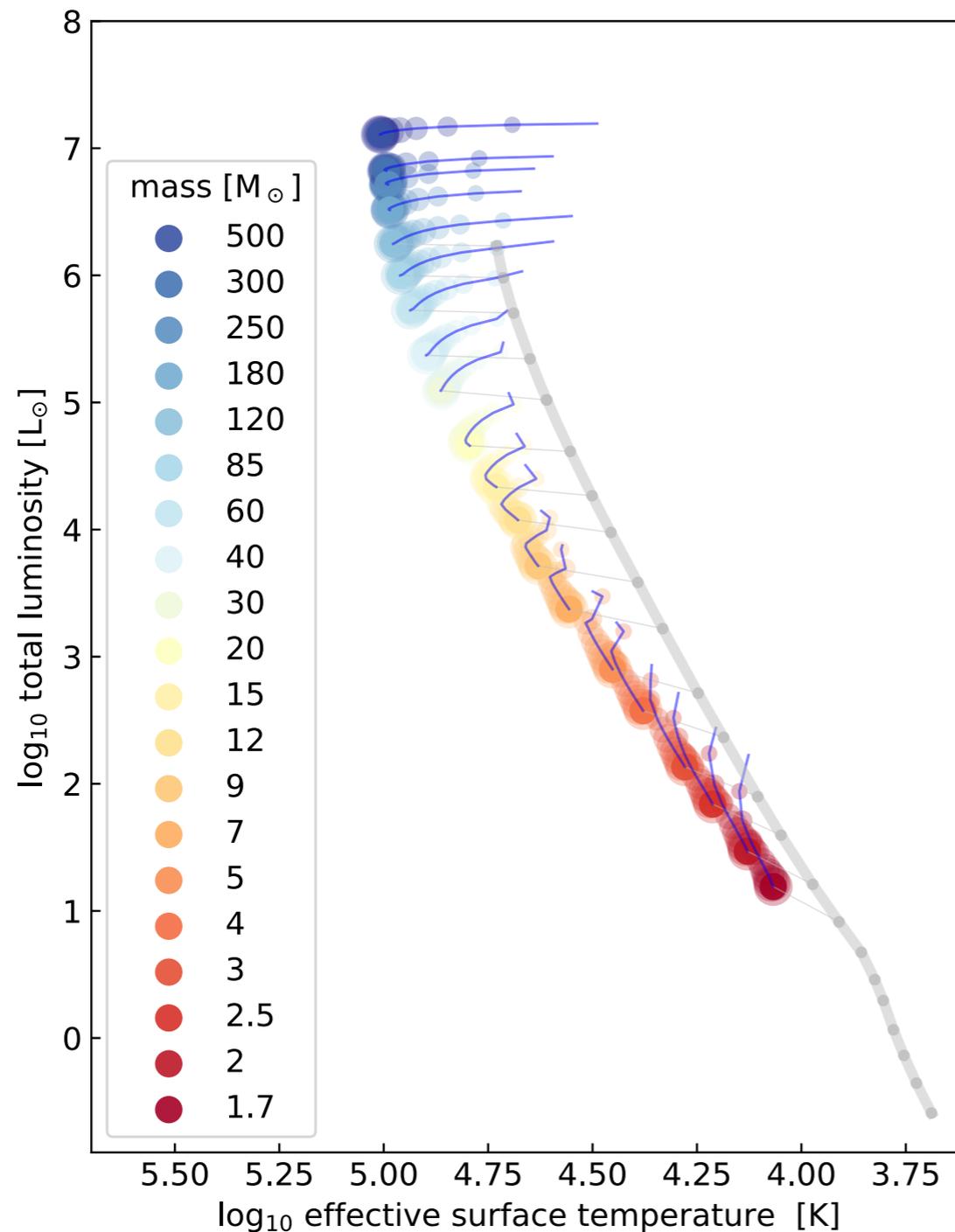


(Klessen, & Glover (2023, ARAA, 61, 65 -- arXiv.2303.12500))

some properties of Pop III stars



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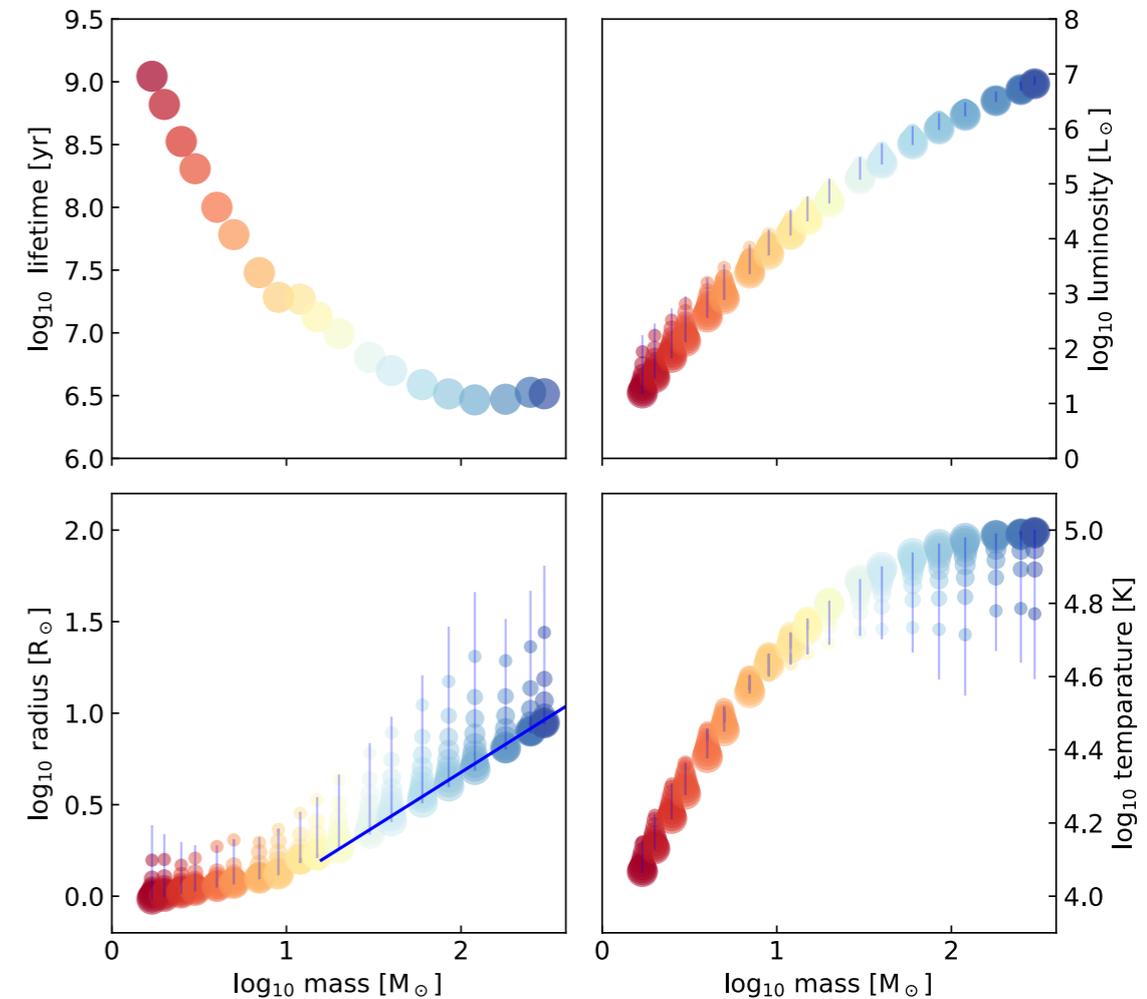
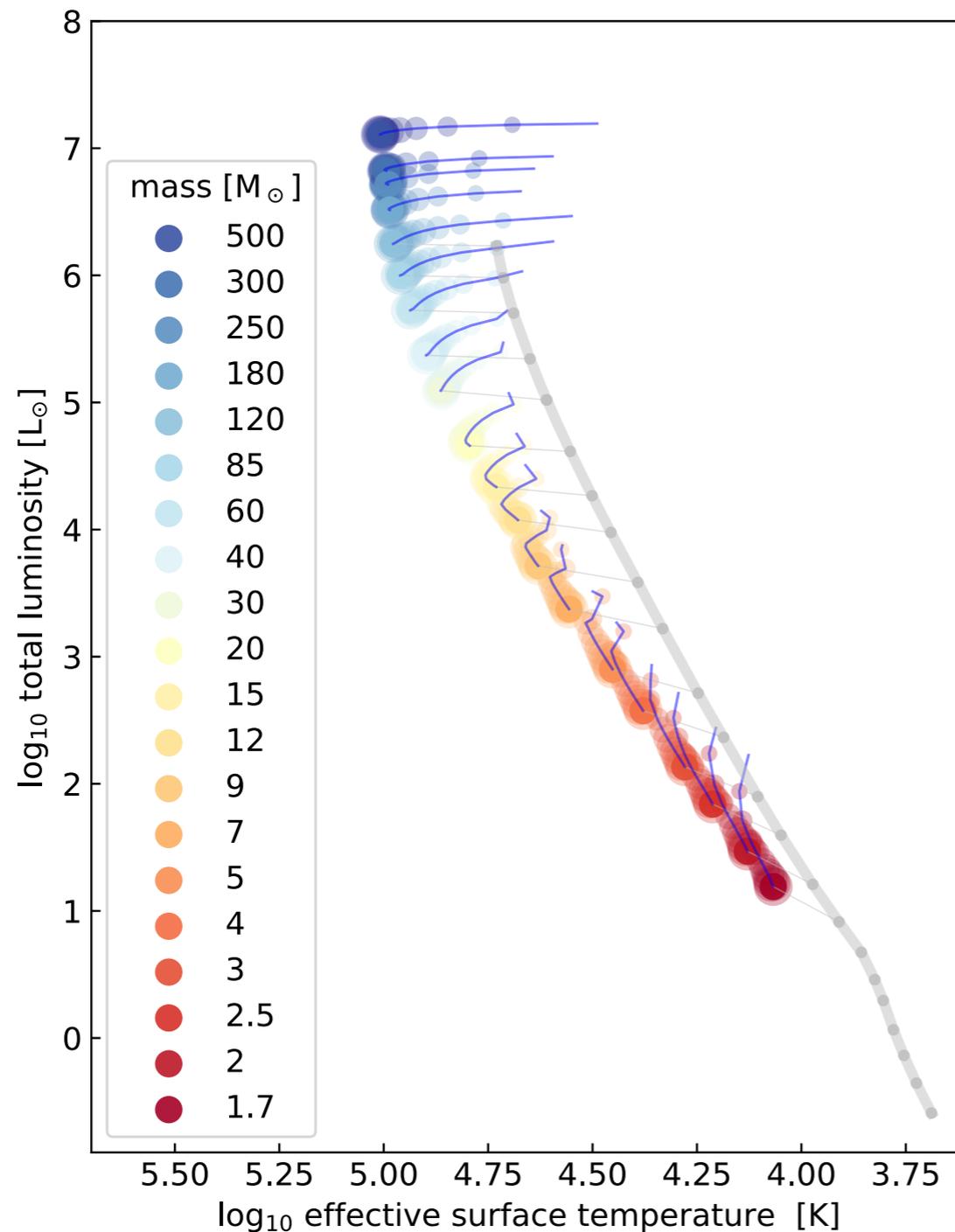
Pop III stars are typically more compact and hotter than their Pop II/I counterparts. But they have similar bolometric luminosity.

Klessen, & Glover (2023, ARAA, 61, 65 -- arXiv.2303.12500)

some properties of Pop III stars



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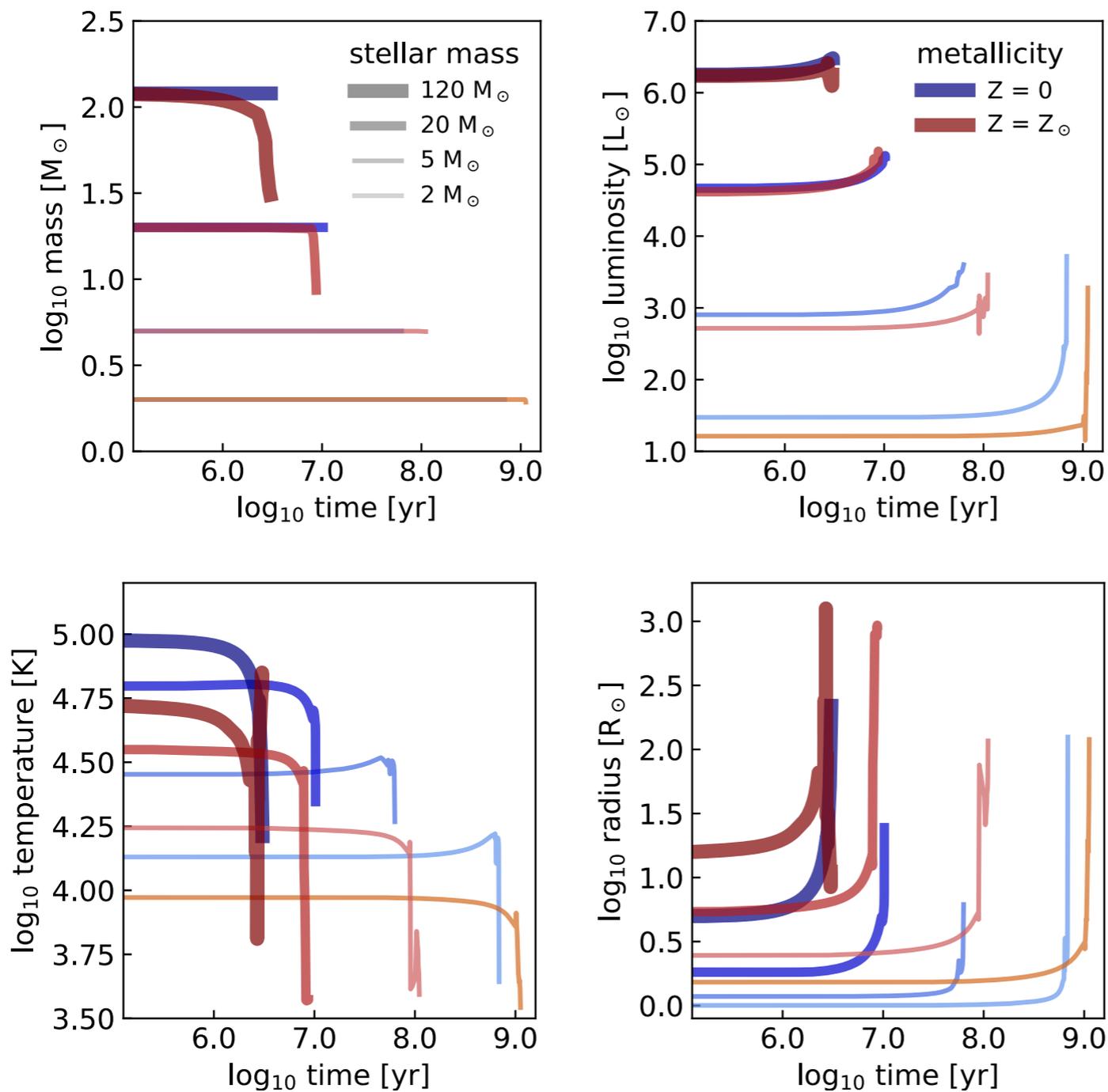
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some properties of Pop III stars

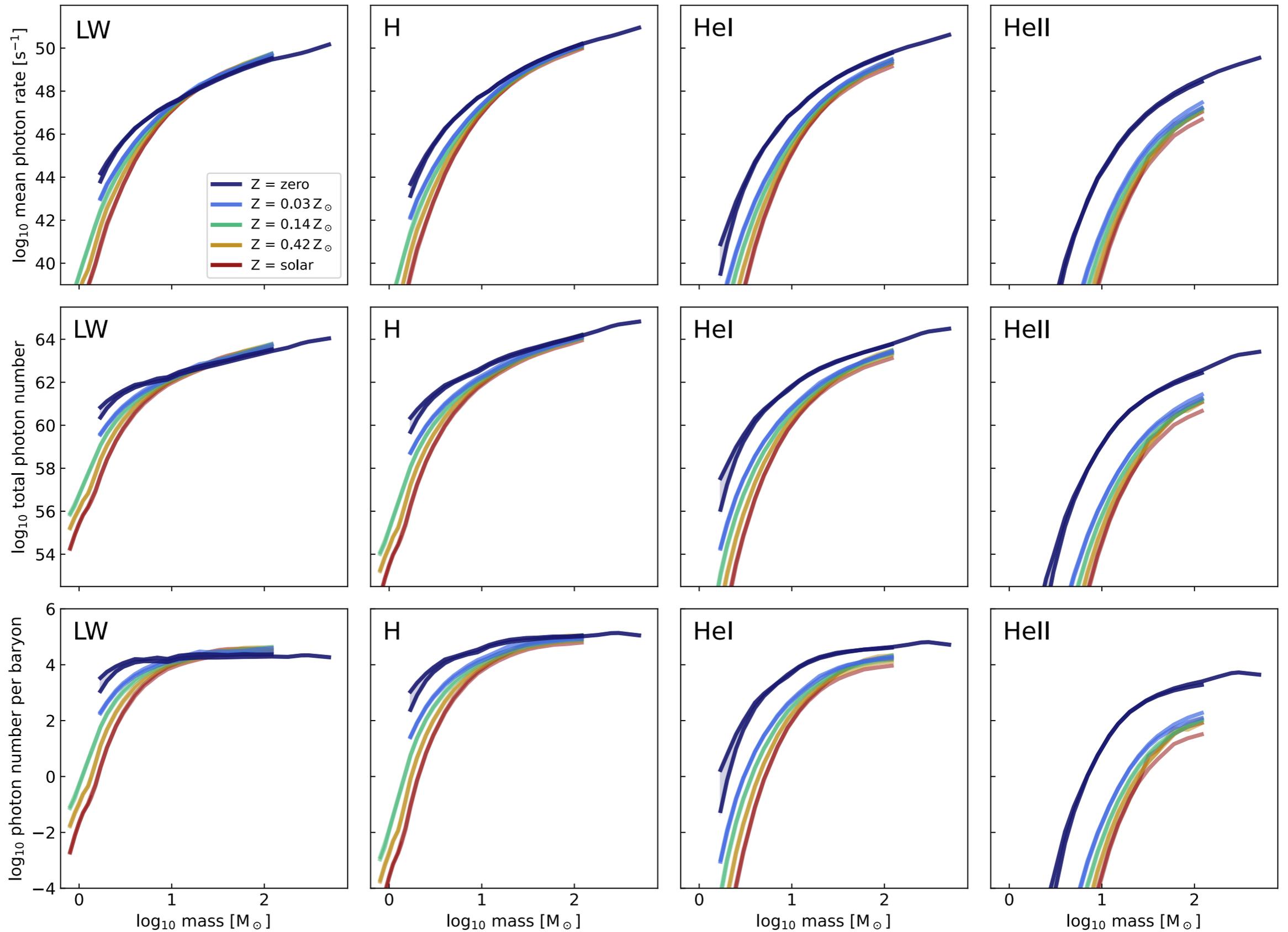


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Klessen, & Glover (2023, ARAA, 61,65 -- arXiv.2303.12500)
based on data by Murphy et al. (2021, MNRAS 501, 2745, 2021, MNRAS, 506, 5731) and Ekström et al. (2012, A&A, 537, A146)

Pop III stars



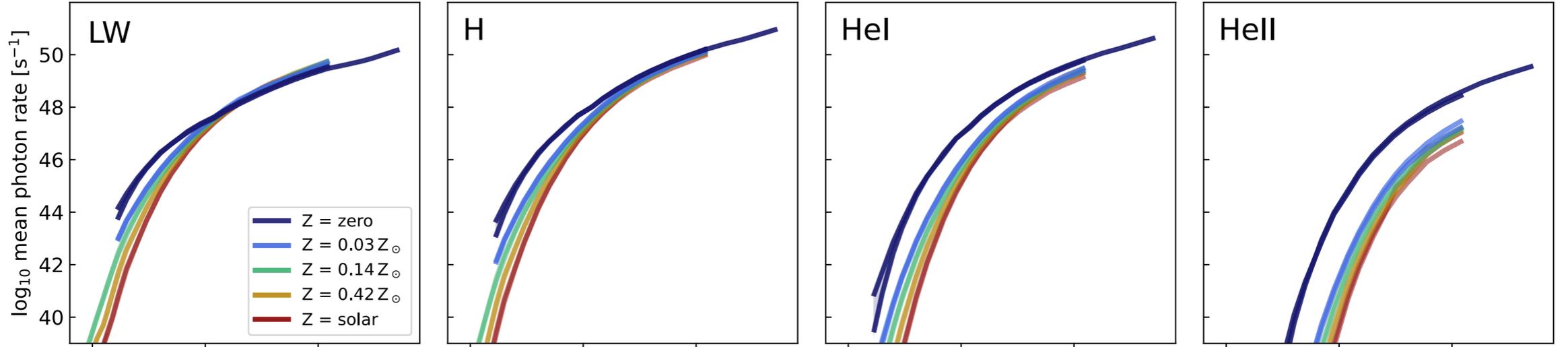


Table A1: Key stellar properties and production rates of ionizing and non-ionizing photons as function of stellar mass and metallicity

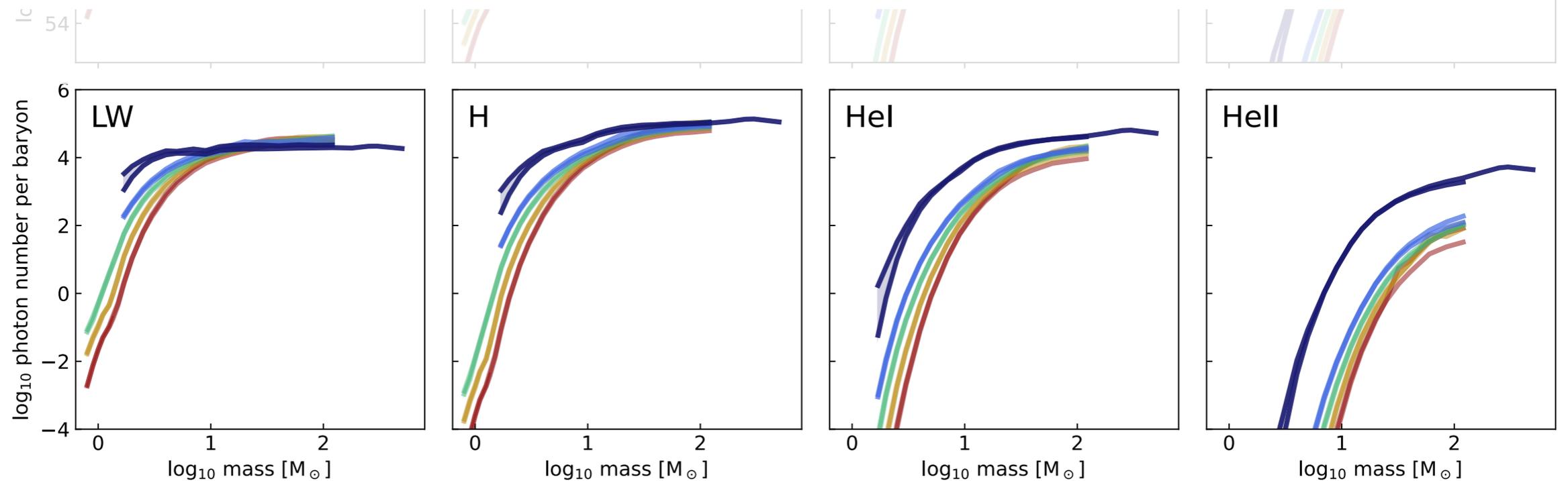
Z [Z_{\odot}]	rot [v_{\max}]	M [M_{\odot}]	age [yr]	T_{*} [K]	L_{*} [L_{\odot}]	R_{*} [R_{\odot}]	Q_{tot} [s^{-1}]	Q_{LW} [s^{-1}]	Q_{H} [s^{-1}]	Q_{HeI} [s^{-1}]	Q_{HeII} [s^{-1}]	N_{tot} -	N_{LW} -	N_{H} -	N_{HeI} -	N_{HeII} -	N^b -	N_{LW}^b -	N_{H}^b -	N_{HeI}^b -	N_{HeII}^b -
0.0	0.0	1.7	9.06	4.10	1.48	1.16	46.51	43.80	43.13	39.51	29.26	63.07	60.36	59.69	56.07	45.82	5.76	3.06	2.39	0	0
0.0	0.0	2.0	8.84	4.17	1.76	1.18	46.70	44.46	43.95	40.90	32.19	63.04	60.80	60.28	57.24	48.53	5.66	3.42	2.91	0	0
0.0	0.0	2.5	8.54	4.25	2.13	1.20	46.96	45.19	44.86	42.43	35.37	63.00	61.23	60.90	58.47	51.41	5.53	3.76	3.43	1.0	0
0.0	0.0	3.0	8.33	4.32	2.41	1.23	47.17	45.65	45.46	43.40	37.36	62.99	61.48	61.28	59.23	53.19	5.44	3.93	3.73	1.68	0
0.0	0.0	4.0	8.02	4.42	2.84	1.29	47.49	46.24	46.22	44.61	39.78	63.00	61.76	61.73	60.13	55.29	5.33	4.08	4.06	2.45	0
0.0	0.0	5.0	7.80	4.48	3.15	1.34	47.71	46.60	46.69	45.35	41.21	63.01	61.90	61.99	60.65	56.51	5.24	4.13	4.22	2.87	0
0.0	0.0	7.0	7.50	4.58	3.59	1.45	48.04	47.05	47.29	46.25	42.94	63.04	62.04	62.29	61.25	57.94	5.12	4.12	4.37	3.33	0.02
0.0	0.0	9.0	7.30	4.64	3.90	1.58	48.29	47.33	47.67	46.80	43.98	63.09	62.13	62.47	61.60	58.78	5.06	4.10	4.44	3.57	0.75
0.0	0.0	12.0	7.29	4.69	4.24	1.84	48.53	47.58	48.01	47.27	44.83	63.31	62.37	62.80	62.06	59.62	5.16	4.21	4.65	3.90	1.46
0.0	0.0	15.0	7.15	4.73	4.48	2.03	48.79	47.84	48.34	47.68	45.49	63.43	62.49	62.98	62.32	60.14	5.18	4.23	4.73	4.07	1.89
0.0	0.0	20.0	7.01	4.77	4.81	2.43	49.08	48.12	48.68	48.10	46.18	63.59	62.63	63.19	62.61	60.69	5.21	4.26	4.82	4.24	2.32
0.0	0.0	30.0	6.82	4.82	5.23	3.22	49.46	48.49	49.12	48.61	46.95	63.78	62.81	63.44	62.93	61.27	5.23	4.26	4.88	4.38	2.72
0.0	0.0	40.0	6.72	4.84	5.50	3.96	49.71	48.73	49.39	48.92	47.39	63.92	62.94	63.60	63.14	61.60	5.25	4.26	4.93	4.46	2.93
0.0	0.0	60.0	6.61	4.86	5.85	5.26	50.03	49.03	49.72	49.29	47.90	64.13	63.13	63.82	63.40	62.01	5.28	4.28	4.97	4.54	3.15
0.0	0.0	85.0	6.53	4.87	6.10	6.77	50.29	49.26	49.97	49.56	48.26	64.32	63.29	64.00	63.59	62.30	5.31	4.28	4.99	4.59	3.29
0.0	0.0	120.0	6.48	4.88	6.34	8.55	50.51	49.47	50.19	49.80	48.57	64.50	63.45	64.17	63.79	62.55	5.34	4.29	5.02	4.63	3.40
0.0	0.0	180.0	6.49	4.92	6.57	9.44	50.66	49.62	50.41	50.06	48.91	64.65	63.61	64.40	64.05	62.90	5.32	4.28	5.07	4.72	3.57
0.0	0.0	250.0	6.54	4.92	6.76	11.37	50.83	49.76	50.56	50.23	49.13	64.87	63.81	64.60	64.27	63.17	5.40	4.33	5.13	4.80	3.70
0.0	0.0	300.0	6.53	4.92	6.86	13.06	50.95	49.86	50.66	50.33	49.24	64.98	63.89	64.69	64.36	63.28	5.43	4.34	5.14	4.81	3.72
0.0	0.0	500.0	6.38	4.90	7.14	19.61	51.29	50.17	50.95	50.62	49.54	65.17	64.04	64.82	64.49	63.42	5.39	4.27	5.05	4.72	3.64

General comment: Note that the part of the table depicted here only covers models of non-rotating zero-metallicity Pop III stars. The complete table is available electronically in space-separated ASCII format from ARAA or from the authors at heibox.uni-heidelberg.de/f/6b5b3fcbd3974fb98d50/. It can be easily read, for example, using the `astropy.io.ascii.read` command.

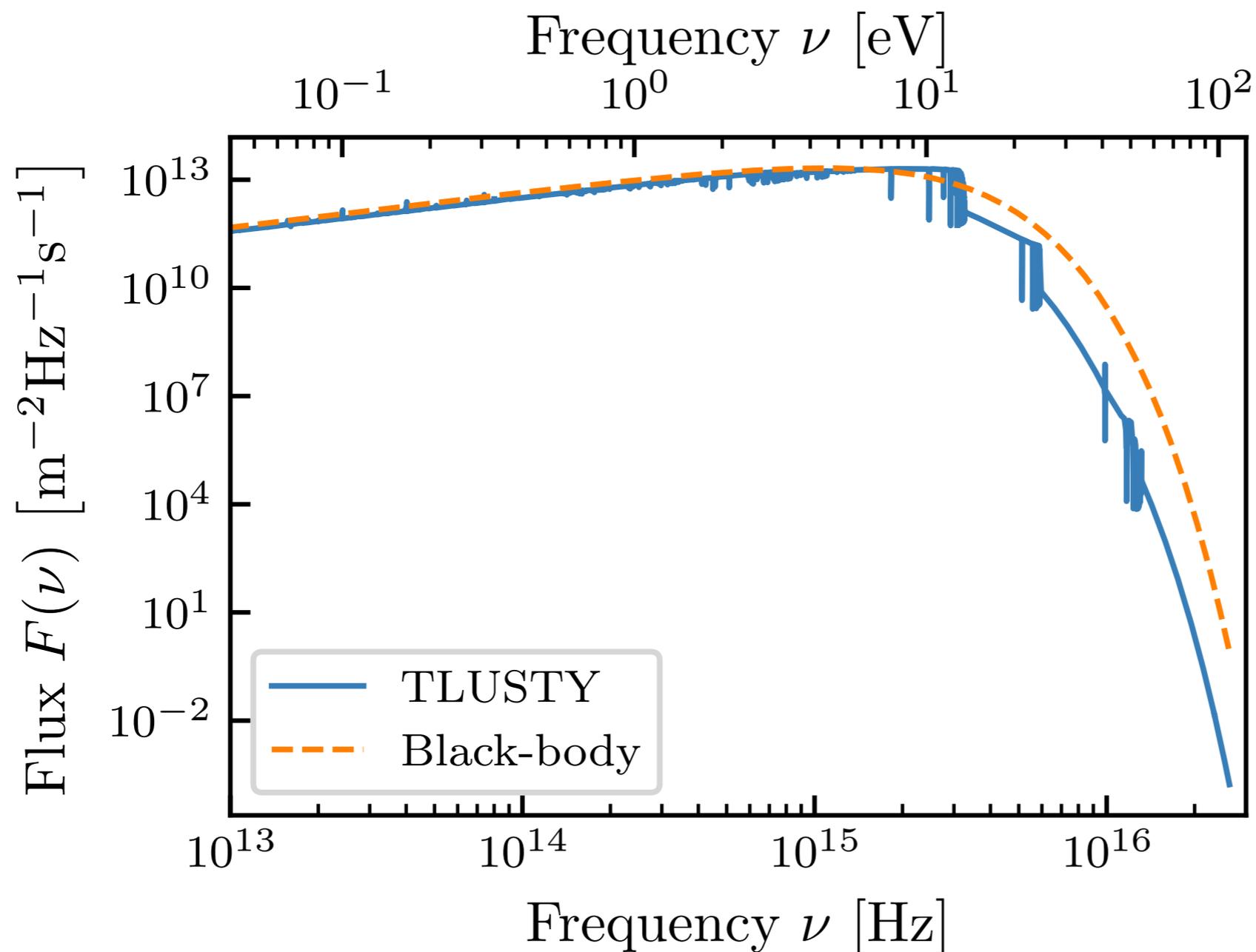
Table A2: Population averaged number of photons per baryon (in log units)

population	IMF	$\langle N^b \rangle$	$\langle N_{\text{LW}}^b \rangle$	$\langle N_{\text{H}}^b \rangle$	$\langle N_{\text{HeI}}^b \rangle$	$\langle N_{\text{HeII}}^b \rangle$
Pop III	log-flat	5.31	4.11	4.72	4.29	3.05
Pop I	Kroupa	6.11	2.67	2.69	1.50	0

Column description: population = metal-free Pop III or solar-metallicity Pop I stars ■ IMF = stellar initial mass function, either logarithmically flat or (Kroupa 2002) multi-component power-law model ■ $\langle N^b \rangle$ = decadic logarithm of the population averaged total number of photons emitted per stellar baryon ■ $\langle N_{\text{LW}}^b \rangle$ = decadic logarithm of the population averaged number of LW photons emitted per stellar baryon ■ $\langle N_{\text{H}}^b \rangle$ = decadic logarithm of the population averaged number of H ionizing photons emitted per stellar baryon ■ $\langle N_{\text{HeI}}^b \rangle$ = decadic logarithm of the population averaged number of He ionizing photons emitted per stellar baryon ■ $\langle N_{\text{HeII}}^b \rangle$ = decadic logarithm of the population averaged number of He⁺ ionizing photons emitted per stellar baryon



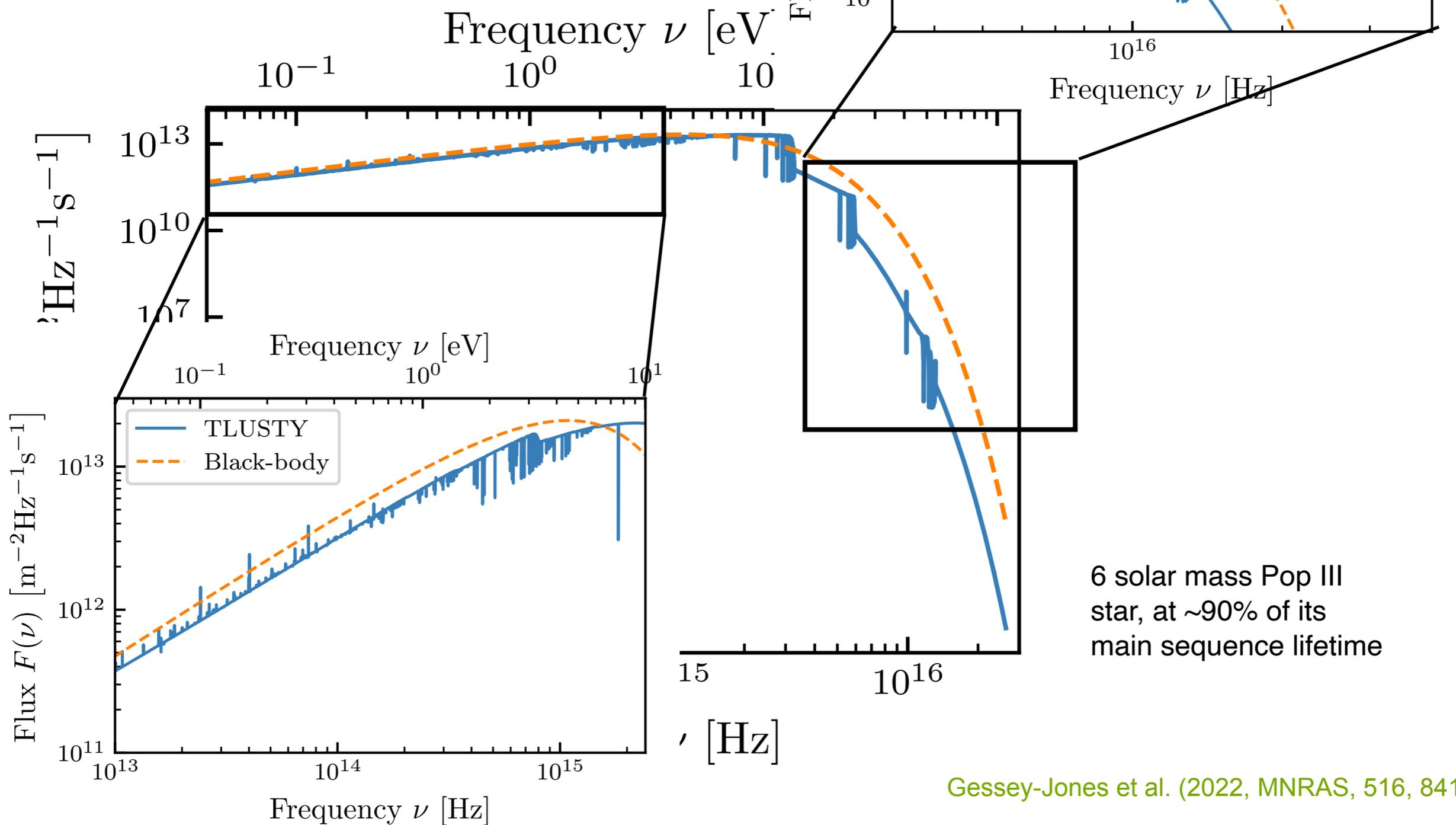
BUT: note that the spectra are more complex than simply blackbodies, and so this consideration may be wrong by a factor of a few



6 solar mass Pop III
star, at ~90% of its
main sequence lifetime

Pop III stars

BUT: note that the spectra are more complex than simply blackbodies, and so this consideration may be wrong by a factor of a few





Pop II stars



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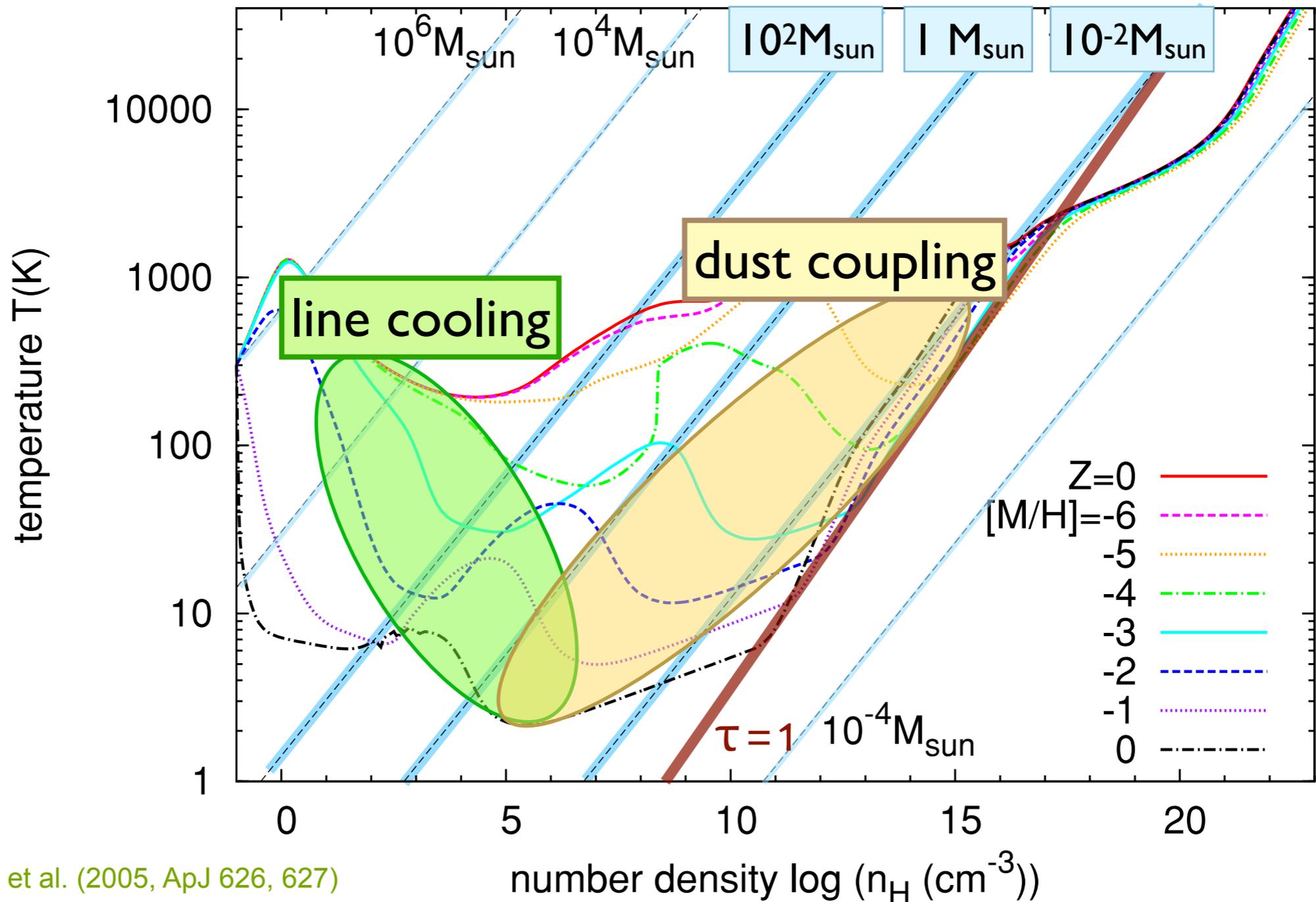


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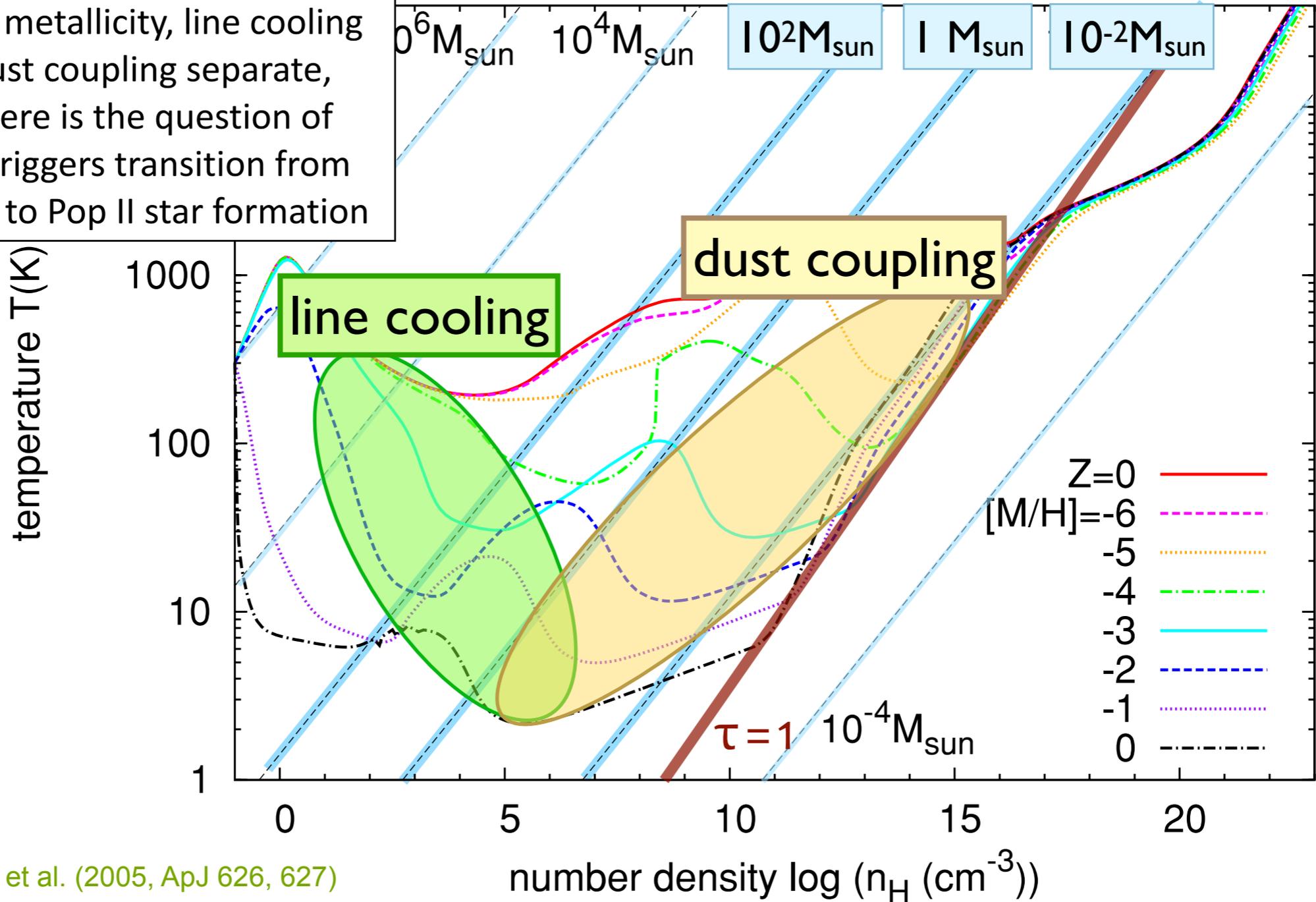
transition from Pop III to Pop II star formation



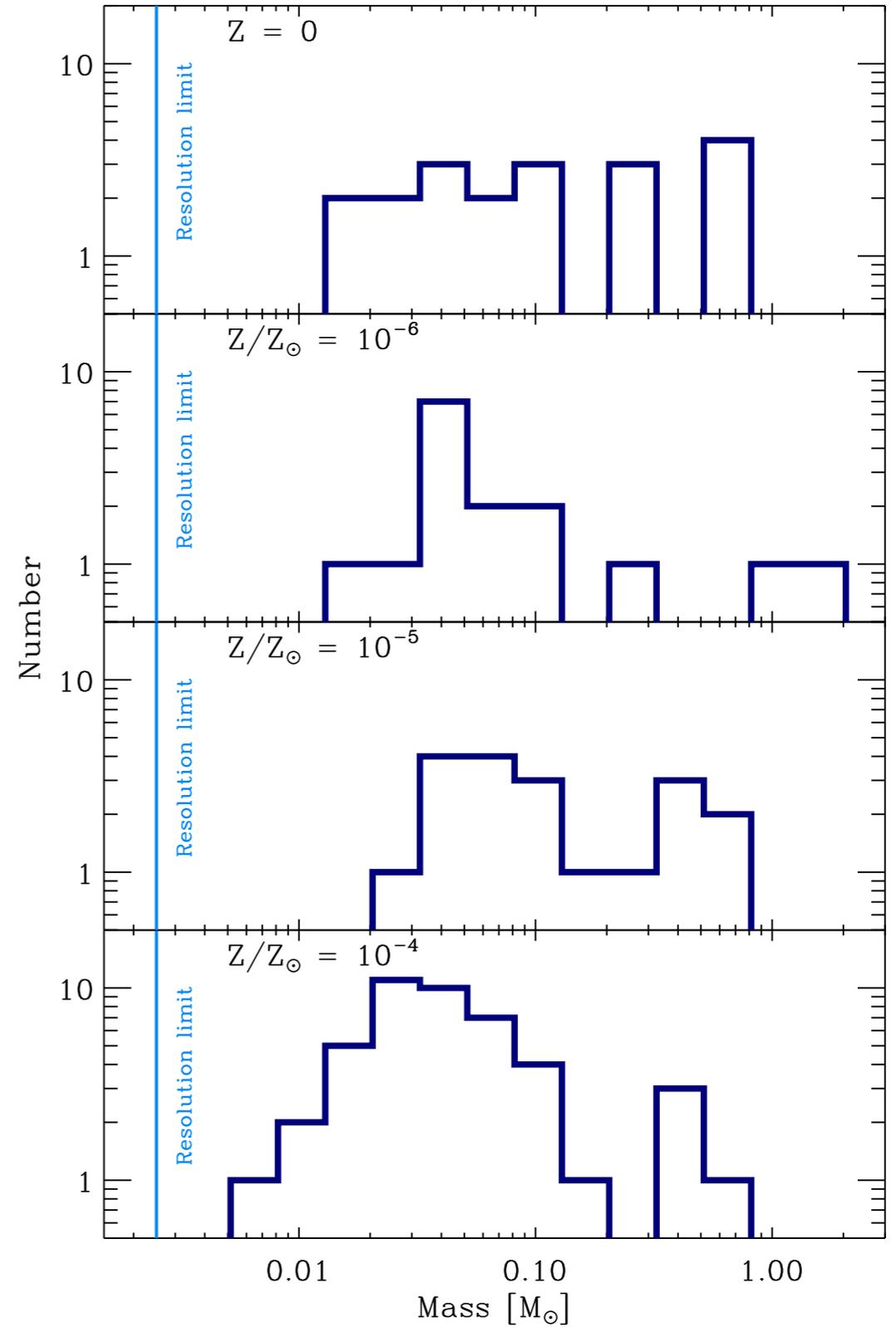
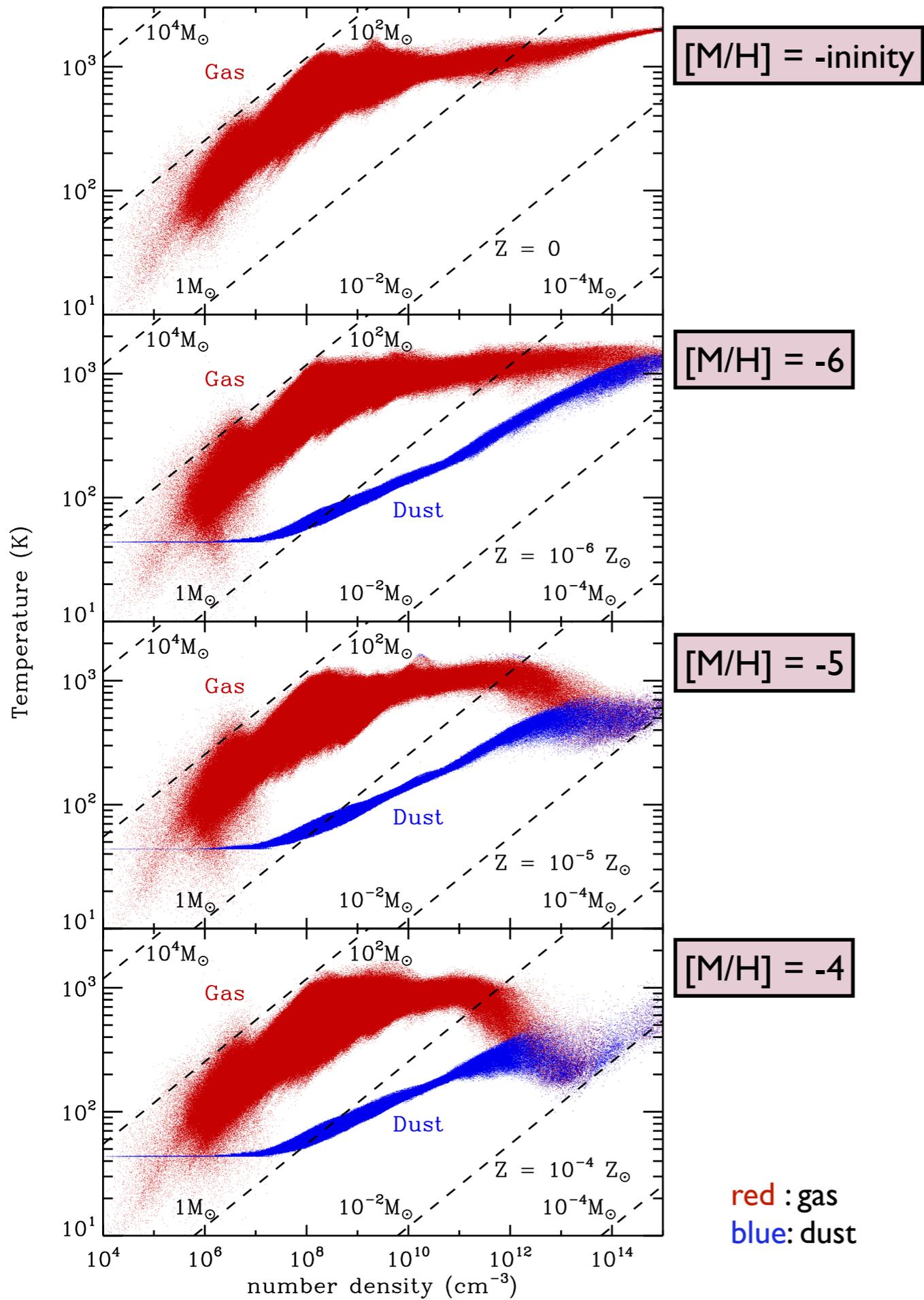
transition from Pop III to Pop II star formation



at low metallicity, line cooling and dust coupling separate, and there is the question of what triggers transition from Pop III to Pop II star formation



Omukai et al. (2005, ApJ 626, 627)



transition from Pop III to Pop II star formation

hints for changes in the mass spectrum in the metallicity range $10^{-4} - 10^{-5} Z_{\text{sun}}$

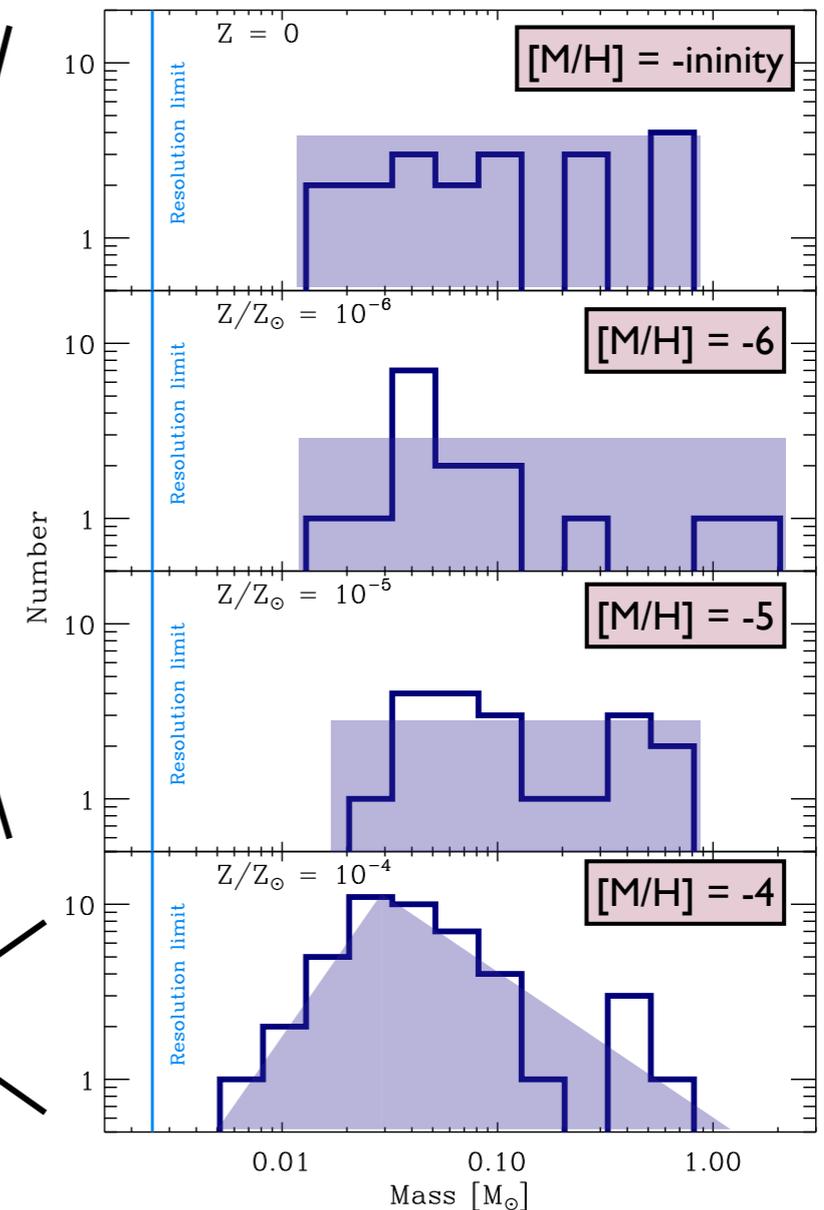
driven by dust coupling

disk fragmentation mode

gravoturbulent fragmentation mode



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Caffau et al. (2011, Nature 477, 67), Schneider et al. (2006, MNRAS 369, 825), Schneider et al. (2012, MNRAS, 423, L60), Chiaki et al (2013, ApJ, 762, 50), Chiaki et al (2016, MNRAS, 463, 2781), Chon et al. (2021, MNRAS, 508, 4175)

Dopcke et al. (2013, ApJ, 776, 103)

transition from Pop III to Pop II star formation



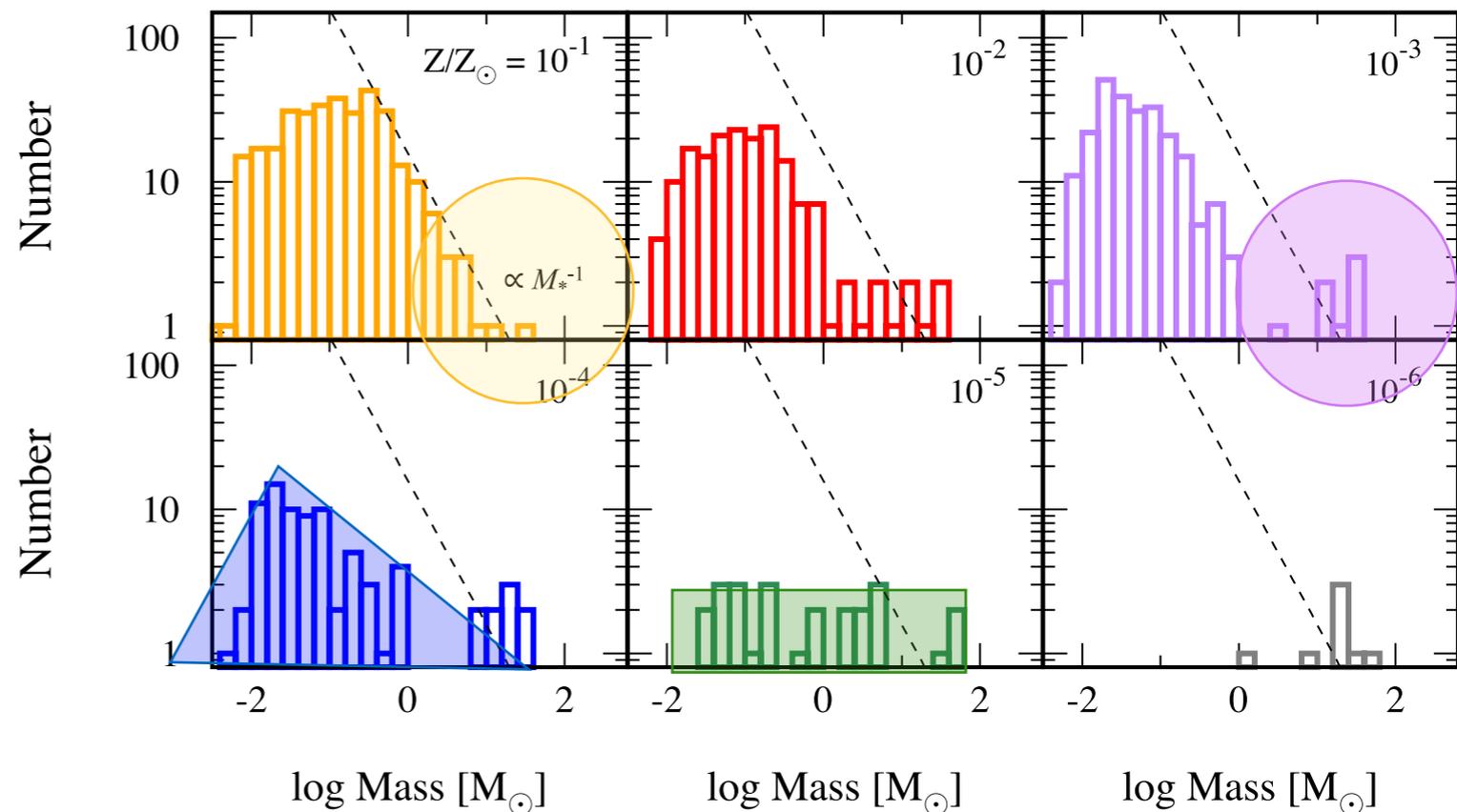
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hints for changes in the mass spectrum in the metallicity range $10^{-4} - 10^{-5} Z_{\text{sun}}$

driven by dust coupling

BUT: depending on features you look at you may place transition to different Z

also stellar dynamical aspects and run-away collisions are important



Caffau et al. (2011, Nature 477, 67), Schneider et al. (2006, MNRAS 369, 825), Schneider et al. (2012, MNRAS, 423, L60), Chiaki et al (2013, ApJ, 762, 50), Dopcke et al., 2013, ApJ, 776, 103), Chiaki et al (2016, MNRAS, 463, 2781)

Chon et al. (2021, MNRAS, 508, 4175)

transition from Pop III to Pop II star formation

hints for changes in the mass spectrum in
the metallicity range $10^{-4} - 10^{-5} Z_{\text{sun}}$

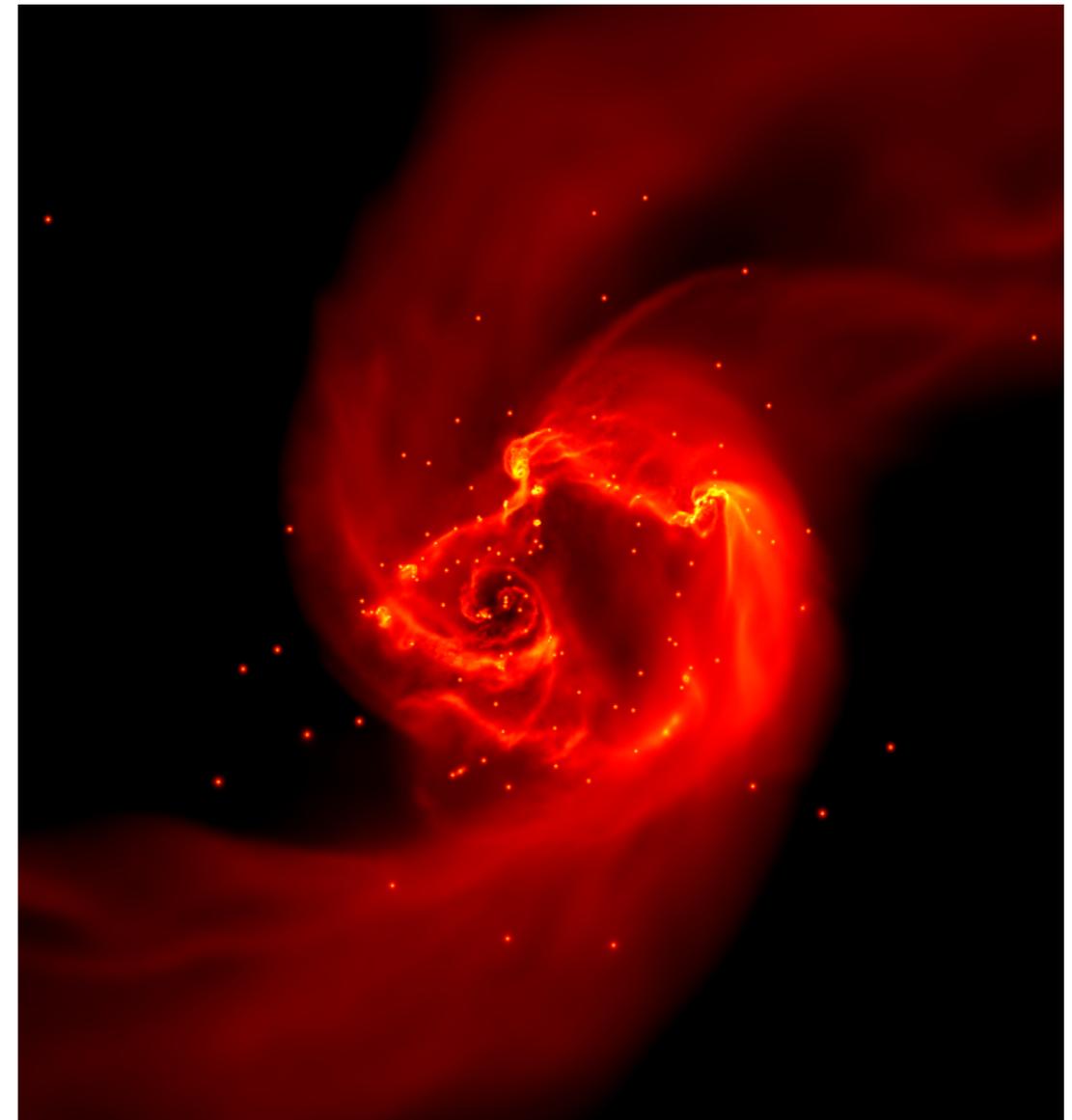
driven by dust coupling

also stellar dynamical aspects
and run-away collisions are
important

- mass spectrum
peaks *below* $1 M_{\text{sun}}$
- cluster VERY dense
 $n_{\text{stars}} = 2.5 \times 10^9 \text{ pc}^{-3}$
- fragmentation
at density
 $n_{\text{gas}} = 10^{12} - 10^{13} \text{ cm}^{-3}$



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supermassive stars



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critical halo mass for star formation



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criteria for collapse and star formation

- look at competition between gravity (density ρ) and gas pressure (sound speed c_s or temperature T): **Jeans mass**
- critical mass:

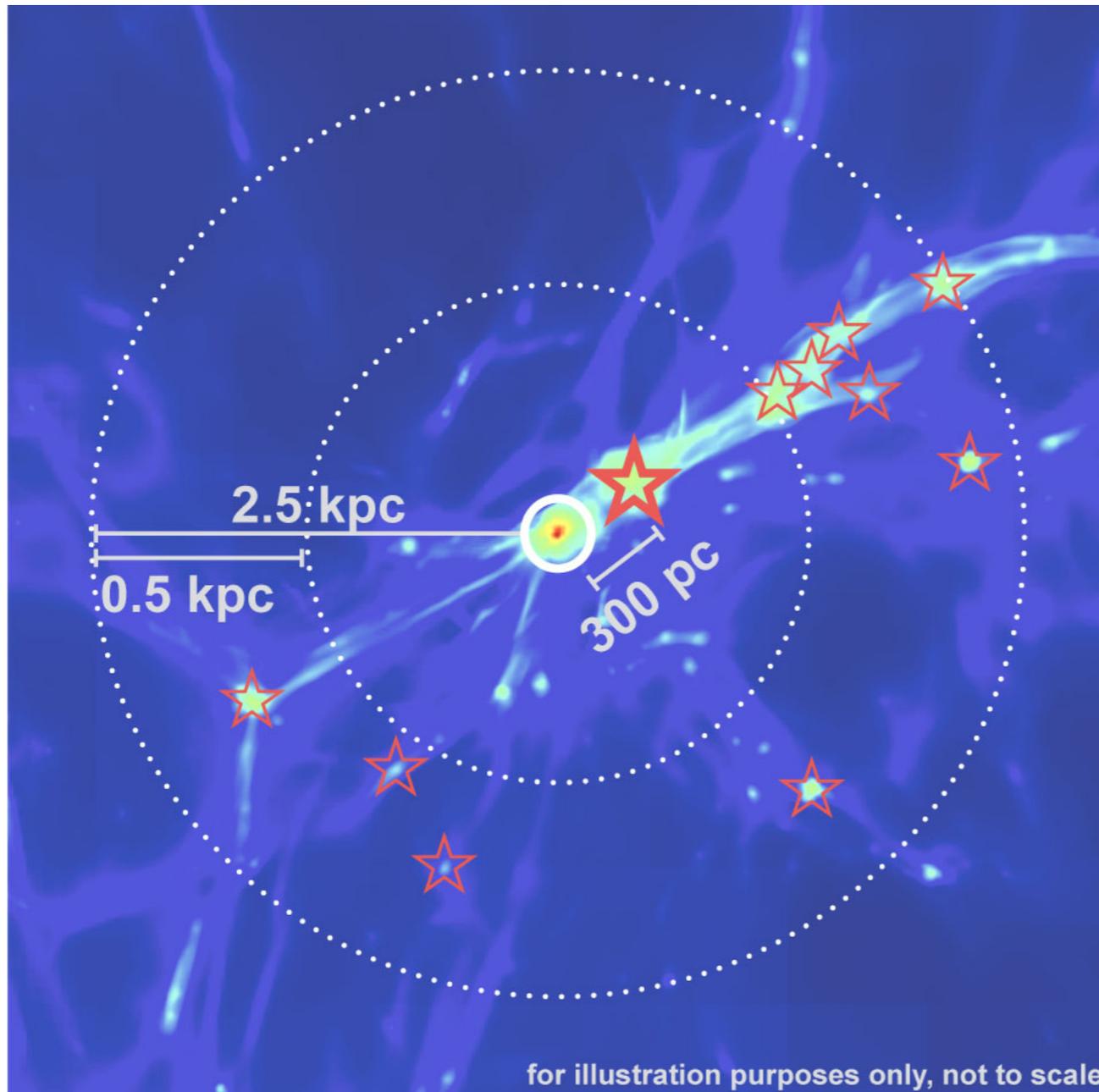
$$M_J = \frac{\pi^{5/2}}{6} \left(\frac{1}{G}\right)^{3/2} \rho^{-1/2} c_s^3 = \frac{\pi^{5/2}}{6} \left(\frac{k}{G}\right)^{3/2} \left(\frac{1}{\mu m_H}\right)^2 n^{-1/2} T^{3/2}$$

- M_J goes up if $T \nearrow$ or $\rho \searrow$
—> **larger mass reservoir available in atomic cooling halos (as needed for SMS)**
- note: can be extended by considering effective sound speed
 $c_{s,\text{eff}}^2 = c_s^2 + \sigma^2$ with $\sigma = \sigma_{\text{turb}}$ or $\sigma = v_{\text{Alfven}}$
—> **higher masses favored in magnetized halos and in presence of high streaming velocity**

atomic cooling halos



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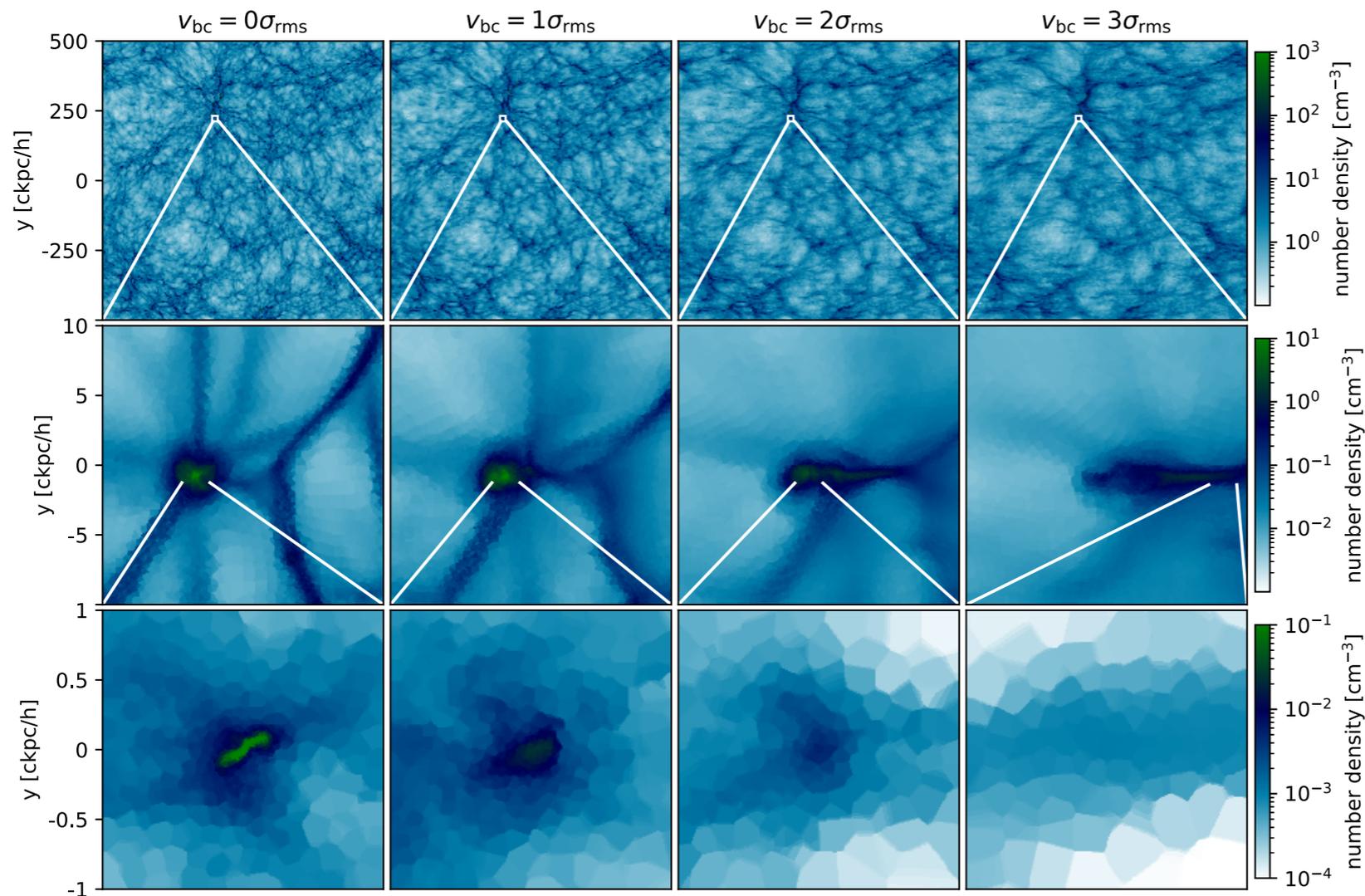
- halos come in groups
- some form Pop III stars earlier
- their LW/UV radiation prevents keeps neighboring halos in atomic phase → **not, no SF**
- need well tuned conditions: “goldilock” scenario
- these sit there and accumulate mass until they collapse in atomic phase → **SF**
- talks by John Regan, John Wise, Lewis Prole

impact of streaming velocity and LW background



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- streaming velocity and LW background can be included in early galaxy formation simulations



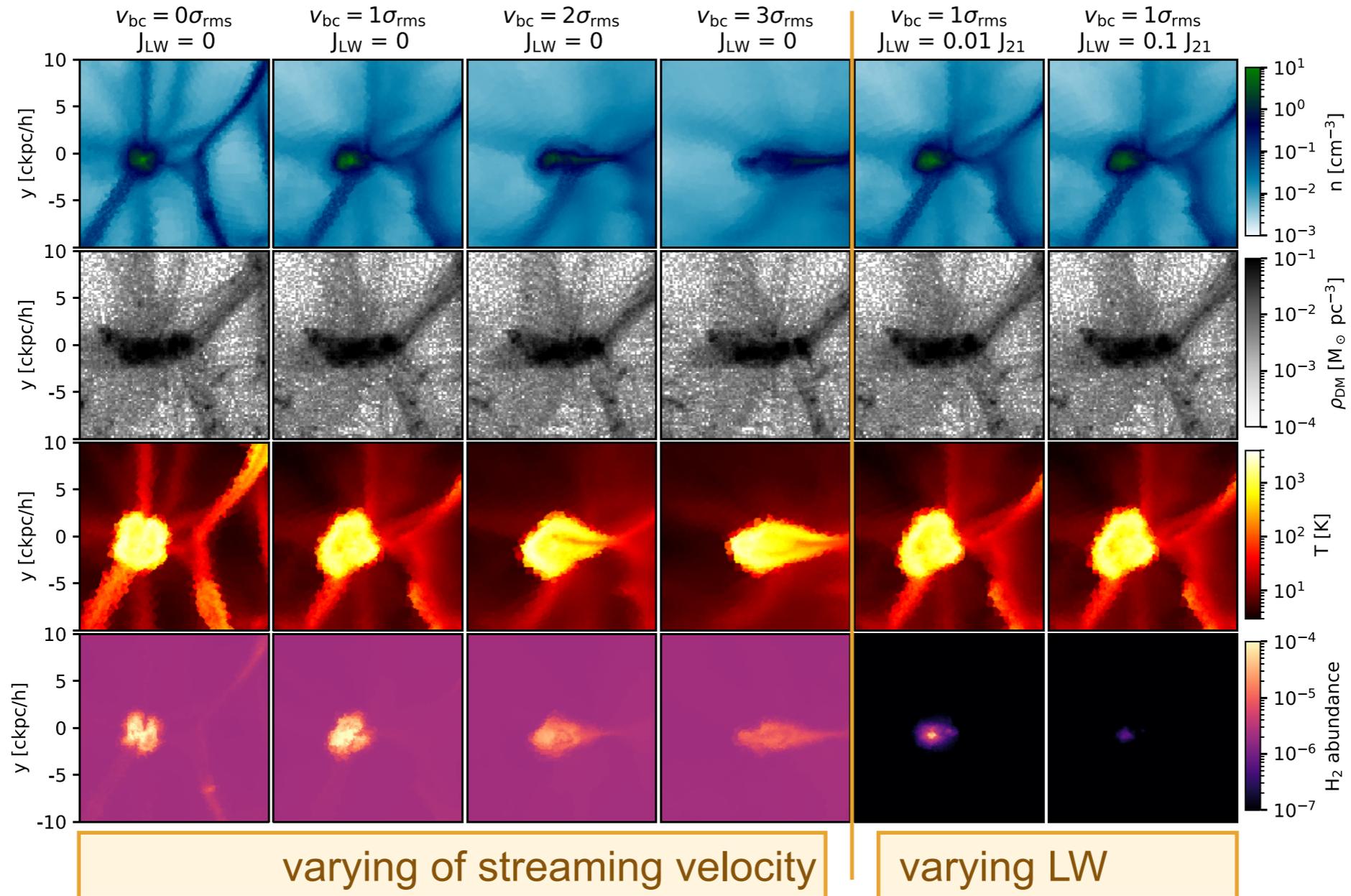
changing strength of streaming velocity

Schauer et al. (2021, MNRAS, 507, 1775)

impact of streaming velocity and LW background



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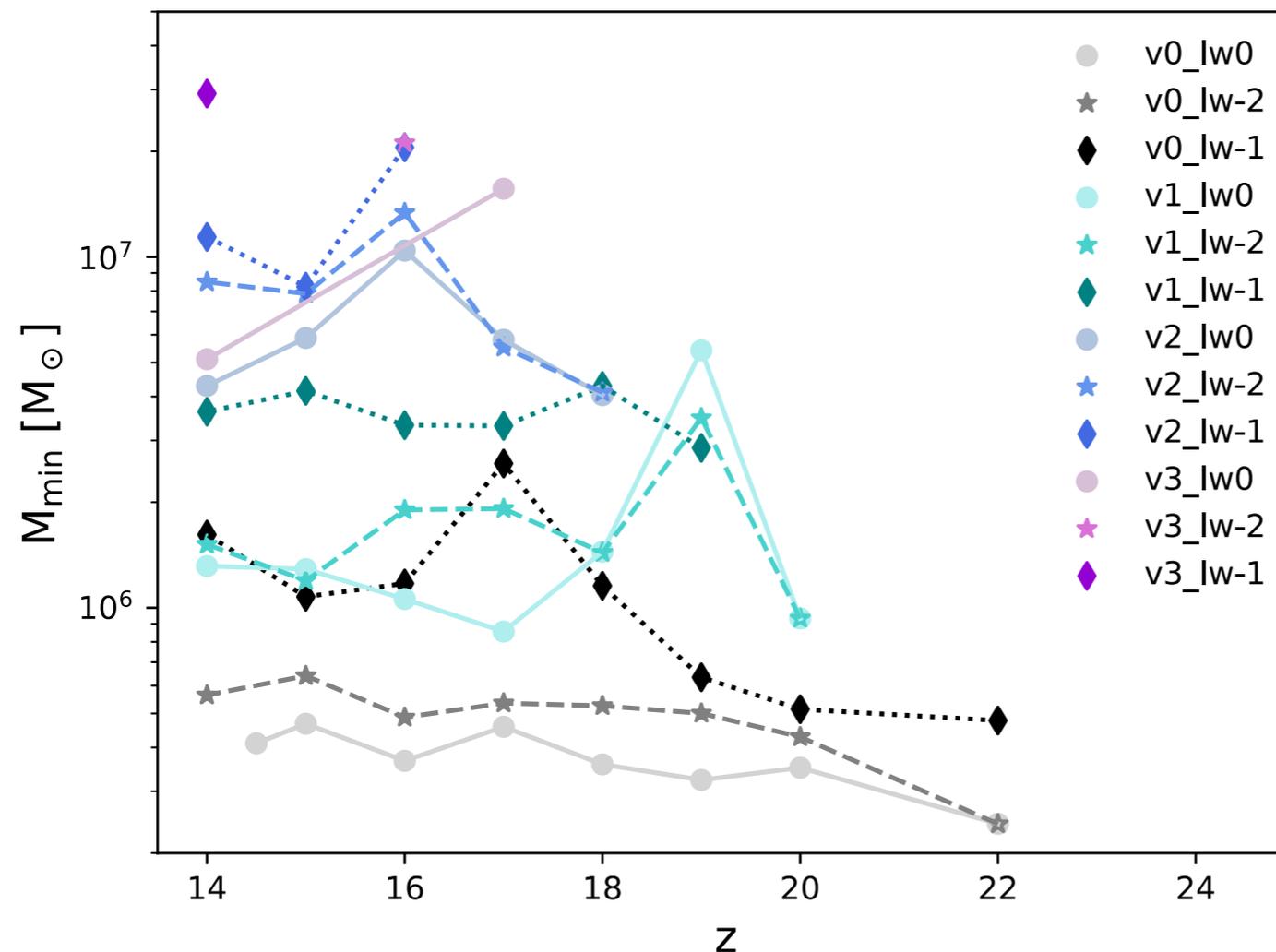


impact of streaming velocity and LW background



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- streaming velocity and LW background change critical mass for collapse



↑ more streaming
higher M_{crit}

↑ more LW
higher M_{crit}

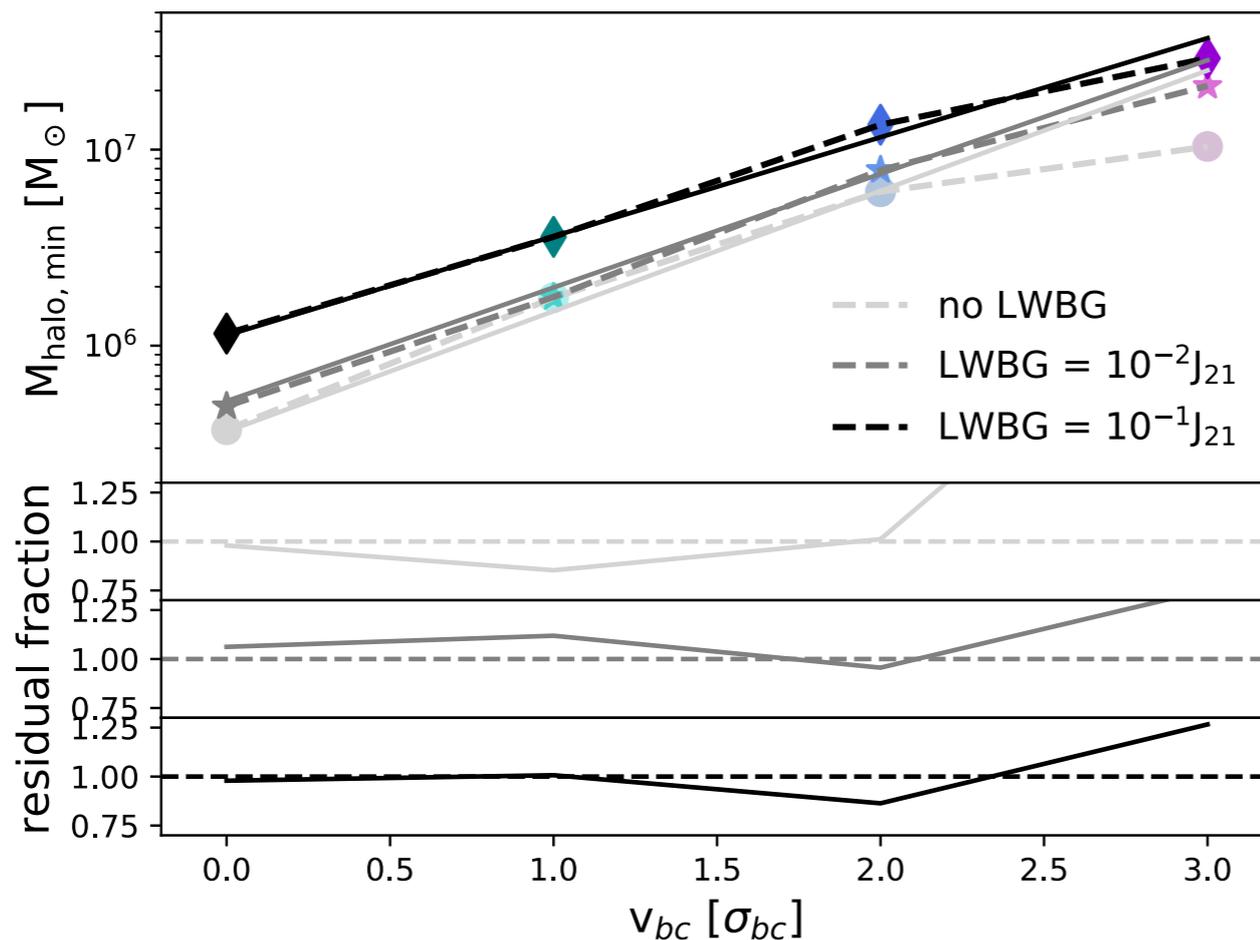
minimum halo mass of
star-forming halos at a
given redshift depends
on streaming and LW

impact of streaming velocity and LW background



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- analytic fit formula for M_{crit} as function of σ and J_{21}



this can be included as sub-grid estimate in numerical simulations or semi-analytic models

fit formula:

$$\log_{10} M_{\text{min}} = \log_{10} M_0 + s \times \frac{v_{bc}}{\sigma_{\text{rms}}},$$

with

$$\log_{10} M_0 = 5.562 \times \left(1 + 0.279 \times \sqrt{J_{21}}\right),$$

and

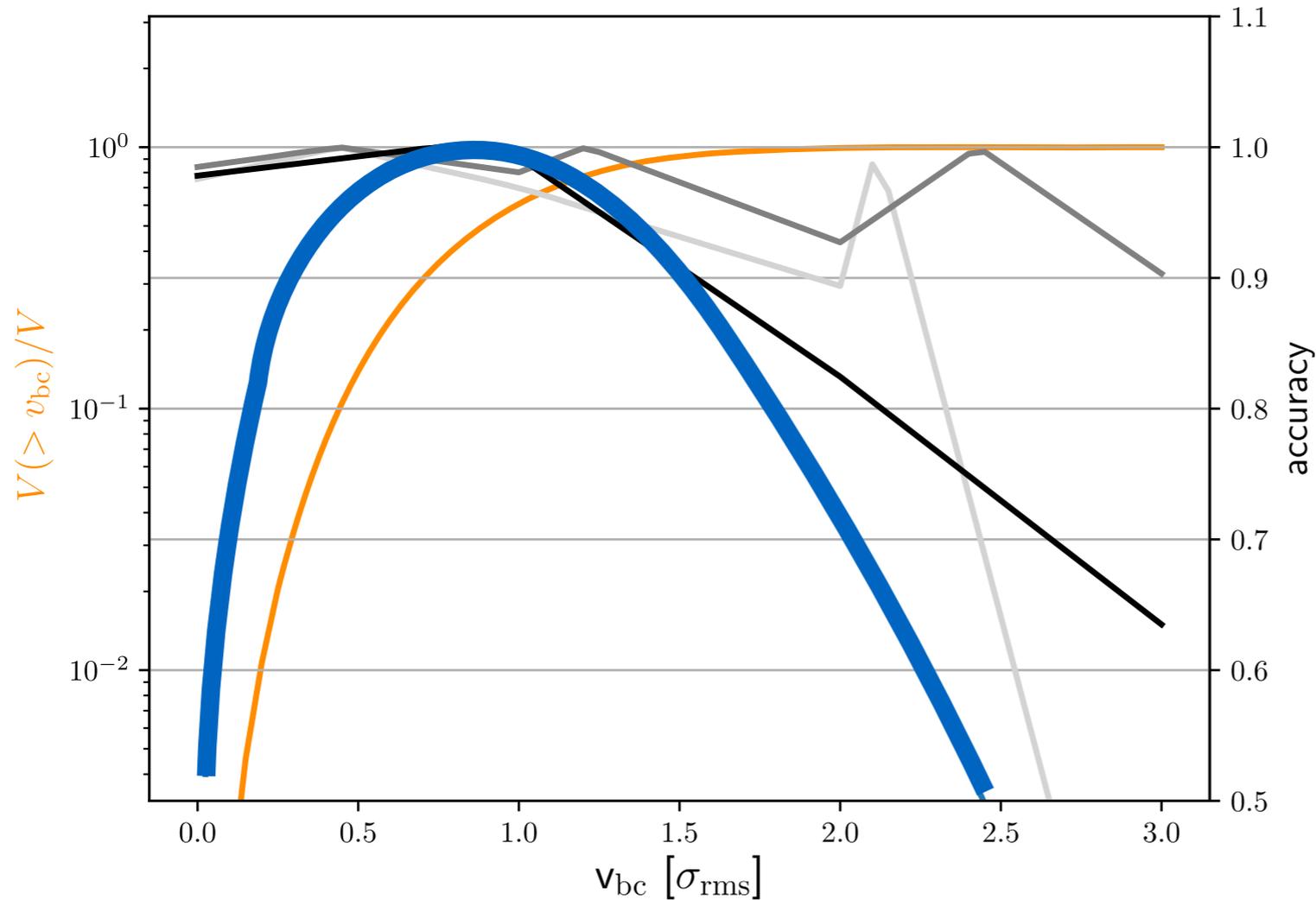
$$s = 0.614 \times \left(1 - 0.560 \times \sqrt{J_{21}}\right).$$

what is most likely streaming velocity?



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- distribution of streaming velocities



most likely streaming
velocity is $0.8 \sigma_{rms}$

blue: differential

orange: cumulative

atomic cooling halos —> fragmentation!



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- halos come in groups
- some form Pop III stars earlier
- their LW/UV radiation prevents keeps neighboring halos in atomic phase —> **not, no SF**
- these sit there and accumulate mass until they collapse in atomic phase —> **SF**
- BUT: now rapid H₂ formation, and lots of fragmentation —> **cluster of stars**
- again not good environment for direct collapse BH

atomic cooling halos —> fragmentation!



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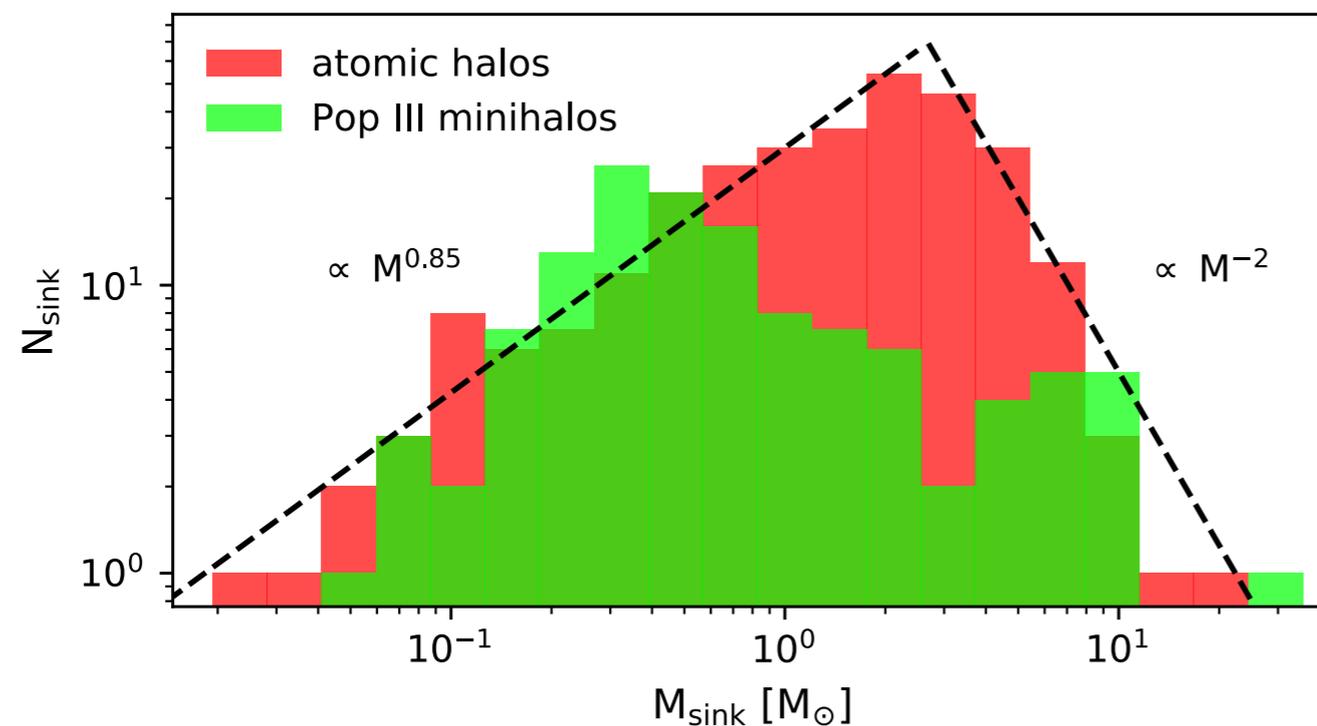


Fig. 9: Comparison of the sink particle mass function from the 3 atomic cooling halos at ~ 100 yr versus the 15 H_2 cooling minihalos from LP23 at ~ 300 yr. Power laws of $M^{0.85}$ and M^{-2} are superimposed to give the reader an idea of the slopes involved.

- halos come in groups
- some form Pop III stars earlier
- their LW/UV radiation prevents keeps neighboring halos in atomic phase —> **not, no SF**
- these sit there and accumulate mass until they collapse in atomic phase —> **SF**
- BUT: now rapid H_2 formation, and lots of fragmentation —> **cluster of stars**
- again not good environment for direct collapse BH

not just large mass reservoir, SMS also need dM/dt



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what is the resulting accretion rate?

- simple isothermal models give $\dot{M} = m_0 c_s^3 / G$ (see e.g. Shu 1977)
- **so again $\dot{M} \nearrow$ if $T \nearrow$**

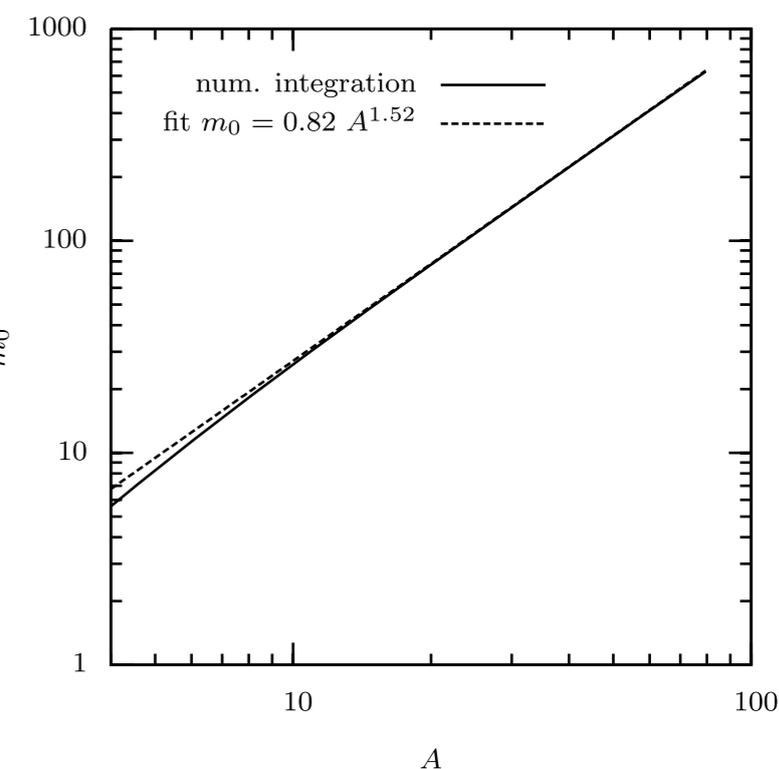
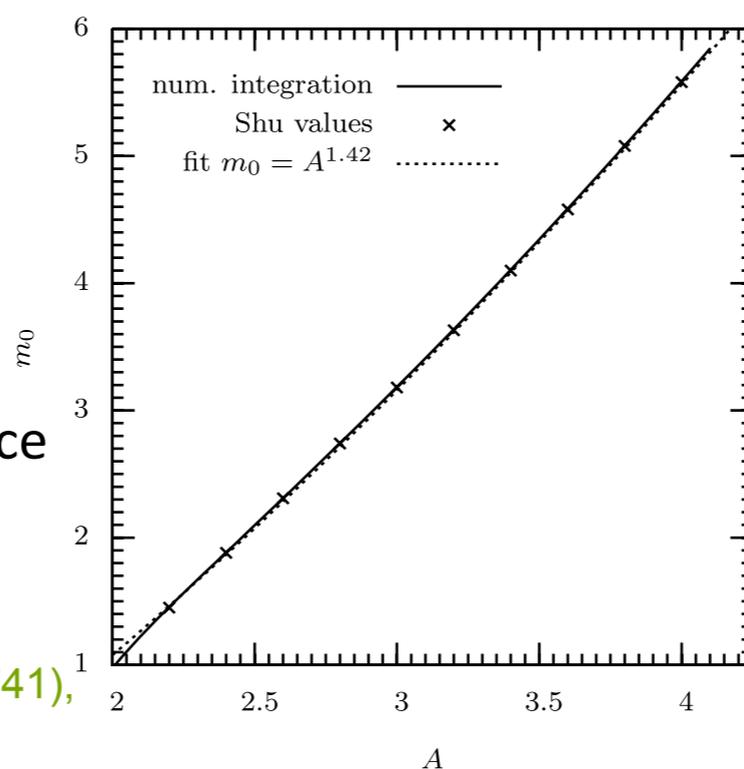
- BUT: recall there is also the *multiplication factor* $m_0 \propto A^{3/2}$ with $A \propto N_J^{2/3}$ so that $m_0 \propto N_J$ with N_J number of Jeans masses (Girichidis et al. 2011)

- **also: $\dot{M} \nearrow$ in collisions of two halos or two proto-galaxies**

(e.g. Mayer et al. 2010, Lorenz Zwick's talk)

- again high degree of turbulence will lead to **fragmentation**

Shu (1977, ApJ, 214, 488),
Girichidis et al. (2011, MNRAS, 413, 2741),
Mayer et al. (2010, Nature, 466, 108)



stellar evolution with different dM/dt



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How do stars evolve for different accretion rates?

- for $\dot{M} \geq 0.1 M_{\odot}/\text{yr}$ stars evolve with bloated radii
- see also Devesh Nandal's talk!

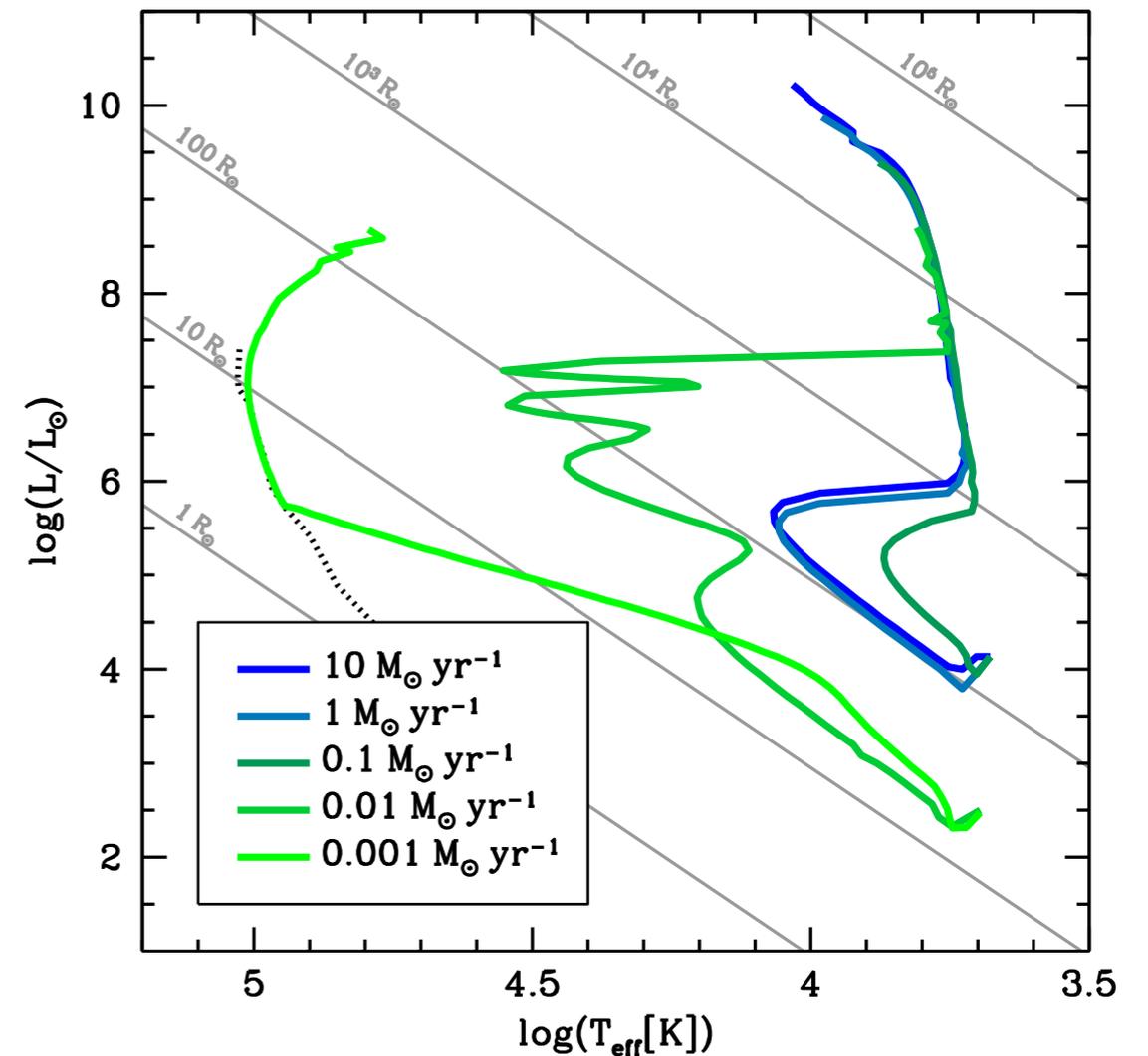


Figure 1. Evolutionary tracks on the HR diagram for the models at the indicated accretion rates. The grey straight lines indicate the stellar radius, and the black dotted curve is the ZAMS of Schaerer (2002).

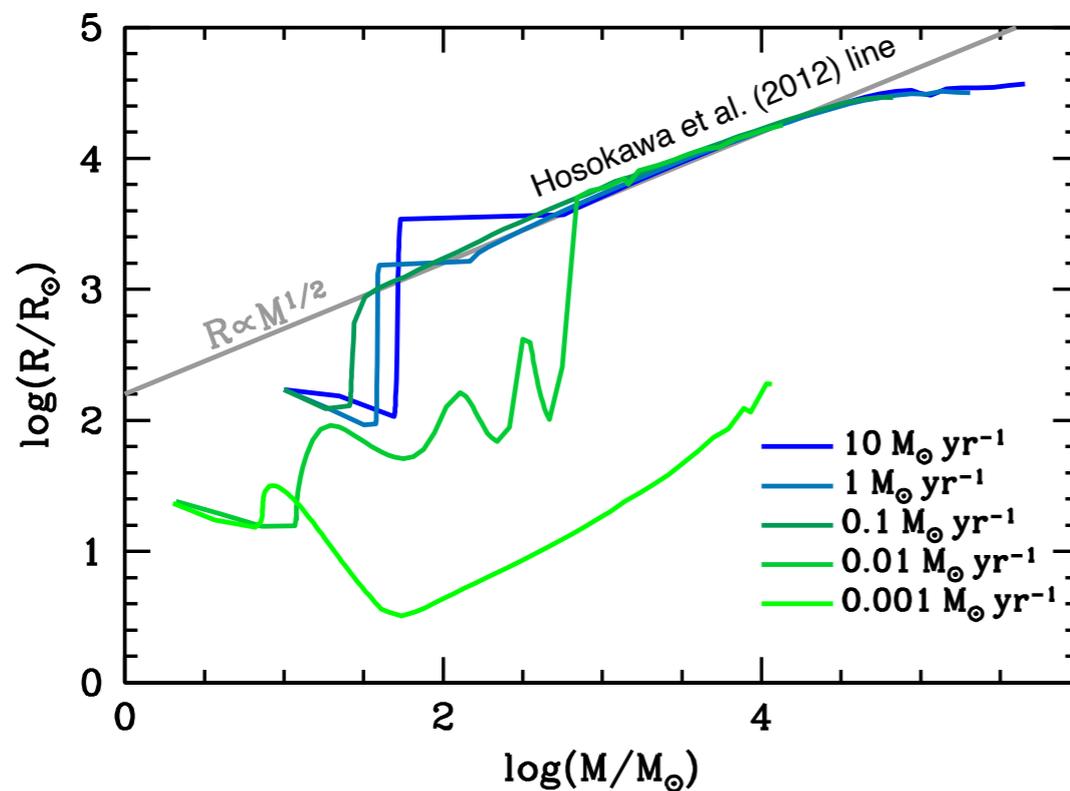
Haemmerlé et al. (2018, MNRAS 474, 2757)
see also Hosokawa et al. (2012, ApJ, 756, 93),

stellar evolution with different dM/dt



How do stars evolve for different accretion rates?

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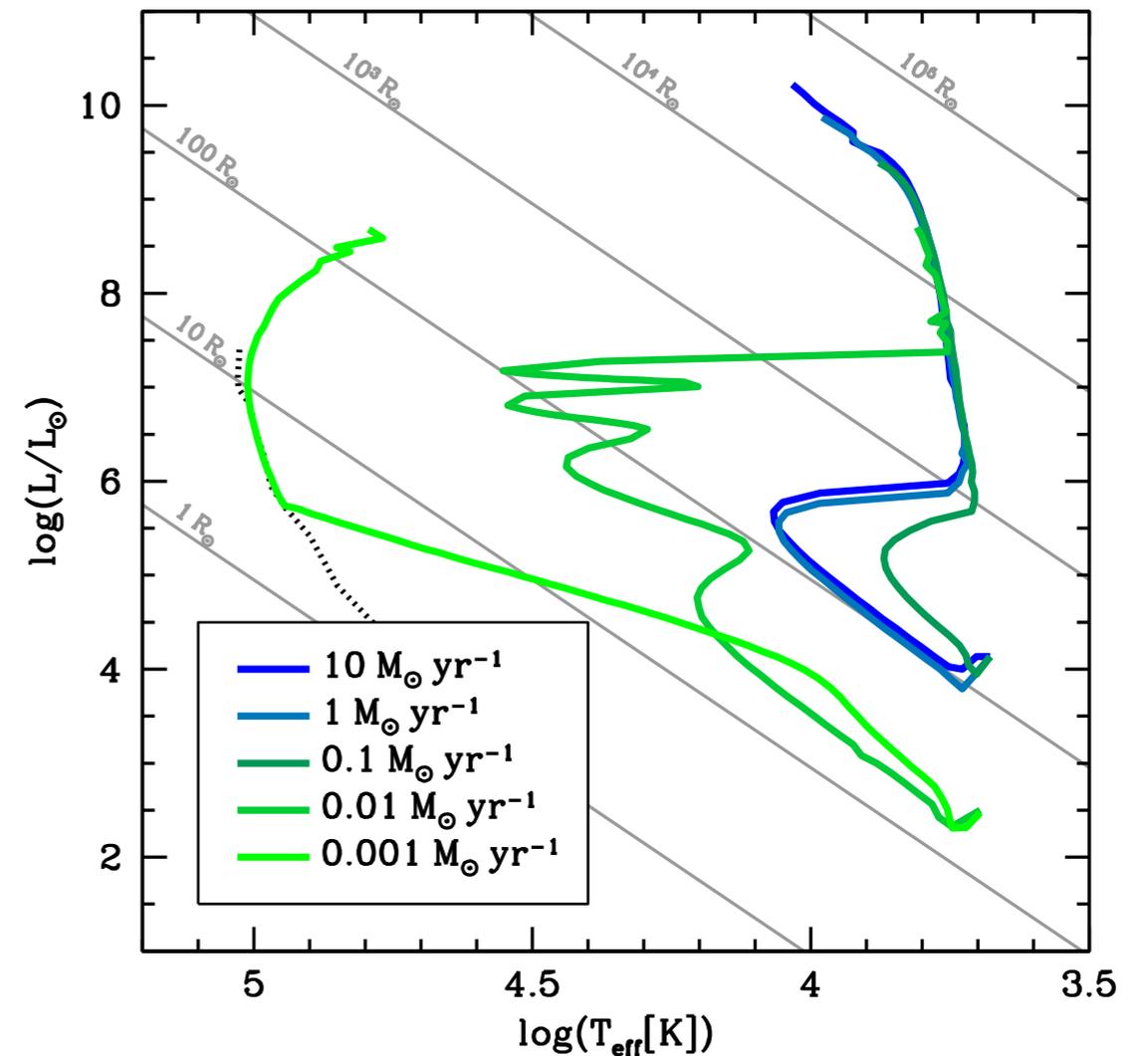
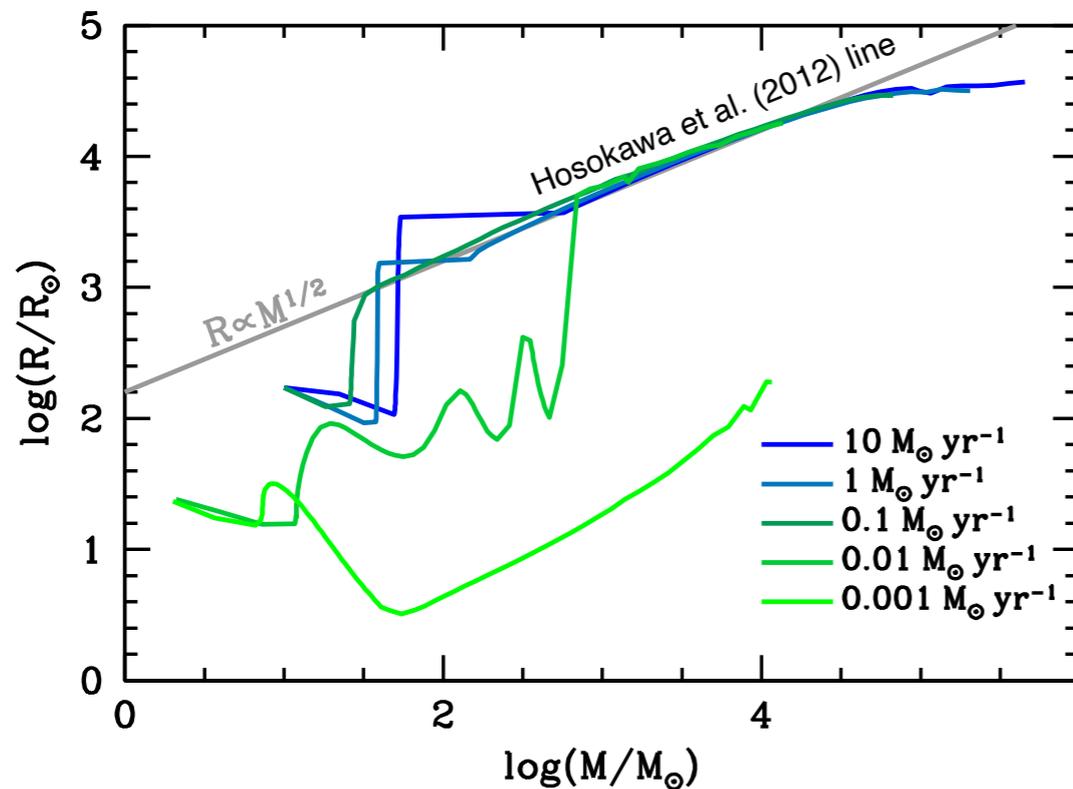


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stellar evolution with different dM/dt

How do stars evolve for different accretion rates?

- for $\dot{M} \geq 0.1 M_{\odot}/\text{yr}$ stars evolve with bloated radii
- different stellar structure for different \dot{M}



Haemmerlé et al. (2018, MNRAS 474, 2757)
 see also Hosokawa et al. (2012, ApJ, 756, 93),

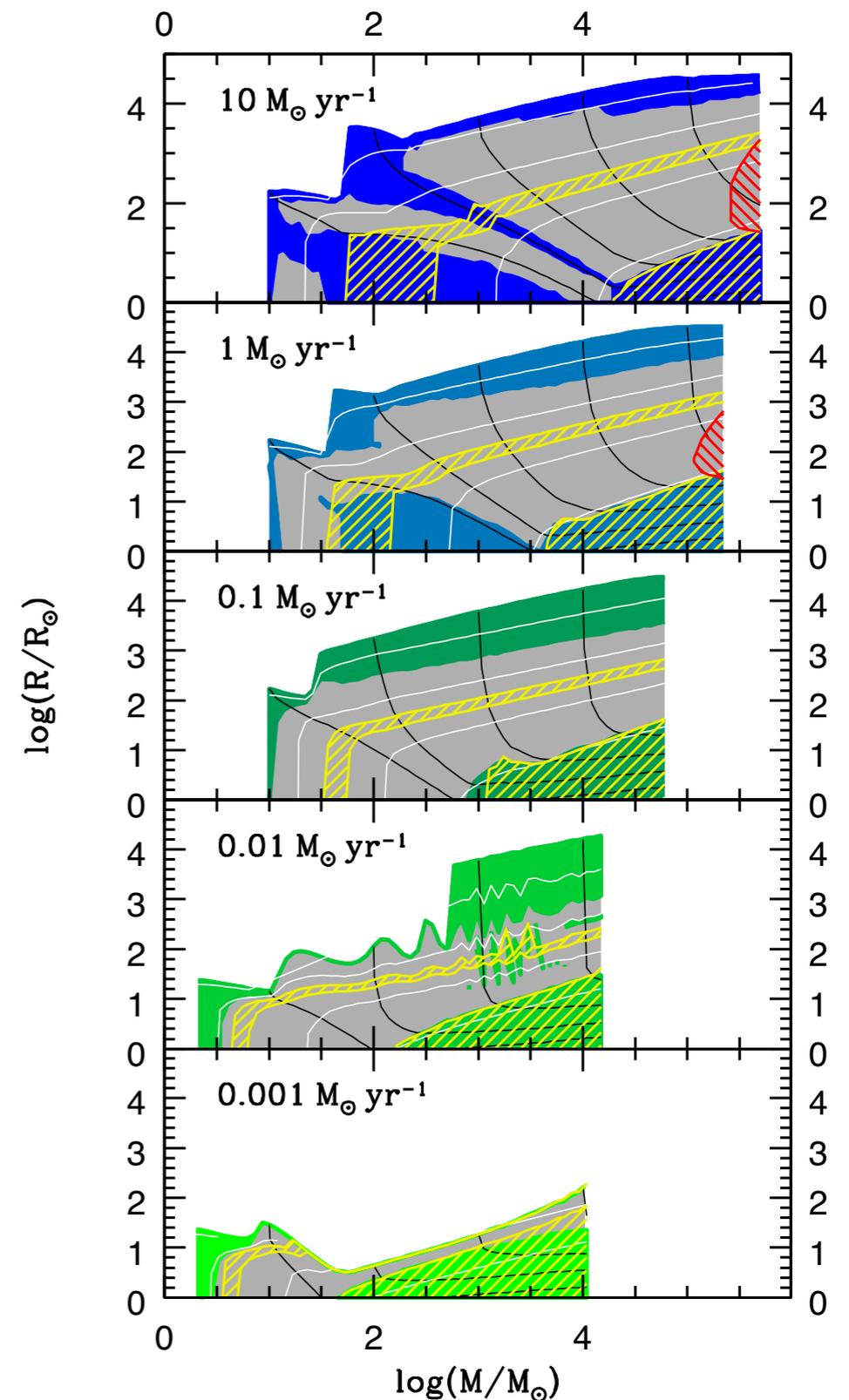


Figure 2. Internal structures of the models for the indicated accretion rates. In each panel, the upper curve is the stellar radius, the blue and green areas indicate convective zones, and the grey areas indicate radiative transport. The yellow hatched areas correspond to D- and H-burning, and the red hatched areas indicate the GR instability according to the polytropic criterion of equation (7) with $n = 3$. The black curves indicate the Lagrangian layers of $\log(M_r/M_{\odot}) = 1, 2, 3, 4$ and 5 , and the white ones are isotherms of $\log(T[\text{K}]) = 5, 6, 7$ and 8 .

stellar evolution with different dM/dt

How do stars evolve for different accretion rates?

- for $\dot{M} \geq 0.1 M_{\odot}/\text{yr}$ stars evolve with bloated radii
- different stellar structure for different \dot{M}
- for large \dot{M} stars evolve until GR instability sets in

pathway to supermassive stars!

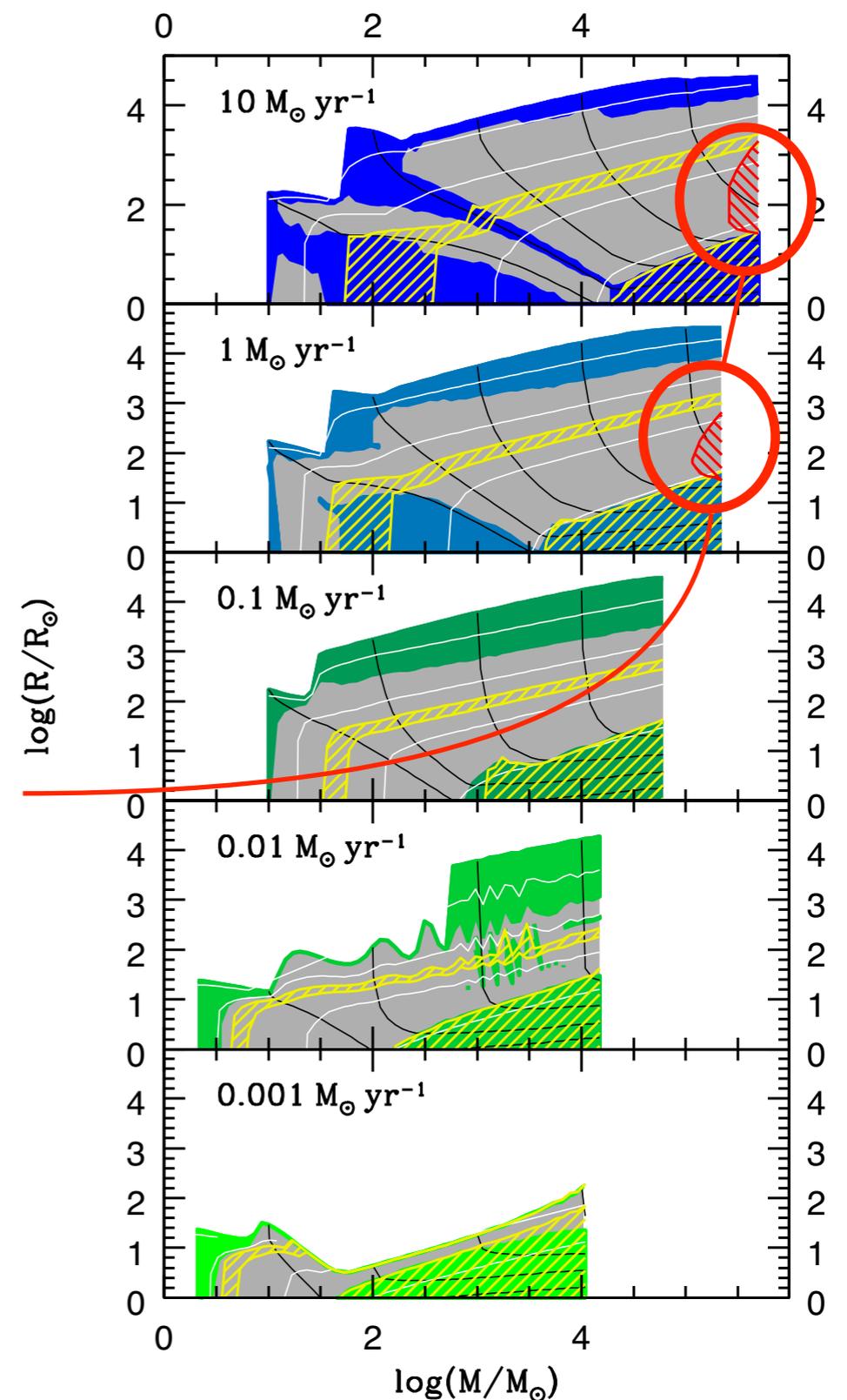


Figure 2. Internal structures of the models for the indicated accretion rates. In each panel, the upper curve is the stellar radius, the blue and green areas indicate convective zones, and the grey areas indicate radiative transport. The yellow hatched areas correspond to D- and H-burning, and the red hatched areas indicate the GR instability according to the polytropic criterion of equation (7) with $n = 3$. The black curves indicate the Lagrangian layers of $\log(M_r/M_{\odot}) = 1, 2, 3, 4$ and 5 , and the white ones are isotherms of $\log(T[\text{K}]) = 5, 6, 7$ and 8 .

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stellar evolution with different dM/dt



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How do stars evolve for different accretion rates?

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- different stellar structure for different \dot{M}
- for large \dot{M} stars evolve until GR instability sets in

pathway to supermassive stars!

- BUT: results *depend very strongly* on numerical details (example here: mass/resolution of outermost layer)

Haemmerlé et al. (2018, MNRAS 474, 2757)
see also Hosokawa et al. (2012, ApJ, 756, 93),

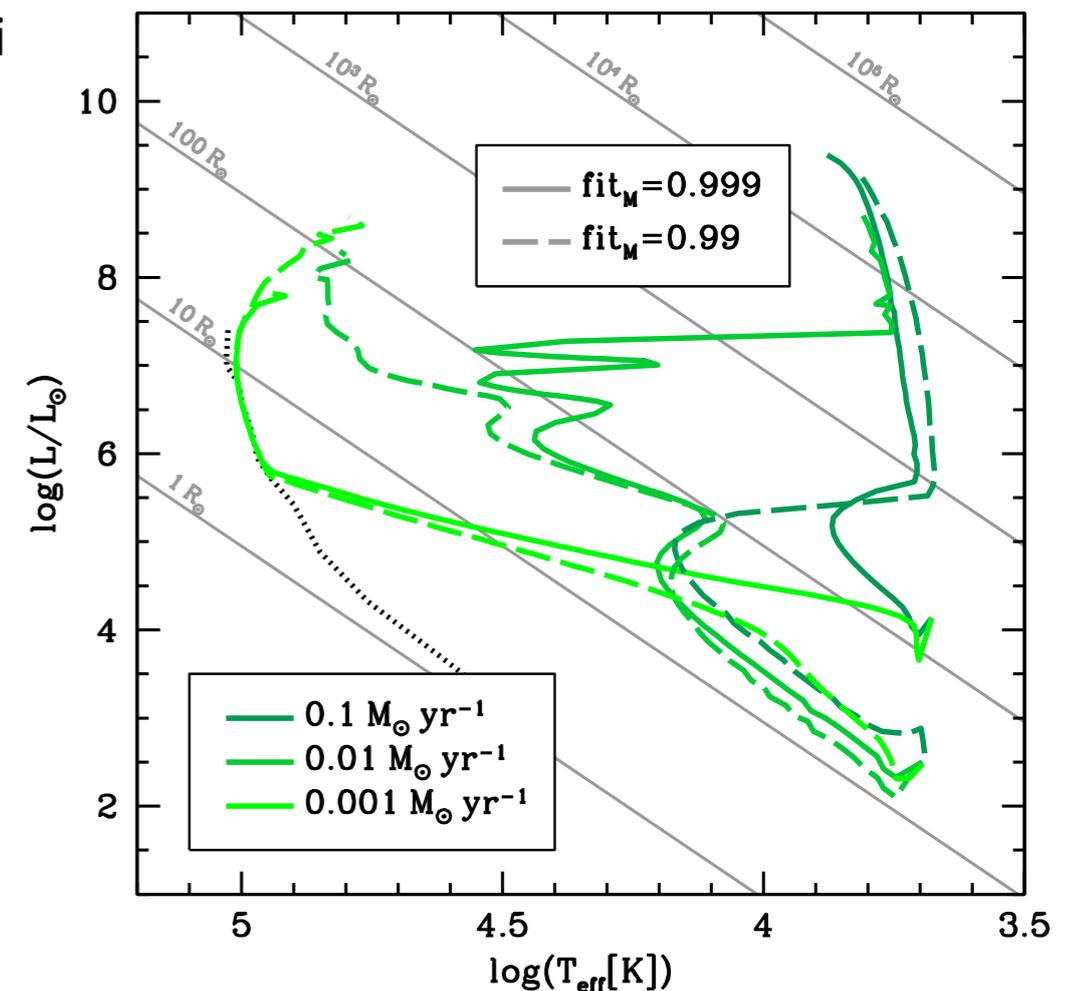
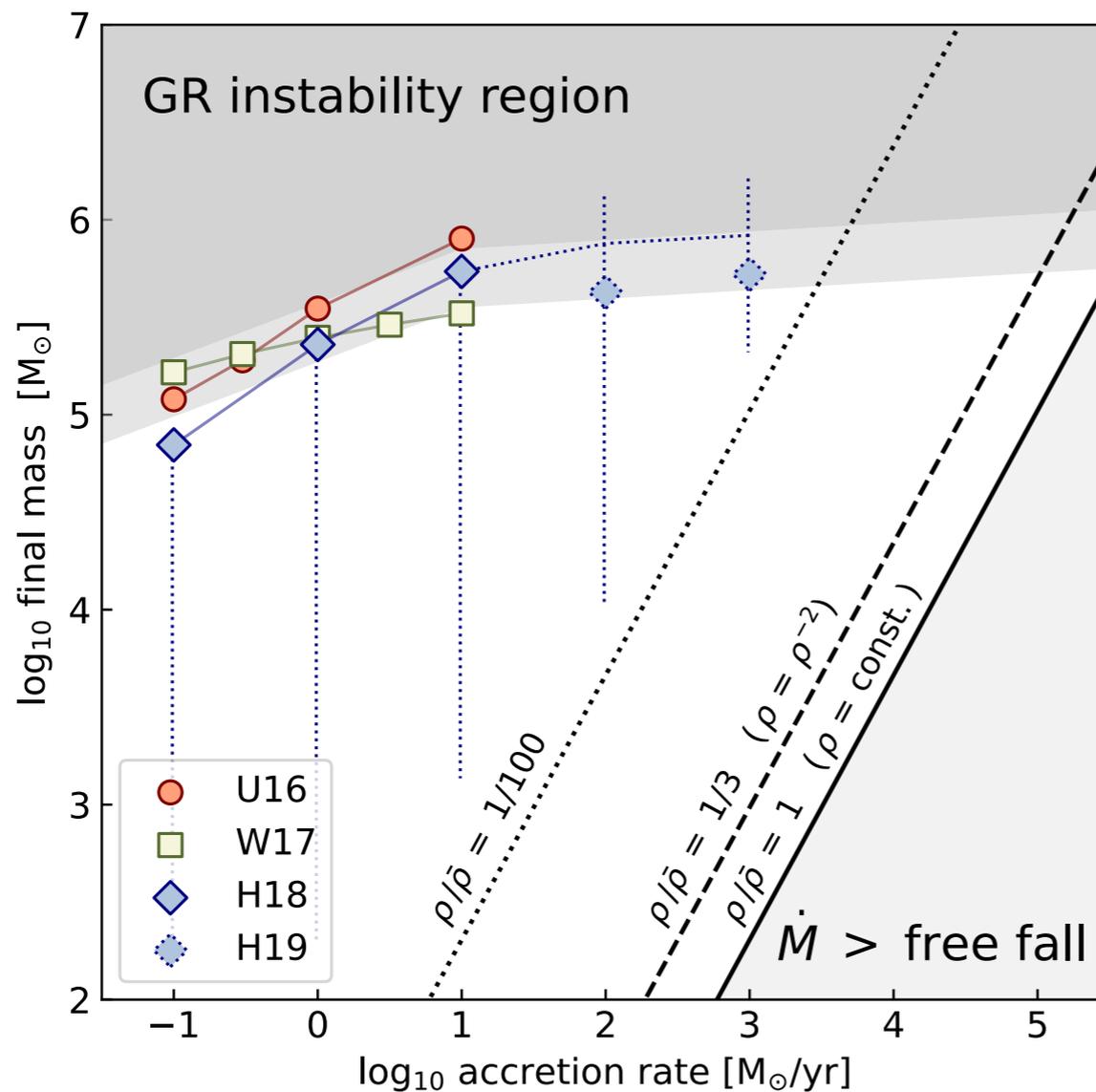


Figure 9. Evolutionary tracks of the models for the indicated accretion rates, for $\text{fit}_M = 0.999$ (solid lines) and 0.99 (dashed lines). The grey straight lines indicate the stellar radius, and the black dotted curve is the ZAMS of Schaerer (2002).

what is the maximum stellar mass possible?



- for accretion rate above 0.1 M_⊙/yr, stars can easily reach several 10⁵ M_⊙ before GR instability kicks in
- then they collapse directly into a black hole of the same mass
- while accreting the stars are extremely puffed up and cold (3000 - 4000 K)
- no ionizing radiation: hard to see, little impact

Haemmerlé (2020, A&A 644, A154)
 Haemmerlé (2021a, A&A 647, A83)
 Haemmerlé (2021b, A&A 650, A204)

Umeda et al. (2016, ApJ, 830, L34),
 Woods et al. (2017, ApJ, 842, L6),
 Haemmerlé et al. (2018, MNRAS, 474, 2757)

image from Klessen, & Glover (2023, ARAA, 61, 65)

we face a dilemma!



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to form SMS, we need

- (1) a sufficiently large mass reservoir ($M_{\text{gas}} \sim 10^6 M_{\odot}$)
- (2) maintain $\dot{M} \geq 0.1 M_{\odot}/\text{yr}$ for a sufficiently long time

then can reach masses above $10^5 M_{\odot}$ before the GR instability kicks in and they collapse into a BH...

BUT:

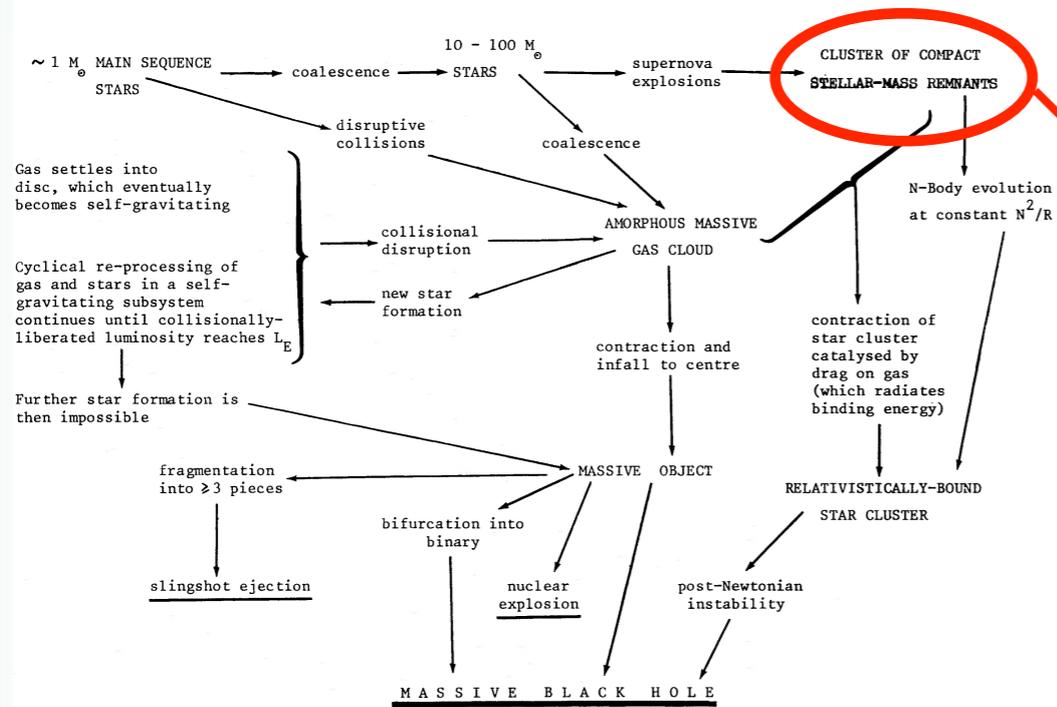
- (3) gas under these conditions will fragment!

WHAT IS THE WAY OUT?

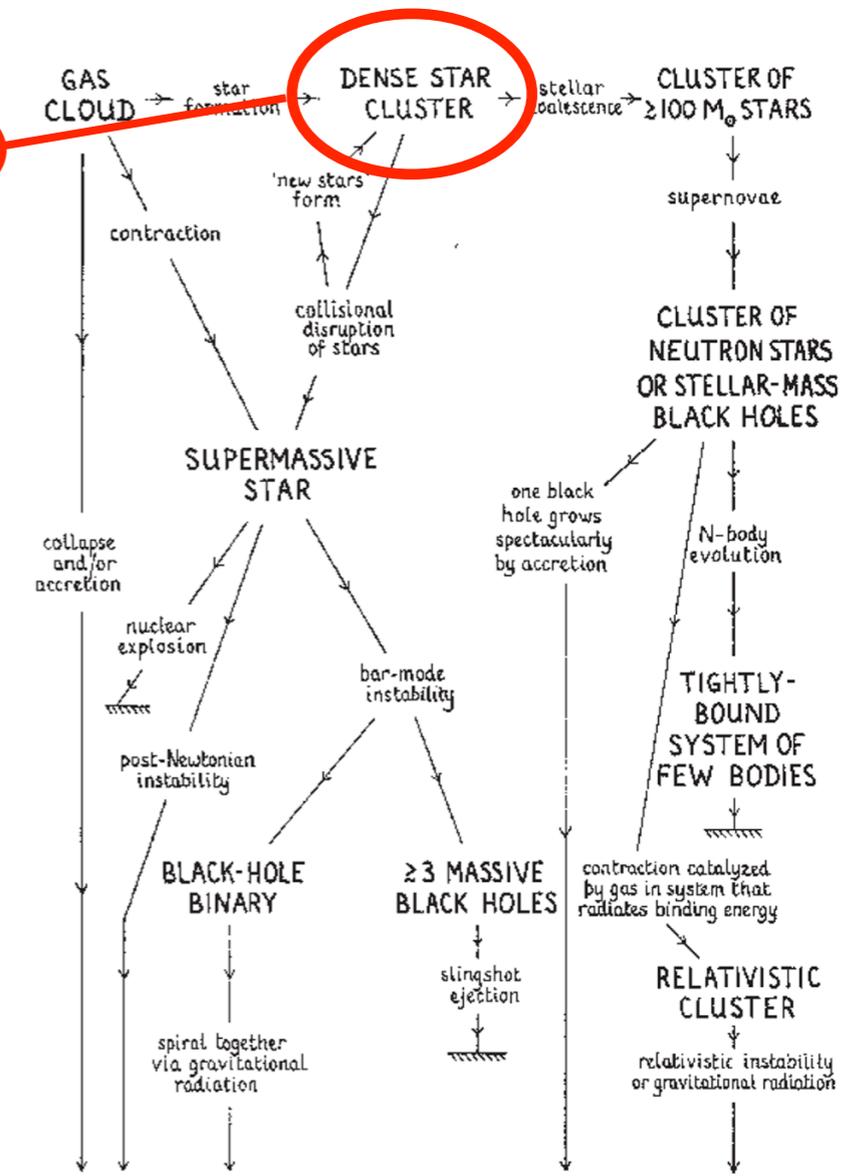
(proto)stellar clusters !!



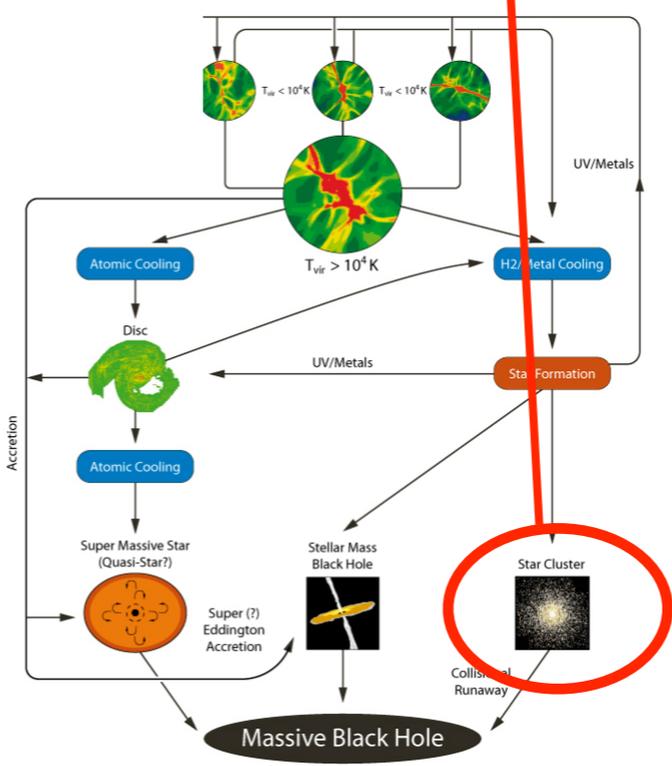
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CLUSTERS



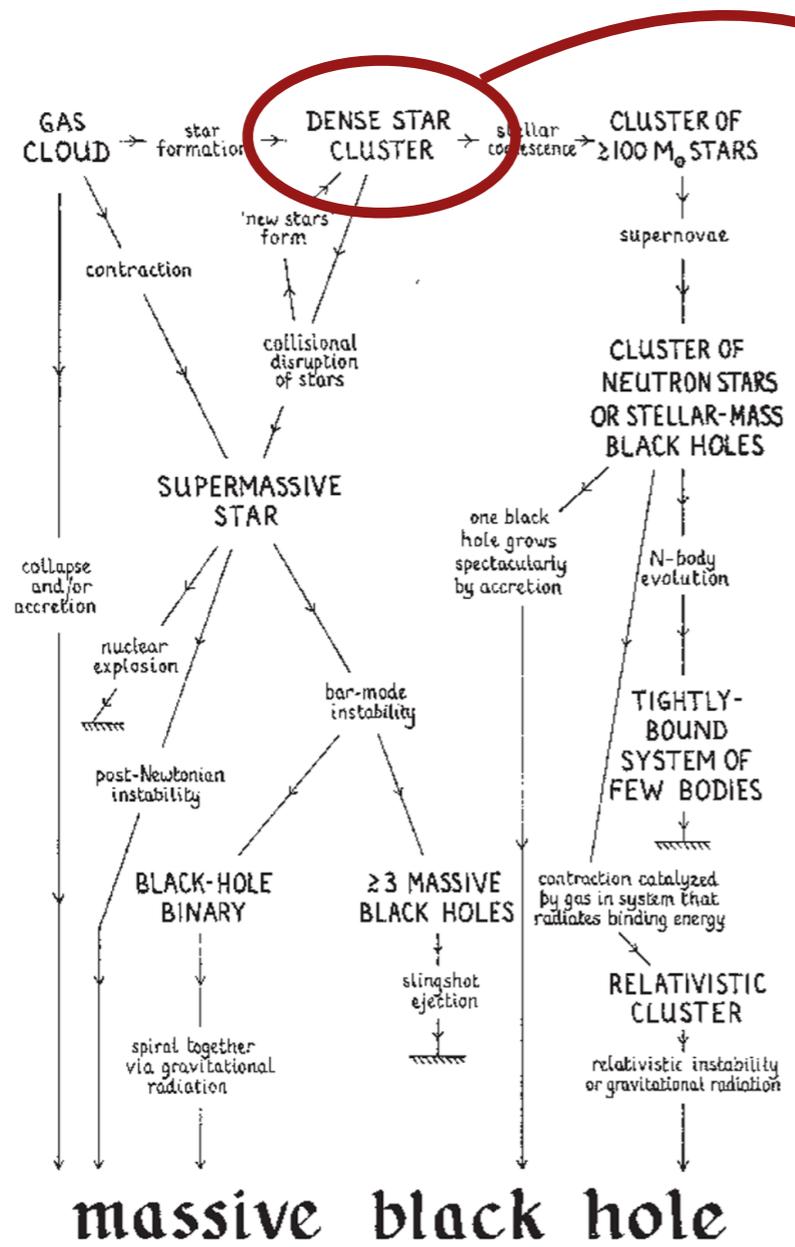
massive black hole



solution

Begelman & Rees (1978, MNRAS, 185, 847), Rees (1984, ARA&A, 22, 471),
Regan & Haehnelt (2009, MNRAS, 396, 343), Woods et al. (2019, PASA, 36, e027)

how to form seeds of supermassive BHs?



importance of run-away collisions and mergers in dense clusters

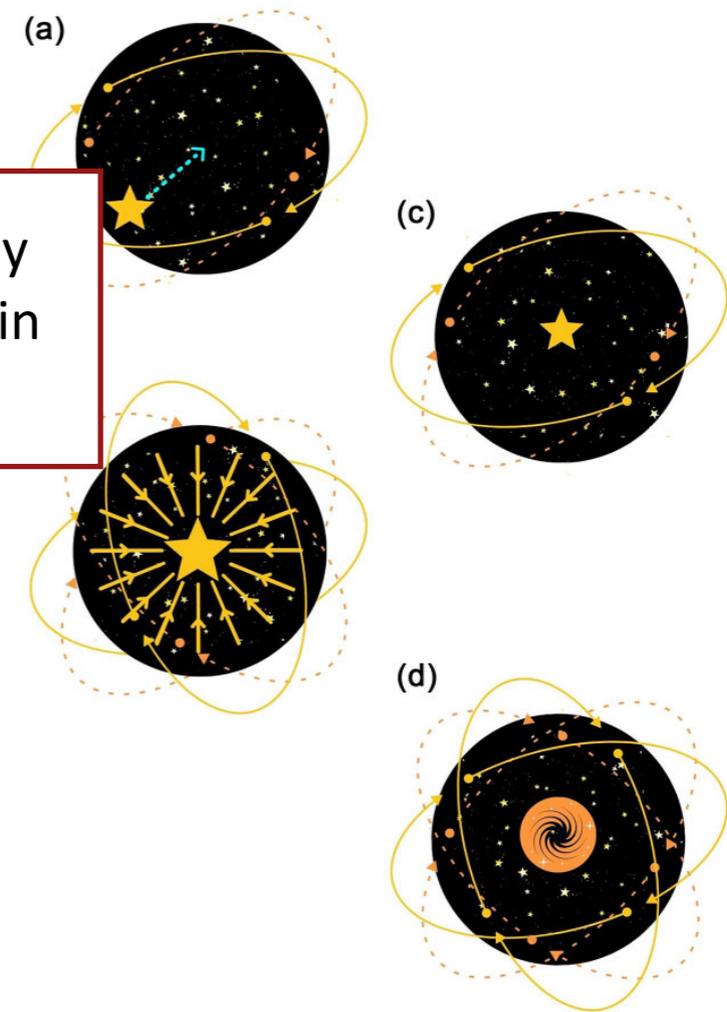


Figure 1. A sketch of the expected evolution of the stellar cluster and its central massive object. (a–b) The most massive star falls to the centre as a result of dynamical friction. (c) The most massive star in the centre accretes material through stellar collisions and from the gas. (d) The supermassive star collapses into a very massive black hole.

Figure 1. Original diagram from Rees (1978, 1984), outlining the possible formation pathways for supermassive black holes. In this review, as in the conference, our focus is on the left side of the diagram.

how to form seeds of supermassive BHs?



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clusters that form in massive and very dense gas clouds have

- (1) a sufficiently large mass reservoir ($M_{\text{gas}} \sim 10^6 M_{\odot}$)
- (2) individual stars have high accretion rates and evolve along large-R tracks

result is

- (3) combination of high stellar density and large stellar radii results in large collision rates
- (4) together this results in **run-away mass growth** of 1 or 2 objects to build SMS

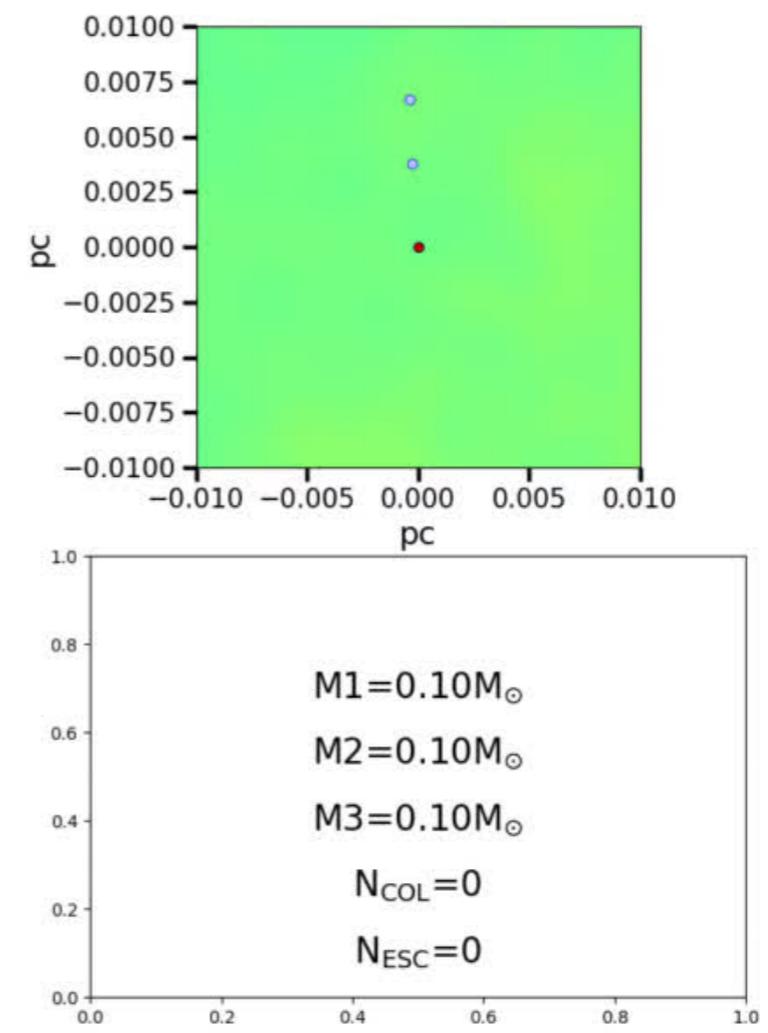
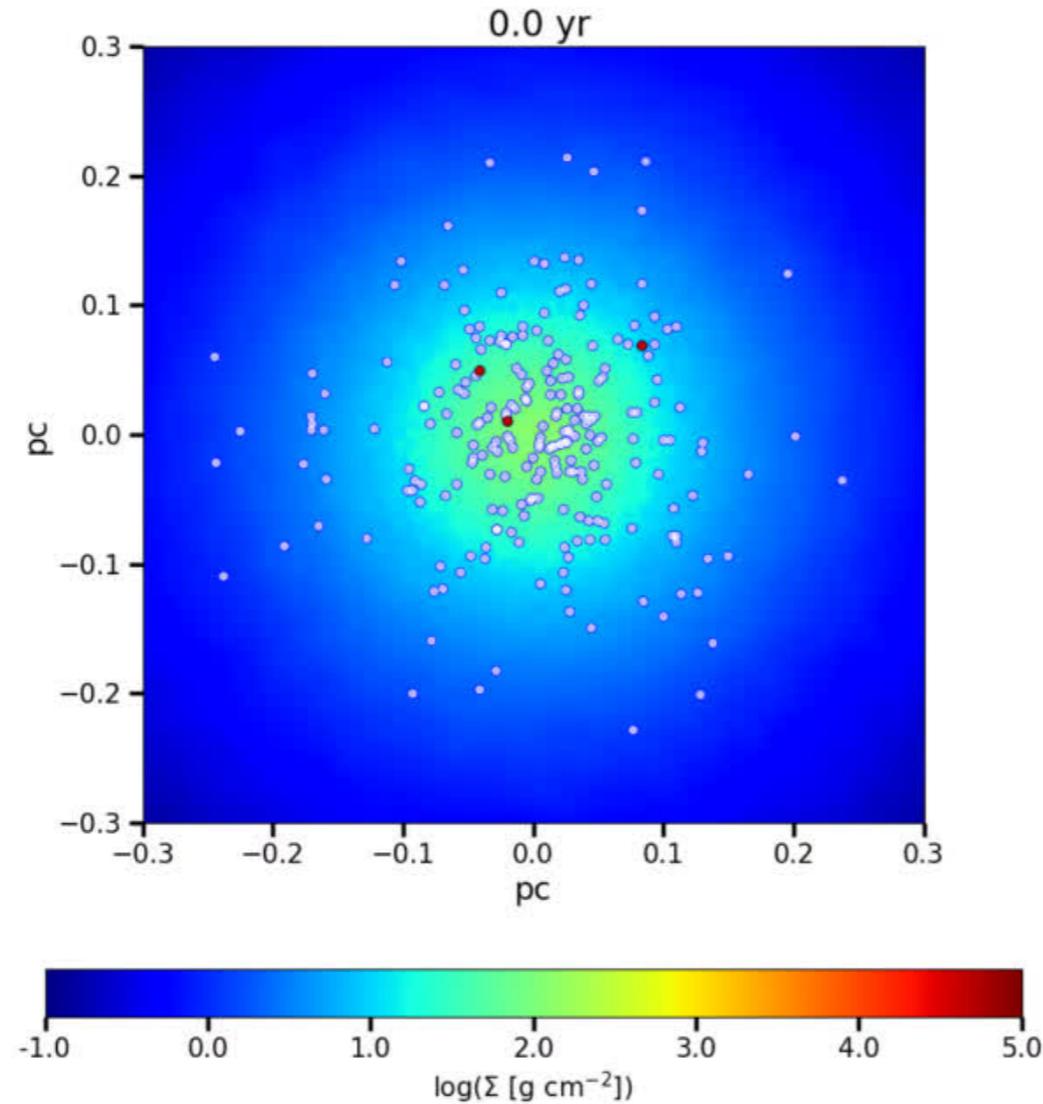
Reinoso et al. (2018, A&A, 614, A14), Boekhold et al. (2018, MNRAS, 476, 366), Alister Seguel et al. (2020, MNRAS, 493, 2352), Reinoso et al. (2020, A&A, 639, A92), Vergara et al. (2021, A&A, 649, A160), Schleicher et al. (2022, MNRAS, 512, 6192), Reinoso et al. (2023, MNRAS, 521, 3553), Schleicher et al. (2023, MNRAS, 521, 3972)

how to form seeds of supermassive BHs?

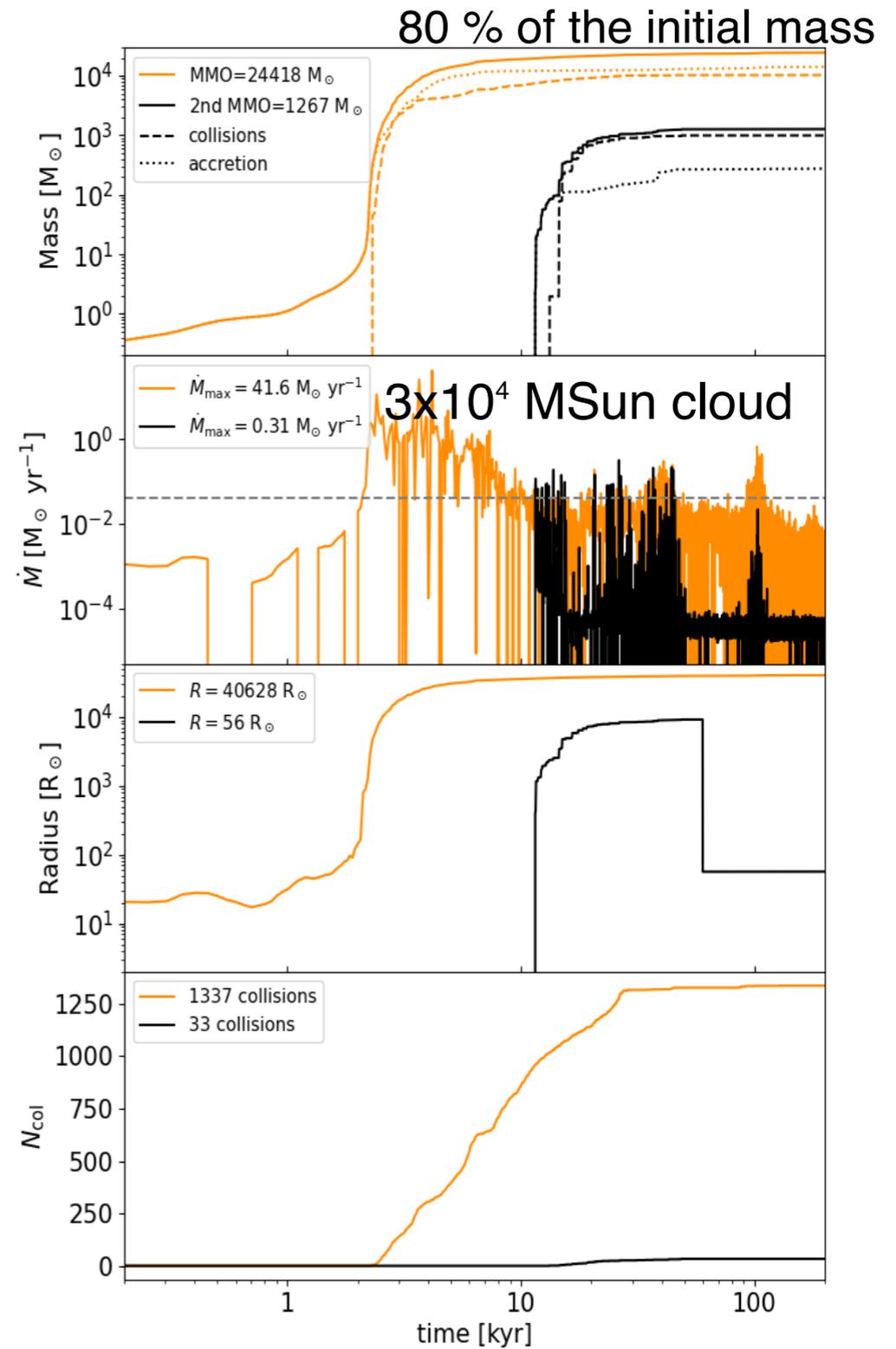
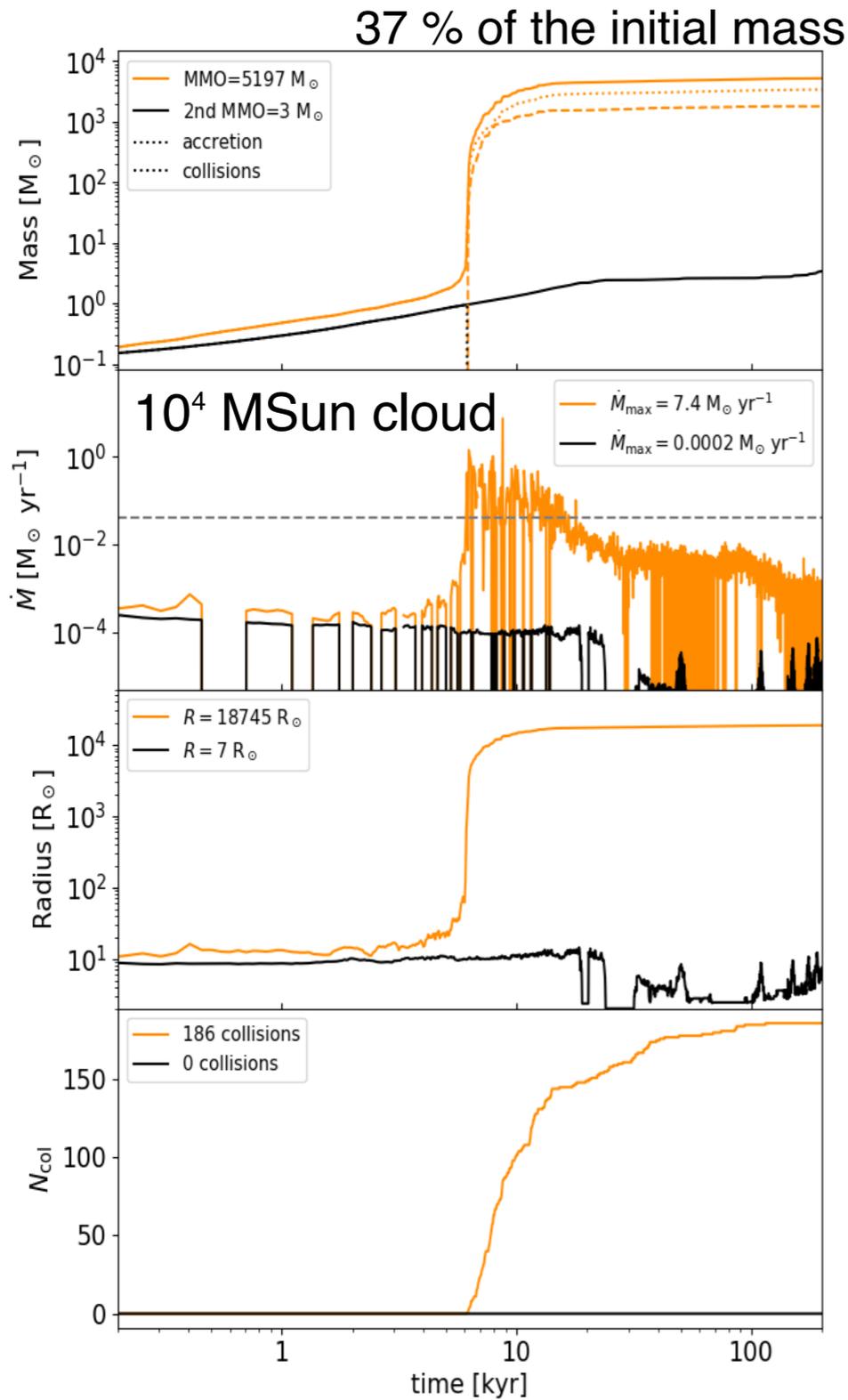


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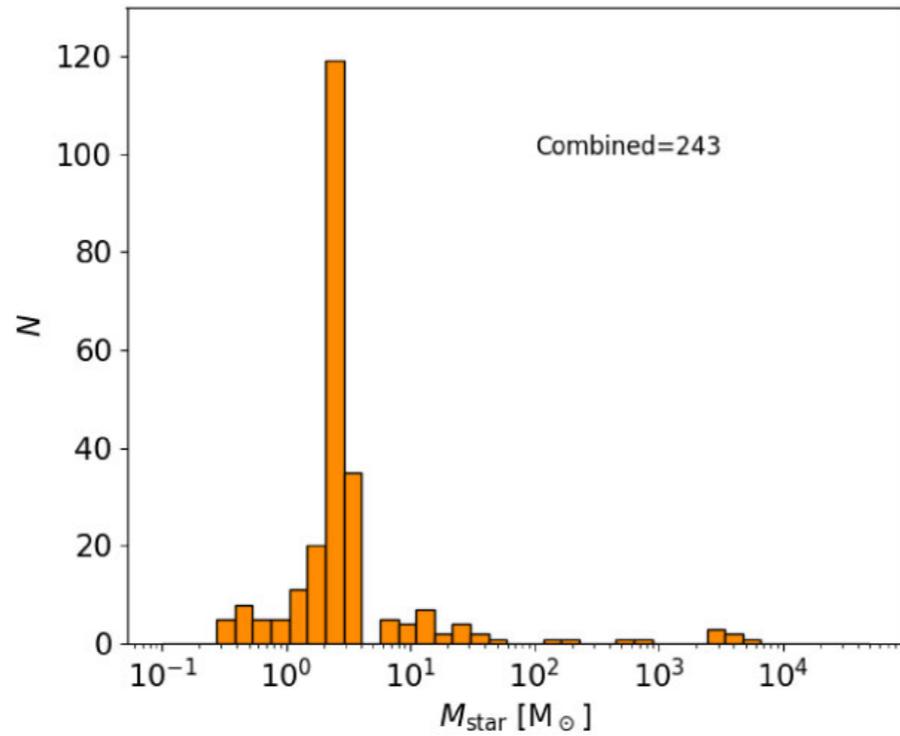
example of $10^4 M_{\odot}$ cloud



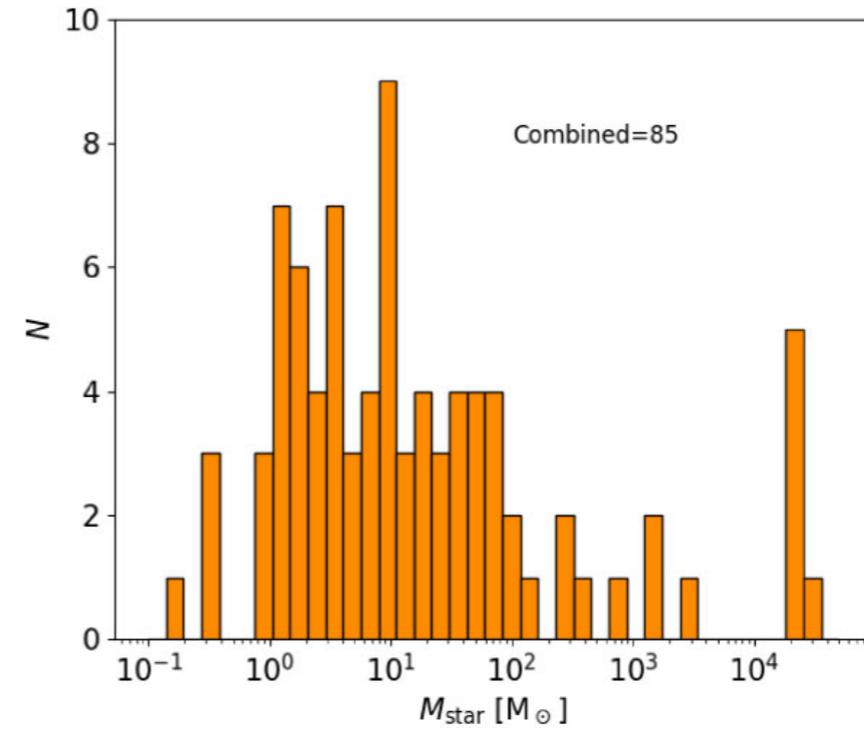
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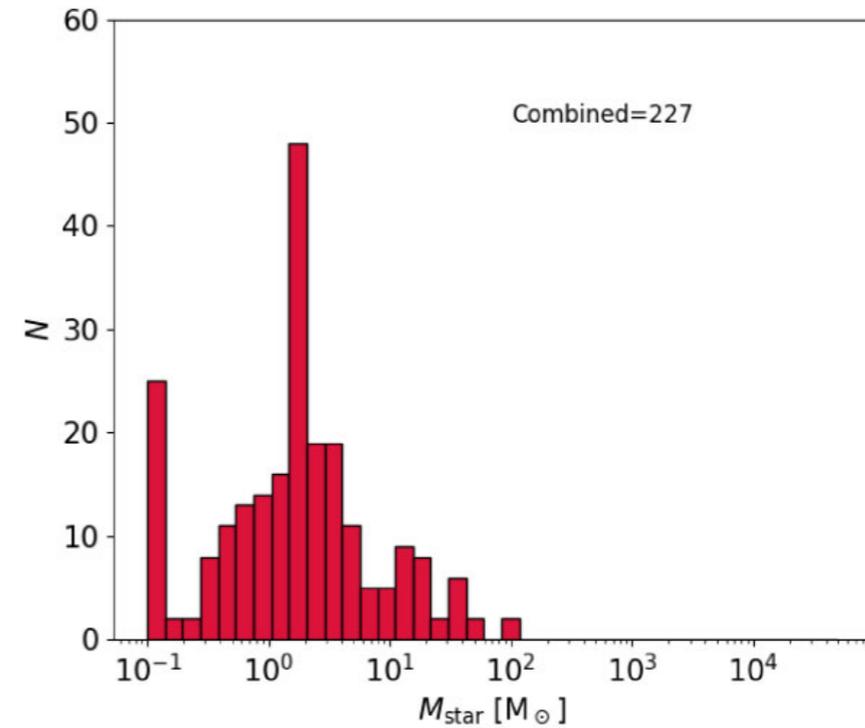
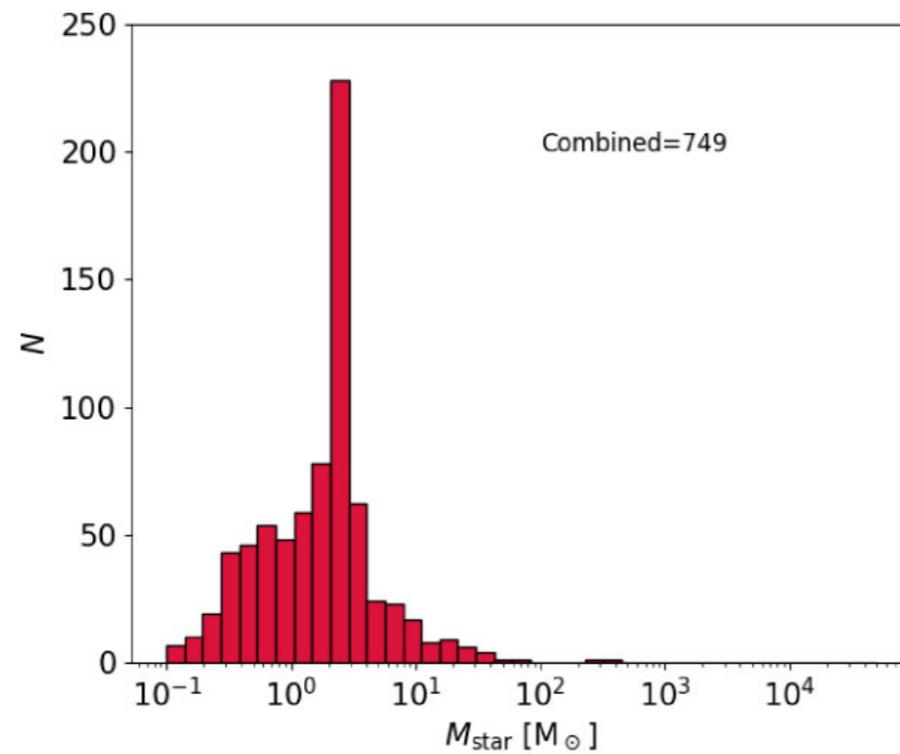
10^4 MSun cloud



3×10^4 MSun cloud



bound



ejected

all simulations combined

Reinoso et al. (2018, A&A, 614, A14), Boekhold et al. (2018, MNRAS, 476, 366), Alister Seguel et al. (2020, MNRAS, 493, 2352), Reinoso et al. (2020, A&A, 639, A92), Vergara et al. (2021, A&A, 649, A160), Schleicher et al. (2022, MNRAS, 512, 6192), Reinoso et al. (2023, MNRAS, 521, 3553), Schleicher et al. (2023, MNRAS, 521, 3972)

Table 1. Summary of simulation outcomes. We present for each simulation the initial gas mass, the final time, the quiescent time adopted for contraction to the main sequence for supermassive stars, the simulation outcome, the total accreted mass, the final stellar mass bound to the most massive object, the mass of the most massive object, the efficiency of massive object formation, the total mass in ejected stars, the number of stars bound to the MMO, the number of ejections and the number of collisions.

Simulation	M_{gas} [M_{\odot}]	t_{end} [yr]	$t_{\text{KH, surf}}$ [t_{KH}]	multiplicity	M_{accreted} [M_{\odot}]	$M_{\text{stellar, bound}}$ [M_{\odot}]	M_{MMO} [M_{\odot}]	ϵ	M_{ejected} [M_{\odot}]	N_{stars}	$N_{\text{ejections}}$	Collision number
M1_t100_1	10^4	200 015	100	single	5414	5305	5197	0.52	109	56	70	256
M1_t100_2	10^4	200 005	100	single	3815	3482	3311	0.33	333	62	112	288
M1_t100_3	10^4	200 043	100	single	4709	4539	3893	0.39	170	56	77	341
M1_t100_4	10^4	200 023	100	single	3730	3315	3048	0.30	415	48	153	291
M1_t100_5	10^4	200 017	100	binary	5854	4821	4096	0.41	1033	6	141	369
M1_t100_6	10^4	200 050	100	binary	4150	3326	2831	0.28	824	15	196	300
M1_t10_1	10^4	200 024	10	single	5397	4952	4326	0.43	445	66	83	343
M1_t10_2	10^4	120 045	10	single	4548	4377	4156	0.42	171	88	79	375
M1_t10_3	10^4	200 022	10	binary	6057	5297	4064	0.41	760	65	147	364
M1_t10_4	10^4	200 029	10	binary	5262	4468	2901	0.29	794	86	141	456
M1_t10_5	10^4	200 036	10	single	6804	6256	4858	0.49	548	89	53	412
M1_t10_6	10^4	112 701	10	single	4617	4255	4135	0.41	362	56	119	301
M3_t100_1	3×10^4	200 021	100	single	26 108	25 808	24 418	0.81	300	13	42	1892
M3_t100_2	3×10^4	200 043	100	single	26 939	26 898	26 890	0.90	41	10	19	1842
M3_t100_3	3×10^4	200 009	100	single	26 388	26 211	24 577	0.82	177	11	34	2547
M3_t100_4	3×10^4	200 038	100	single	23 312	22 850	20 365	0.68	462	36	53	1844
M3_t100_5	3×10^4	200 034	100	single	23 070	22 973	22 618	0.75	97	12	50	2215
M3_t100_6	3×10^4	200 035	100	single	26 966	26 851	24 375	0.81	115	3	29	2522
M3_t10_1	3×10^4	200 008	10	single	20 981	20 831	20 435	0.68	150	13	70	2283
M3_t10_2	3×10^4	200 026	10	single	23 451	23 063	20 776	0.69	388	32	61	1807
M3_t10_3	3×10^4	200 048	10	single	25 871	25 413	22 267	0.74	458	6	50	2354
M3_t10_4	3×10^4	200 014	10	single	22 585	21 889	21 733	0.72	696	10	89	2445
M3_t10_5	3×10^4	200 039	10	single	20 778	20 481	20 368	0.68	297	6	96	2297
M3_t10_6	3×10^4	200 011	10	single	27 051	26 846	26 746	0.89	205	7	42	3514

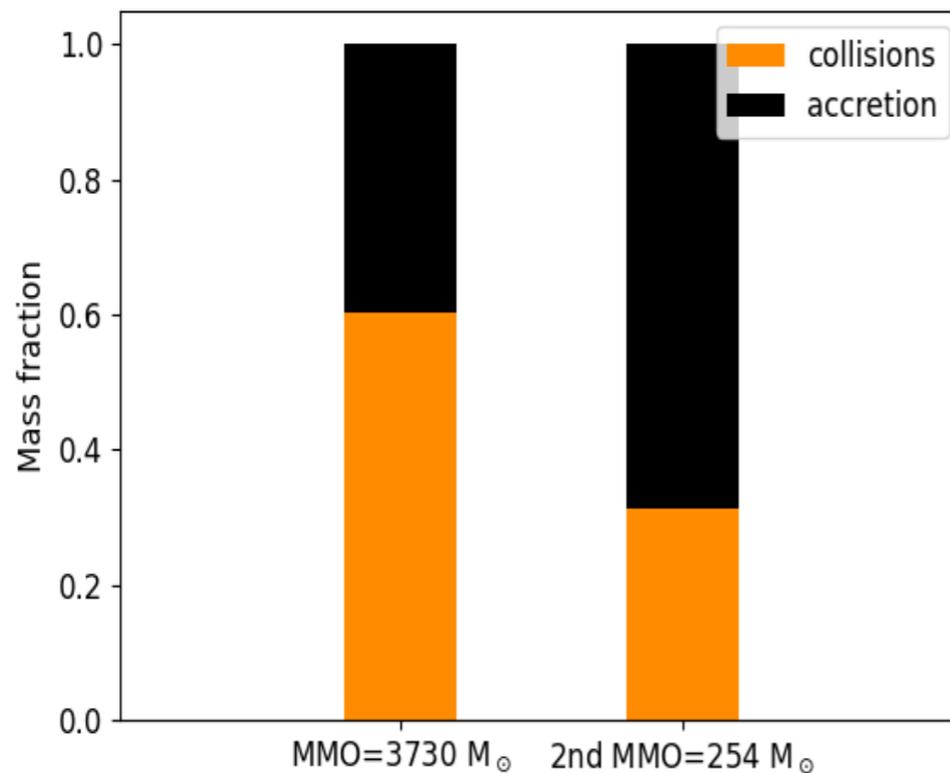
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combination of collisions and accretion



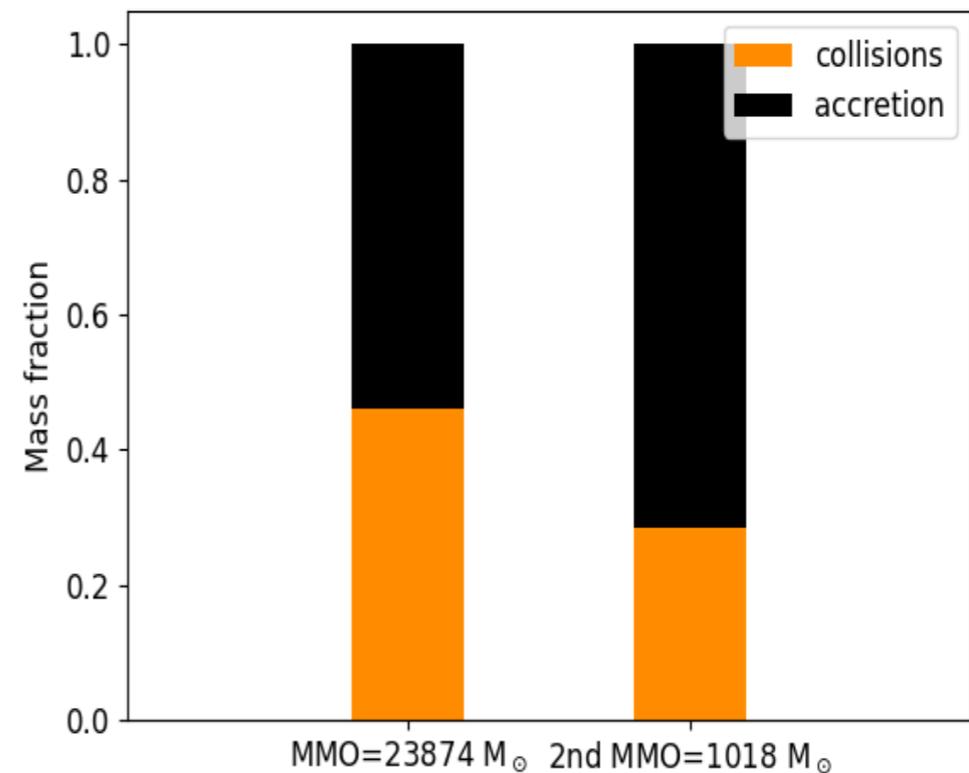
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10^4 MSun cloud



60% of the mass
comes from collisions

3×10^4 MSun cloud



40% of the mass
comes from collisions

Reinoso et al. (2018, A&A, 614, A14), Boekhold et al. (2018, MNRAS, 476, 366), Alister Seguel et al. (2020, MNRAS, 493, 2352), Reinoso et al. (2020, A&A, 639, A92), Vergara et al. (2021, A&A, 649, A160), Schleicher et al. (2022, MNRAS, 512, 6192), Reinoso et al. (2023, MNRAS, 521, 3553), Schleicher et al. (2023, MNRAS, 521, 3972)



constraints



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observational constraints



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- directly observing Pop III stars at high redshift is highly challenging
 - maybe SNe with JWST, but where to point
 - this may help to constrain the high-mass end of Pop III IMF
- more promising: Galactic archeology
 - maybe we find genuine low-mass Pop III stars (0.8 Msun should have survived until present day)
 - use detailed abundance pattern in EMP stars to high-mass end constrain high-mass end of IMF (no evidence of PISNe)
- very exciting: gravitational wave events
 - binary properties and high-mass end of Pop III IMF
- other testable expectation:
 - larger stellar density in clusters of lower metallicity, consequently: larger numbers of close binaries (and higher-order multiples)

(for further discussions, see Klessen, & Glover (2023, ARAA, 61, 65 -- arXiv.2303.12500)



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IMF of Pop III stars is not well understood
most likely log-flat and thus top heavy

transition to Pop II star formation at metallicities
 $\log(Z/Z_{\text{sun}}) \sim -5$ due to dust

supermassive stars can easily reach
 $10^5 M_{\odot}$ if subject to high accretion rates

best constraints to be expected from
Galactic archeology and gravitational waves



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thanks

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